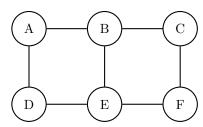
$\square$  A

## Q1. Worst-Case Backtracking

Consider solving the following CSP with standard backtracking search where we enforce arc consistency of all arcs before every variable assignment. Assume every variable in the CSP has a domain size d > 1.



(a)	For each of the variable orderings, mark the variables for which backtracking search (with arc consistency checking) could end up considering more than one different value during the search. (i) Ordering: $A,B,C,D,E,F$											
	☐ A (ii) Ordering	$\square B$ g: $B, D, F, E, C,$	$\square$ $C$	$\Box$ D	$\Box E$	$\Box F$						
		$\Box B$	$\square$ $C$	$\Box$ D	$\Box$ E	$\Box F$						
(b)	<ul> <li>b) Now assume that an adversary gets to observe which variable ordering you are using, and after doing so chooses to add one additional binary constraint between any pair of variables in the CSP to maximize the number of backtracking variables in the worst case. For each of the following variable orderings select which additional binary constraint the adversary should add. Then, mark the variables for which backtracking search (with arc consistency checking) could end up considering more than one different value when solving the modified CSP.</li> <li>(i) Ordering: A, B, C, D, E, F The adversary should add the additional binary constraint:</li> </ul>											
	0	AC	$\bigcirc$ AE	$\bigcirc$ A		$\bigcirc$ BD						
	O	BF	$\bigcirc$ $CD$	$\bigcirc$ $C$	E	$\bigcirc$ DF						
	When so	lving the modifi	ed CSP with this o	rdering, backtracki	ng might occur at:							
	$\square$ A	$\square$ B	$\square$ C	$\square$ D	$\square$ E	$\square$ $F$						
	(ii) Ordering: $B, D, F, E, C, A$ The adversary should add the additional binary constraint:											
	$\bigcirc$	AC	$\bigcirc$ AE	$\bigcirc$ A	F	$\bigcirc$ $BD$						
	$\circ$	BF	$\bigcirc$ $CD$	$\bigcirc$ $C$	E	$\bigcirc$ DF						
	When solving the modified CSP with this ordering, backtracking might occur at:											

 $\square$  D

 $\square$  E

 $\square$  F

 $\square$  C

 $\square$  B

## Q2. CSPs: Potluck Pandemonium

1. Pho

The potluck is coming up and the staff haven't figured out what to bring yet! They've pooled their resources and determined that they can bring some subset of the following items.

2.	apricots										
3.	rozen Yogurt										
4.	ried Rice										
5.	apple Pie										
6.	animal Crackers										
	are five people on the course staff: Taylor, Jonathan, Faraz, Brian, and Alvin. Each of them will only one item to the potluck.										
i.	f (F)araz brings the same item as someone else, it cannot be (B)rian.										
ii.	A)lvin has pho-phobia so he won't bring Pho, but he'll be okay if someone else brings it.										
iii.	(B)rian is no longer allowed near a stove, so he can only bring items 2, 3, or 6.										
iv.	(F)araz literally can't even; he won't bring items 2, 4, or 6.										
v.	(J) on a than was busy, so he didn't see the last third of the list. Therefore, he will only bring item 1, 2, 3, or 4.										
vi.	(T)aylor will only bring an item that is before an item that (J)onathan brings.										
vii.	$\Gamma$ )aylor is allergic to animal crackers, so he won't bring item 6. (If someone else brings it, he'll just stay way from that table.)										
viii.	F)araz and (J)onathan will only bring items that have the same first letter (e.g. Frozen Yogurt and Fried tice).										
ix.	B) rian will only bring an item that is after an item that (A) lvin brings on the list.										
х.	J)onathan and (T)aylor want to be unique; they won't bring the same item as anyone else.										
(a)	Which of the listed constraints are unary constraints? $\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$										
	□ vi □ vii □ viii □ ix □ x										
(b)	Rewrite implicit constraint viii. as an explicit constraint.										

(c)	How many edg	ges are	ther	re in	the	cons	train	t gra	ph f	or th	is CS	SP?								
( <b>1</b> )								a.												
(d)	The table belo	w sho	ws tł	ne va	riabl –	le do	main	_		ll una			aints	s hav	e be	en er	forc€	ed.		
						Α		2	3	4	5	6								
						В		2	3			6								
						${f F}$	1		3		5									
						J	1	2	3	4										
						$\mathbf{T}$	1	2	3	4	5									
	Following the	MRV	heuri	istic,	whi	ch va	riab	le sh	ould	we a	ssign	first	t? Bi	reak	all t	ies al	phab	etically	J.	
	O	A		,		$\bigcirc$	В				_	F				) J	•	·	$\bigcirc$	Т
(e)	To decouple this from the previous question, assume that we choose to assign (F)araz first. In this question, we will choose which value to assign to using the Least Constraining Value method.  To determine the number of remaining values, enforce arc consistency to prune the domains. Then, count the total number of possible assignments ( <b>not</b> the total number of remaining values). It may help you to enforce arc consistency twice, once before assigning values to (F)araz, and then again after assigning a value.									unt you										
	<ul><li>(i) Assigning</li><li>(ii) Assigning</li></ul>																			
	(iii) Assigning	_																	_	_
	(iv) Using the	e LCV 1	metl		whice		lue s	hould	we 3	_	n to	F'? If	ther $4$	e is a	i tie,	choc	se th $5$	e lower	numb	ber. ) 6
	Extra tables for		k:		) <u> </u>	_			) O	•			, <u>1</u>				0			, 0
	211010 1005105 1	A		2	3	4	5	6	Γ	$\overline{\mathbf{A}}$		2	3	4	5	6				
		В		$\frac{2}{2}$	3	_		6		В		$\frac{2}{2}$	3	_		6				
		F	1	_	3		5		+	$\overline{\mathbf{F}}$	1	-	3		5					
		J	1	2	3	4			-	$\overline{\mathbf{J}}$	1	2	3	4						
		$\frac{\mathbf{J}}{\mathbf{T}}$	1	$\frac{2}{2}$	3	4	5			$\frac{\mathbf{J}}{\mathbf{T}}$	1	$\frac{2}{2}$	3	4	5					
														<b>T</b>						
		<b>A</b>		_	0	4	_	0		_			0	4						

$\mathbf{A}$		2	3	4	5	6
В		2	3			6
$\mathbf{F}$	1		3		5	
J	1	2	3	4		
$\mathbf{T}$	1	2	3	4	5	

$\mathbf{A}$		2	3	4	5	6
В		2	3			6
$\mathbf{F}$	1		3		5	
J	1	2	3	4		
$\mathbf{T}$	1	2	3	4	5	