Q1. CSP: Air Traffic Control

We have five planes: A, B, C, D, and E and two runways: international (28L/28R) and domestic (1L/1R) (simplified from the SFO runway configuration). We would like to schedule a time slot and runway for each aircraft to **either** land or take off. We have four time slots: {1,2,3,4} for each runway, during which we can schedule a landing or take off of a plane. We must find an assignment that meets the following constraints:

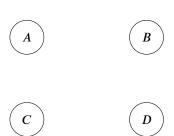
- Plane B has lost an engine and must land in time slot 1.
- Plane D can only arrive at the airport to land during or after time slot 3.
- Plane A is running low on fuel but can last until at most time slot 2.
- Plane D must land before plane C takes off, because some passengers must transfer from D to C.
- No two aircrafts can reserve the same time slot for the same runway.
- (a) Complete the formulation of this problem as a CSP in terms of variables, domains, and constraints (both unary and binary). Constraints should be expressed implicitly using mathematical or logical notation rather than with words.

Variables: A, B, C, D, E for each plane.	Domains:	
Constraints: (you do not have to use all	ll lines)	
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- (b) For the following subparts, we add the following two constraints:
 - Planes A, B, and C cater to international flights and can only use the international runway.
 - Planes D and E cater to domestic flights and can only use the domestic runway.
 - (i) With the addition of the two constraints above, we completely reformulate the CSP. You are given the variables and domains of the new formulation. Complete the constraint graph for this problem given the original constraints and the two added ones.

Variables: A, B, C, D, E for each plane. **Constraint Graph:**

Domains: $\{1, 2, 3, 4\}$



(E)

(ii) What are the domains of the variables after enforcing arc-consistency? Begin by enforcing unary constraints. (Cross out values that are no longer in the domain.)

A | 1 2 3 4 B | 1 2 3 4 C | 1 2 3 4 D | 1 2 3 4 E | 1 2 3 4

(iii) Arc-consistency can be rather expensive to enforce, and we believe that we can obtain faster solutions using only **forward-checking** on our variable assignments. Using the Minimum Remaining Values heuristic, perform backtracking search on the graph, breaking ties by picking lower values and characters first. List the (*variable*, *assignment*) pairs in the order they occur (including the assignments that are reverted upon reaching a dead end). Enforce unary constraints before starting the search.

(You don't have to use this table, it won't be graded.)

2 3 Α 2 3 В 1 4 2 \mathbf{C} 1 3 D 1 2 3 Ε 2 3 1

Answer:

(c) Suppose we have just one runway and *n* planes, where no two planes can use the runway at once. We are assured that the constraint graph will always be tree-structured and that a solution exists. What is the runtime complexity in terms of the number of planes, *n*, of a CSP solver that runs arc-consistency and then assigns variables in a topological ordering?

 \bigcirc O(1)

 \bigcirc O(n)

 \bigcirc $O(n^2)$

 \bigcirc $O(n^3)$

 \bigcirc $O(n^n)$

O None of the Above

Q2. CSPs

In this question, you are trying to find a four-digit number s	satisfying the following conditions:
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in this question, you are trying	to mid a four digit mamoer s	ansiging the following condition	
1. the number is odd,			
2. the number only contains the	e digits 1, 2, 3, 4, and 5,		
3. each digit (except the leftmo	st) is strictly larger than the	digit to its left.	
can choose from. The las	t variable only has 1, 3, and		d the domains are the five digits we er must be odd. The constraints are thms, the domains are
12345	12345	12345	1 2 3 4 5
(i) Before assigning an arc consistency is en	_	ncy. Write the values remaining i	n the domain of each variable after
The secon The third The fourth (iii) Now suppose we ass	digit n digit (rightmost) sign to the leftmost digit first	•	tering by enforcing arc consistency, st digit? Break ties from large (5)
number be after one	_	=	ith the number 1332, what will our from left to right, and break value
(b) The following questions a binary constraints unless		ne above parts. Assume for these	following questions, there are only
(i) [true or false] When	•		main when the algorithm terminates
(ii) [true or false] Once	-	ed as a pre-processing step, for	ward checking can be used during
(iii) In a general CSP with arc consistency using		possible values, what is the wors	t case time complexity of enforcing

imber of times a back-
an assignment, partial
exists?
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track in a general CSP,
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