MT Review Search

Q1. They See Me Rolling (Search Problem)

Pacman buys a car to start Rolling in the Pac-City! But driving a car requires a new set of controls because he can now travel faster than 1 grid per turn (second). Instead of solely moving [North, South, East, West, Stop], Pacman's car has two distinct integers to control: throttle, and steering.

Throttle: $t_i \in \{1,0,-1\}$, corresponding to {Gas, Coast, Brake}. This controls the **speed** of the car by determining its acceleration. The integer chosen here will be added to his velocity for the next state. For example, if Pacman is currently driving at 5 grid/s and chooses Gas he will be traveling at 6 grid/s in the next turn.

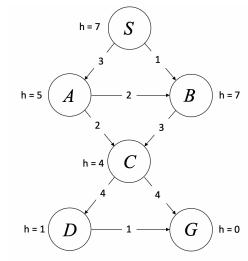
Steering: $s_i \in \{1, 0, -1\}$, corresponding to {Turn Left, Neutral, Turn Right}. This controls the **direction** of the car. For example, if he is facing North and chooses Turn Left he will be facing West in the next turn.

ne e	at. For example, if he is facing fvorth and chooses full Left he will be facing west in the next turn.						
(a)	(a) Suppose Pac-city has dimension m by n , but only $k < mn$ squares are legal roads. The speed limit Pac-city is 3 grid/s. For this sub-part only, suppose Pacman is a law-abiding citizen, so $0 \le v \le 3$ at a time, and he only drives on legal roads.						
	(i) Without any additional information, what is the tightest upper bound on the size of state space, if he wants to search a route (not necessarily the shortest) from his current location to anywhere in the city. Please note that your state space representation must be able to represent all states in the search space.						
	$\bigcirc 4mn \bigcirc 4k \bigcirc 12mn \bigcirc 12k \bigcirc 16mn \bigcirc 16k \bigcirc 48mn \bigcirc 48k$						
	(ii) What is the maximum branching factor? The answer should be an integer.						
	 (iii) Which algorithm(s) is/are guaranteed to return a path between two points, if one exists? □ Depth First Tree Search □ Depth First Graph Search □ Breadth First Graph Search 						
	(iv) Is Breadth First Graph Search guaranteed to return the path with the shortest grid distance? Yes No						
(b)	Now let's remove the constraint that Pacman follows the speed limit. Now Pacman's speed is limited by the mechanical constraints of the car, which is 6 grid/s, double the speed limit.						
	Pacman is now able to drive twice as fast on the route to his destination. How do the following properties of the search problem change as a result of being able to drive twice as fast? (i) Size of State Space:						
	O Increases O Stays the same O Decreases						
	(ii) Maximum Branching Factor: O Increases O Stays the same O Decreases						
	For the following part, mark all choices that could happen on any graph						
	(iii) The number of nodes expanded with Depth First Graph Search: ☐ Increases ☐ Stays the same ☐ Decreases						

(c)	Now we need to consider that there are $p > 0$ police cars waiting at $p > 0$ distinct locations trying to catch Pacman riding dirty!! All police cars are stationary, but once Pacman takes an action which lands him in the same grid as one police car, Pacman will be arrested and the game ends.							
	Pacman wants to find a route to his destination, without being arrested. How do the following properties of the search problem change as a result of avoiding the police?							
	(i) Size of State Space: O Increases O Stays the same O Decreases							
	(ii) Maximum Branching Factor: ○ Increases ○ Stays the same ○ Decreases							
	For the following part, mark all choices that could happen on any graph (iii) Number of nodes expanded with Breadth First Graph Search: □ Increases □ Stays the same □ Decreases							

Q2. Search Algorithms Potpourri

(a) We will investigate various search algorithms for the following graph. Edges are labeled with their costs, and heuristic values h for states are labeled next to the states. S is the start state, and G is the goal state. In all search algorithms, assume ties are broken in alphabetical order.



- (i) Select all boxes that describe the given heuristic values.
 - ☐ Neither ☐ admissible ☐ consistent
- (ii) Given the above heuristics, what is the order that the states are going to be expanded in, assuming we run A* graph search with the heuristic values provided.

Index	1	2	3	4	5	Not Expanded
\mathbf{S}	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	
A	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
В	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
\mathbf{C}	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
D	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
G	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	

- (iii) Assuming we run A* graph search with the heuristic values provided, what path is returned?
 - $\bigcirc \quad S \to A \to B \to C \to D \to G \qquad \bigcirc \quad S \to A \to C \to G \qquad \bigcirc \quad S \to A \to C \to D \to G$
 - $\bigcirc S \to A \to C \to D \to G \qquad \bigcirc S \to A \to C \to D \to G$
 - O None of the above
- (iv) Given the above heuristics, what is the order that the states are going to be expanded in, assuming we run greedy graph search with the heuristic values provided.

Index	1	2	3	4	5	Not Expanded
\mathbf{S}	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	
A	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
В	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
$^{\mathrm{C}}$	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
D	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
G	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc

- (v) What path is returned by greedy graph search?
 - $\bigcirc S \rightarrow A \rightarrow B \rightarrow C \rightarrow D \rightarrow G \qquad \bigcirc S \rightarrow A \rightarrow C \rightarrow G \qquad \bigcirc S \rightarrow A \rightarrow C \rightarrow D \rightarrow G \\ \bigcirc S \rightarrow A \rightarrow C \rightarrow D \rightarrow G \qquad \bigcirc S \rightarrow A \rightarrow C \rightarrow D \rightarrow G \qquad \bigcirc None of the above$

(b)	Consider a complete graph, K_n , the undirected graph with n vertices where all n vertices are connected (there is an edge between every pair of vertices), resulting in $\binom{n}{2}$ edges. Please select the maximum possible depth of the resulting tree when the following graph search algorithms are run(assume any possible start and goal vertices).								
		1	$\lceil \frac{n}{2} \rceil$	n-1	$\binom{n}{2}$	None of the above			
	BFS		\bigcirc	\bigcirc	\bigcirc	None of the above			
	DFS		\bigcirc	\bigcirc	\bigcirc	0			
(c)	(c) Given two admissible heuristics h_A and h_B . (i) Which of the following are guaranteed to also be admissible heuristics?								
	(ii) Consider performing A* tree search. Which is generally best to use if we want to expand the fewest number of nodes?								
	$ \bigcirc h_A + h_B \bigcirc \frac{1}{2}(h_A + h_B) $	(n_A)	$\frac{1}{2}(h_{I})$	3)	$\frac{1}{2}(h_A$	$(A + h_B)$ \bigcirc $(A * h_B)$ \bigcirc $(A * h_B)$			
(d)	d) Consider performing tree search for some search graph. Let $depth(n)$ be the depth of search node n and $cost(n)$ be the total cost from the start state to node n . Let G_d be a goal node with minimum depth, and G_c be a goal node with minimum total cost.								
	(i) For iterative deepening (where we repeatedly run DFS and increase the maximum depth allowed by 1), mark all conditions that are guaranteed to be true for every node n that could be expanded during the search, or mark "None of the above" if none of the conditions are guaranteed.								
	$ \Box cost(n) \leq cost(G_c) \Box cost(n) \leq cost(G_d) \Box depth(n) \leq depth(G_c) \Box depth(n) \leq depth(G_d) \bigcirc None of the above $								
	(ii) What is necessarily true regarding iterative deepening on any search tree?								
	☐ Complete as opposed to DFS tree search ☐ Strictly faster than DFS tree search ☐ Strictly faster than BFS tree search ☐ More memory efficient than BFS tree search ☐ A type of stochastic local search ☐ None of the above								