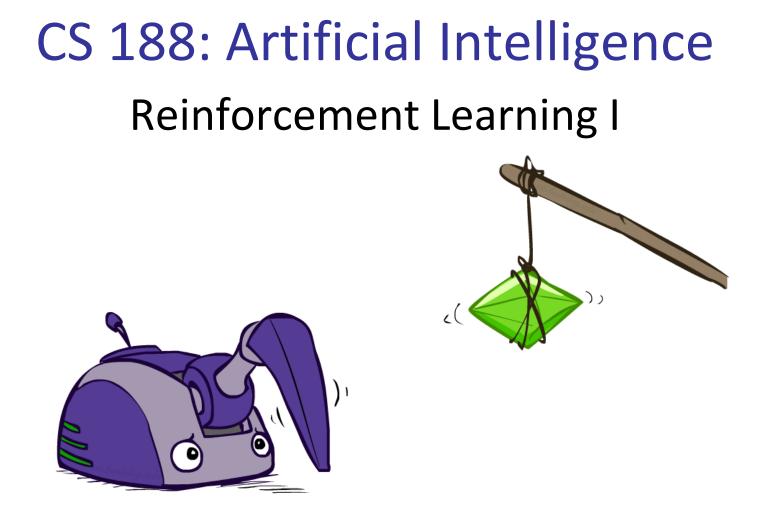
#### Announcements

- John Oliver "Last Week Tonight" on AI, ChatGPT, etc. (NSFW)
- Latin American and Caribbean states <u>announce support for a treaty</u> banning some types of autonomous weapons and regulating others
- United States, China, and many other countries announce support for a voluntary code of conduct on responsible use of autonomous weapons
- Midterm next Monday (March 6) 8-10pm (more details++ on ed)



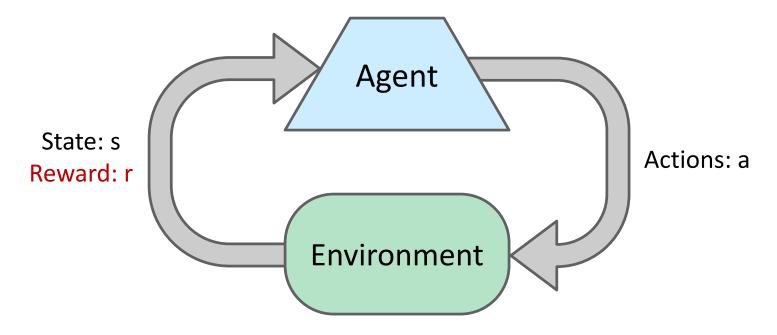
Instructors: Stuart Russell and Peyrin Kao

University of California, Berkeley

# **Reinforcement learning**

- What if the MDP is initially unknown? Lots of things change!
  - Exploration: you have to try unknown actions to get information
  - Exploitation: eventually, you have to use what you know
  - Regret: early on, you inevitably "make mistakes" and lose reward
  - Sampling: you may need to repeat many times to get good estimates
  - *Generalization*: what you learn in one state may apply to others too

## **Reinforcement Learning**



- Basic idea:
  - Learn how to maximize expected rewards based on observed samples of transitions
  - Not unlike the basic problem faced by all living things

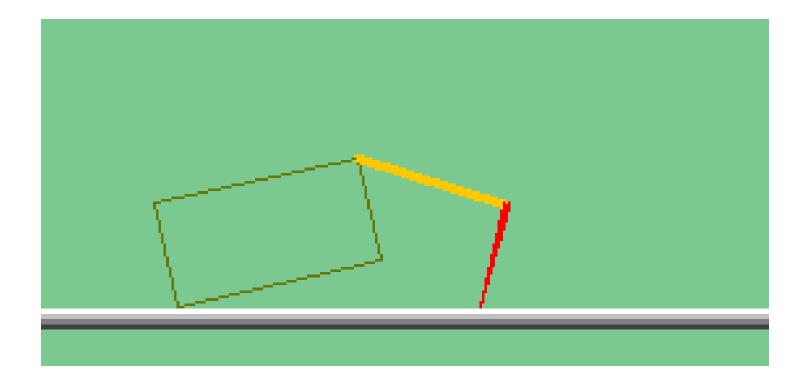
#### Example: Samuel's checker player (1956-67)



### Example: AlphaGo (2016)



#### The Crawler!

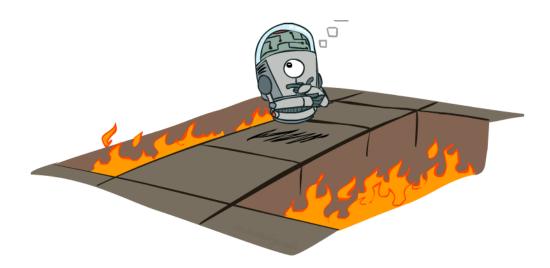


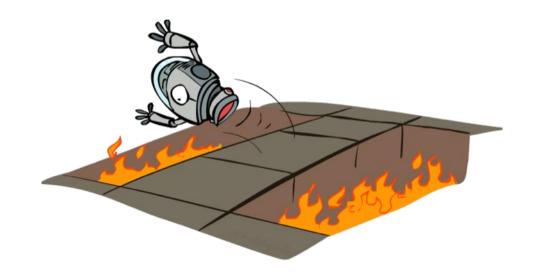
[Demo: Crawler Bot (L10D1)] [You, in Project 3]

## **Reinforcement Learning**

- Still assume a Markov decision process (MDP):
  - A set of states s ∈ S
  - A set of actions (per state) A(s)
  - A transition model T(s,a,s')
  - A reward function R(s,a,s')
- Still looking for a policy π(s)
- New twist: don't know T or R
  - I.e. we don't know which states are good or what the actions do
  - Must explore new states and actions -- to boldly go where no Pacman has gone before

## Offline (MDPs) vs. Online (RL)





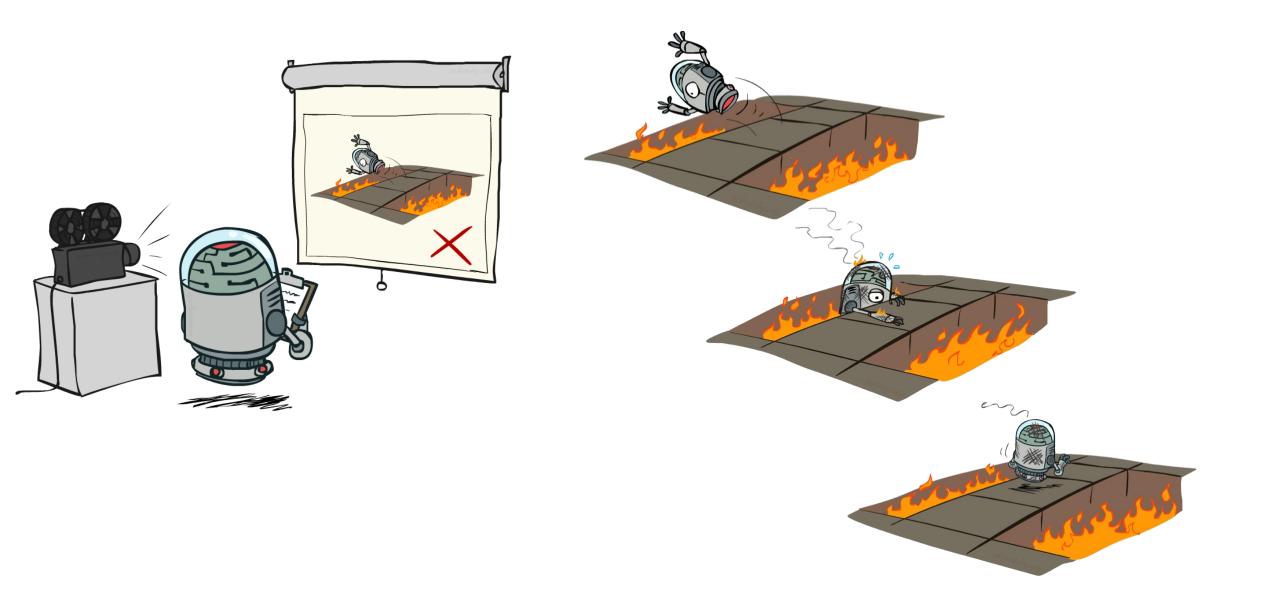
#### **Offline Solution**

**Online Learning** 

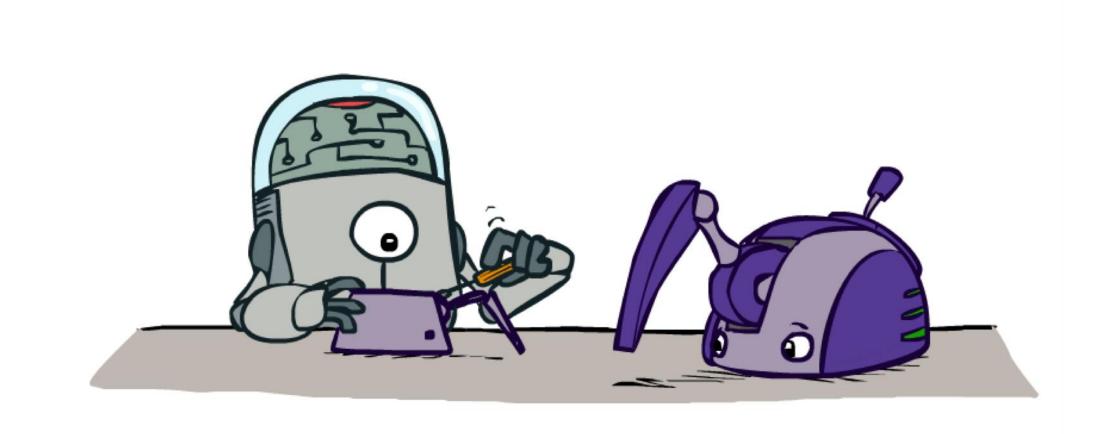
# Approaches to reinforcement learning

- 1. Model-based: Learn the model, solve it, execute the solution
- 2. Learn values from experiences, use to make decisions
  - a. Direct evaluation
  - b. Temporal difference learning
  - c. Q-learning
- 3. Learn policies directly (see AIMA4e Section 22.5)

#### Passive vs Active Reinforcement Learning



#### Model-Based RL



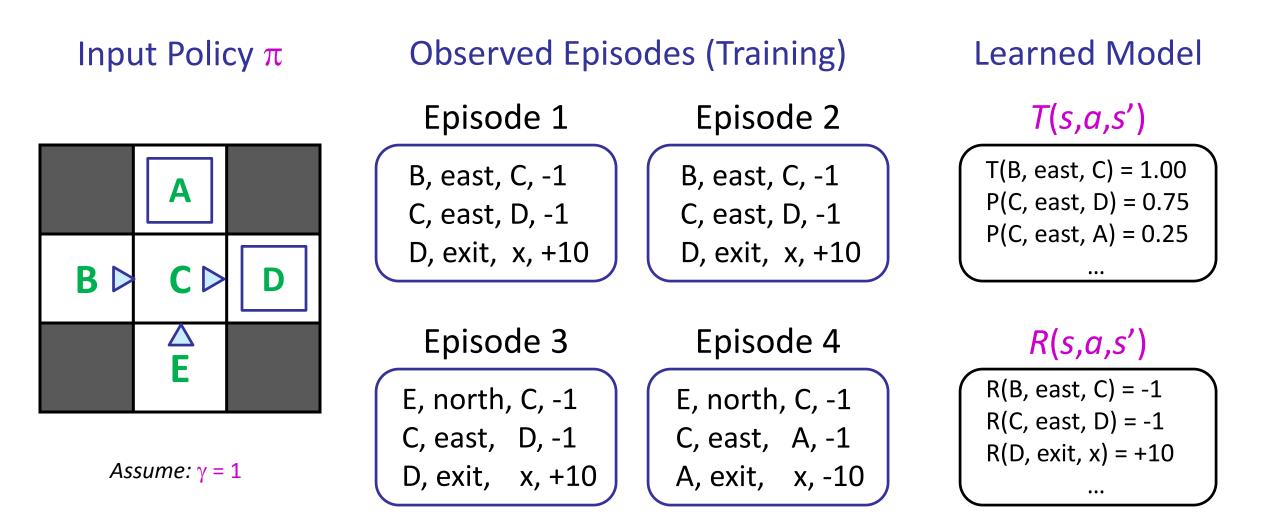
# **Model-Based Learning**

- Model-Based Idea:
  - Learn an approximate model based on experiences
  - Solve for values as if the learned model were correct
- Step 1: Learn empirical MDP model
  - Count outcomes s' for each s, a
  - Directly estimate each entry in T(s,a,s') from counts
  - Discover each R(s,a,s') when we experience the transition
- Step 2: Solve the learned MDP
  - Use, e.g., value or policy iteration, as before





#### Example: Model-Based Learning



#### Pros and cons

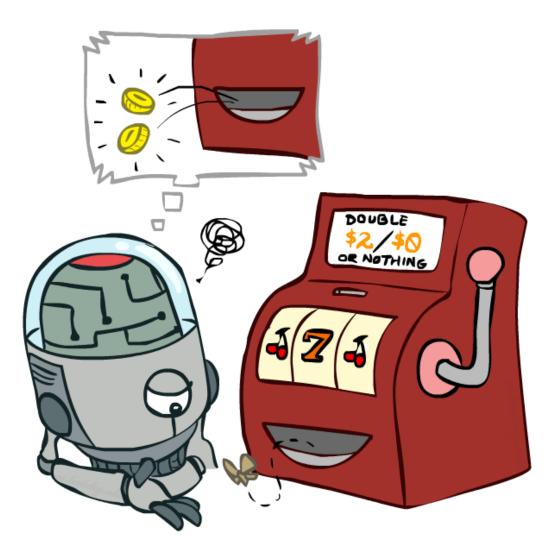
#### Pro:

Makes efficient use of experiences (low sample complexity)

#### Con:

- May not scale to large state spaces
  - Learns model one state-action pair at a time (but this is fixable)
  - Cannot solve MDP for very large |S| (also somewhat fixable)
- Much harder when the environment is partially observable

# Model-Free Learning

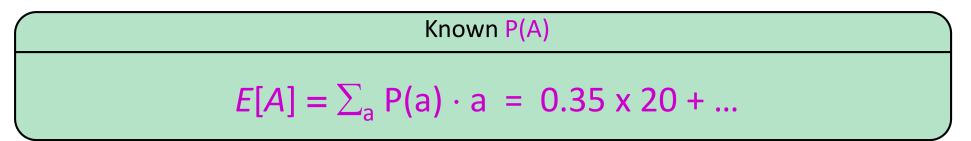


## Basic idea of model-free methods

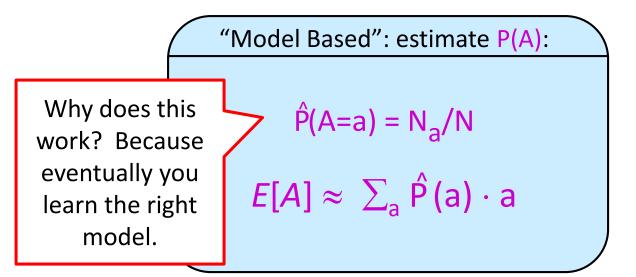
- To approximate expectations with respect to a distribution, you can either
  - Estimate the distribution from samples, compute an expectation
  - Or, bypass the distribution and estimate the expectation from samples directly

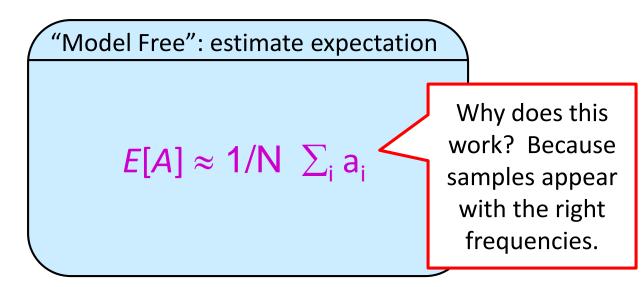
## Example: Expected Age

Goal: Compute expected age of cs188 students

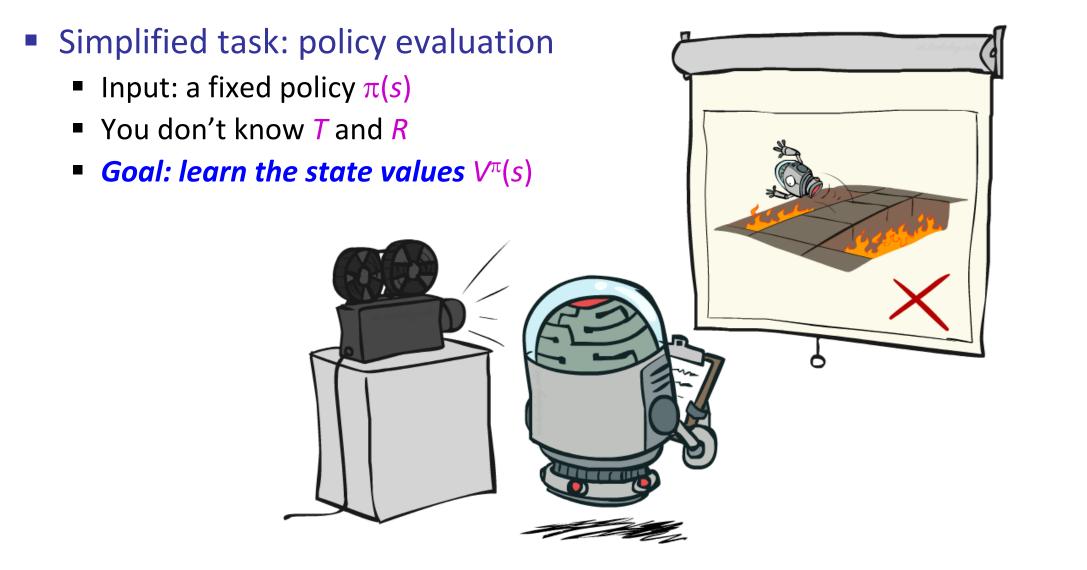


Without P(A), instead collect samples  $[a_1, a_2, ..., a_N]$ 





## **Passive Reinforcement Learning**



## **Direct evaluation**

- Goal: Estimate V<sup>π</sup>(s), i.e., expected total discounted reward from s onwards
- Idea:
  - Use *returns*, the <u>actual</u> sums of discounted rewards from s
  - Average over multiple trials and visits to s
- This is called *direct evaluation* (or direct utility estimation)



#### **Example: Direct Estimation**

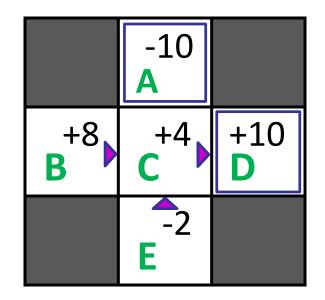


## Problems with Direct Estimation

- What's good about direct estimation?
  - It's easy to understand
  - It doesn't require any knowledge of T and R
  - It converges to the right answer in the limit
- What's bad about it?
  - Each state must be learned separately (fixable)
  - It ignores information about state connections
  - So, it takes a long time to learn

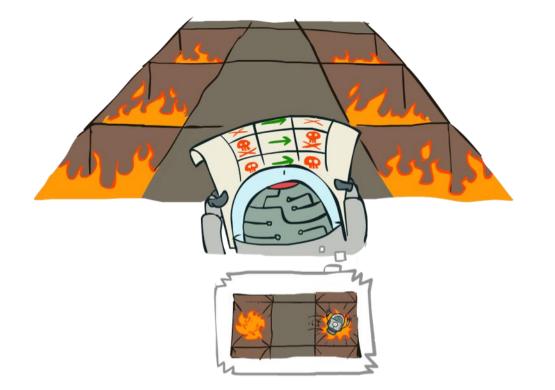
E.g., B=at home, study hard E=at library, study hard C=know material, go to exam

#### **Output Values**



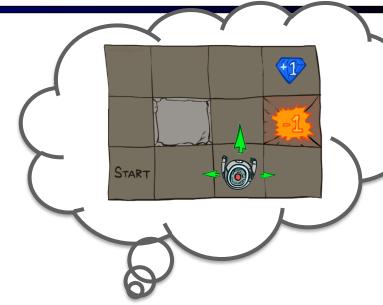
If B and E both go to C under this policy, how can their values be different?

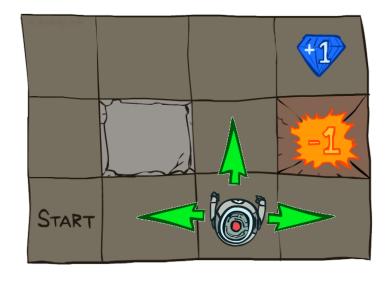
## Temporal difference (TD) learning



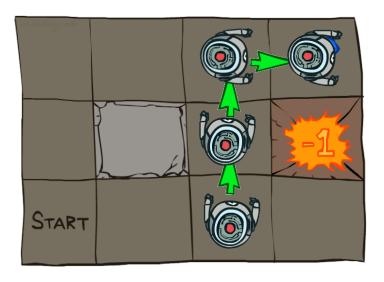


- Given a fixed policy, the value of a state is an expectation over next-state values:
  - $V^{\pi}(s) = \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V^{\pi}(s')]$
- Idea 1: Use actual samples to estimate the expectation:
  - sample<sub>1</sub> =  $R(s, \pi(s), s_1') + \gamma V^{\pi}(s_1')$  sample<sub>2</sub> =  $R(s, \pi(s), s_2') + \gamma V^{\pi}(s_2')$
  - ••••
  - sample<sub>N</sub> =  $R(s,\pi(s),s_N') + \gamma V^{\pi}(s_N')$
  - $V^{\pi}(s) \leftarrow 1/N \sum_{i} sample_{i}$





- Idea 2: Update value of s after each transition s,a,s',r :
- Update V<sup>π</sup> ([3,1]) based on R([3,1],up,[3,2]) and γV<sup>π</sup>([3,2])
- Update  $V^{\pi}([3,2])$  based on R([3,2],up,[3,3]) and  $\gamma V^{\pi}([3,3])$
- Update V<sup>π</sup> ([3,3]) based on R([3,3],right,[4,3]) and γV<sup>π</sup>([4,3])



Idea 3: Update values by maintaining a *running average* 

## Running averages

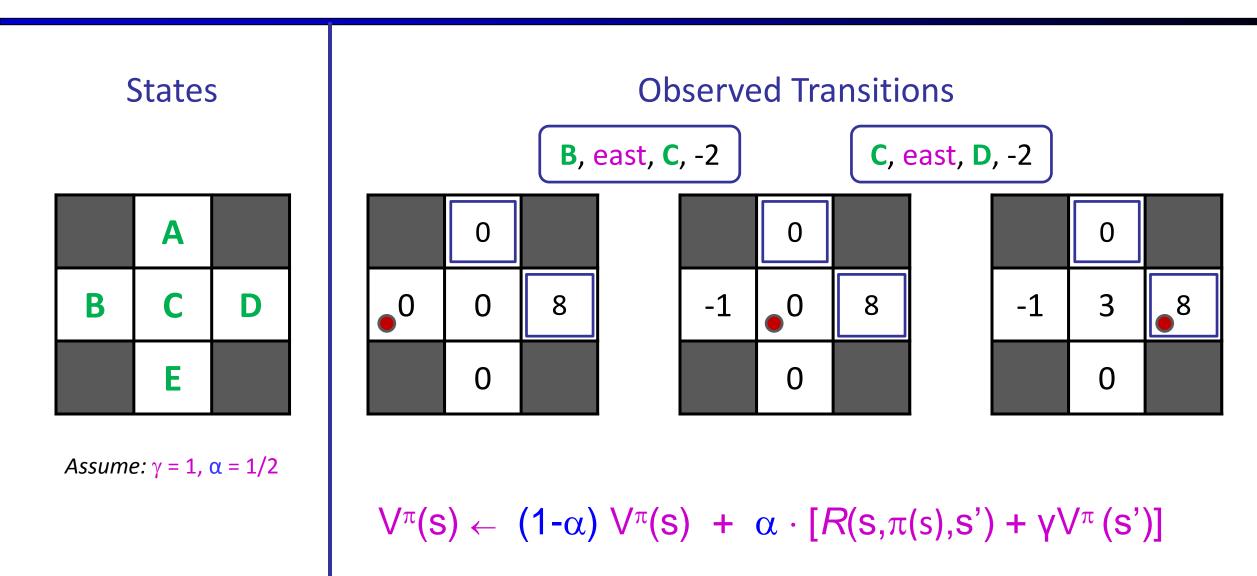
- How do you compute the average of 1, 4, 7?
- Method 1: add them up and divide by N
  - 1+4+7 = 12
  - average = 12/N = 12/3 = 4
- Method 2: keep a running average  $\mu_n$  and a running count **n** 
  - n=0 μ<sub>0</sub>=0
  - n=1  $\mu_1 = (0 \cdot \mu_0 + x_1)/1 = (0 \cdot 0 + 1)/1 = 1$
  - n=2  $\mu_2$  =  $(1 \cdot \mu_1 + x_2)/2$  =  $(1 \cdot 1 + 4)/2$  = 2.5
  - n=3  $\mu_3 = (2 \cdot \mu_2 + x_3)/3 = (2 \cdot 2.5 + 7)/3 = 4$
  - General formula:  $\mu_n = ((n-1) \cdot \mu_{n-1} + x_n)/n$ 
    - =  $[(n-1)/n] \mu_{n-1} + [1/n] x_n$  (weighted average of old mean, new sample)

#### Running averages contd.

- What if we use a weighted average with a fixed weight?
  - $\mu_n = (1-\alpha) \mu_{n-1} + \alpha x_n$
  - n=1  $\mu_1 = x_1$
  - n=2  $\mu_2 = (1-\alpha) \cdot \mu_1 + \alpha x_2 = (1-\alpha) \cdot x_1 + \alpha x_2$
  - n=3  $\mu_3 = (1-\alpha) \cdot \mu_2 + \alpha x_3 = (1-\alpha)^2 \cdot x_1 + \alpha (1-\alpha) x_2 + \alpha x_3$
  - $= n=4 \quad \mu_4 = (1-\alpha) \cdot \mu_3 + \alpha x_4 = (1-\alpha)^3 \cdot x_1 + \alpha (1-\alpha)^2 x_2 + \alpha (1-\alpha) x_3 + \alpha x_4$
- I.e., exponential forgetting of old values
- μ<sub>n</sub> is a convex combination of sample values (weights sum to 1)
- $E[\mu_n]$  is a convex combination of  $E[X_i]$  values, hence unbiased

- Idea 3: Update values by maintaining a *running average*
- sample =  $R(s,\pi(s),s') + \gamma V^{\pi}(s')$
- $V^{\pi}(s) \leftarrow (1-\alpha) \cdot V^{\pi}(s) + \alpha \cdot sample$
- $V^{\pi}(s) \leftarrow V^{\pi}(s) + \alpha \cdot [\text{sample} V^{\pi}(s)]$
- This is the temporal difference learning rule
- Isample V<sup>π</sup>(s)] is the "TD error"
- $\alpha$  is the *learning rate*
- I.e., observe a sample, move V<sup>π</sup>(s) a little bit to make it more consistent with its neighbor V<sup>π</sup>(s')

## **Example: Temporal Difference Learning**



#### Problems with TD Value Learning

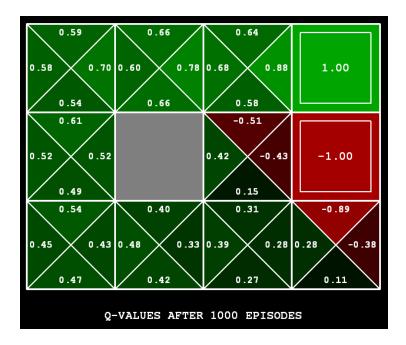
- TD value learning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- But we can't use the value function, or improve the policy, without a transition model to do one-step greedy expectimax!
- (Will see later how to use it with a known model in large state spaces)

# Q-learning as approximate Q-iteration

- Recall the definition of Q values:
  - Q<sup>\*</sup>(s,a) = expected return from doing a in s and then behaving optimally thereafter; and π<sup>\*</sup>(s) = max<sub>a</sub>Q<sup>\*</sup>(s,a)
- Bellman equation for Q values:
  - $Q^*(s,a) = \sum_{s'} T(s,a,s') [R(s,a,s') + \gamma \max_{a'} Q^*(s',a')]$
- Approximate Bellman update for Q values:
  - $Q(s,a) \leftarrow (1-\alpha) \cdot Q(s,a) + \alpha \cdot [R(s,a,s') + \gamma max_{a'}Q(s',a')]$
- We obtain a policy from learned Q(s,a), with no model!
  - (No free lunch: Q(s,a) table is |A| times bigger than V(s) table)

# Q-Learning

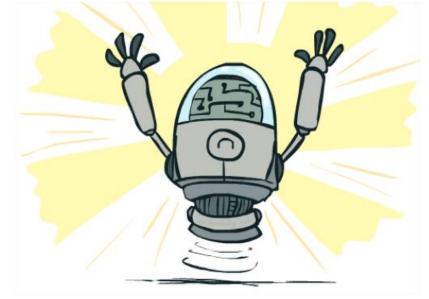
- Learn Q(s,a) values as you go
  - Receive a sample (s,a,s',r)
  - Consider your old estimate: Q(s,a)
  - Consider your new sample estimate:
    sample = R(s,a,s') + γ max<sub>a'</sub> Q(s',a')
  - Incorporate the new estimate into a running average:  $Q(s,a) \leftarrow (1-\alpha) Q(s,a) + \alpha \cdot [sample]$



[Demo: Q-learning – gridworld (L10D2)] [Demo: Q-learning – crawler (L10D3)]

# **Q-Learning Properties**

- Amazing result: Q-learning converges to optimal policy -- even if samples are generated from a suboptimal policy!
- This is called off-policy learning
- Caveats:
  - You have to explore enough (eventually try every state/action pair infinitely often)
  - You have to decrease the learning rate appropriately
    - Technical requirements:  $\sum_{t} \alpha(t) = \infty$ ,  $\sum_{t} \alpha^{2}(t) < \infty$
    - Satisfied by:  $\alpha(t) = 1/t$  or (better)  $\alpha(t) = K/(K+t)$



# Summary

- RL solves MDPs via direct experience of transitions and rewards
- There are several schemes:
  - Learn the MDP model and solve it
  - Learn V directly from sums of rewards, or by TD local adjustments
    - Still need a model to make decisions by lookahead
  - Learn Q by local Q-learning adjustments, use it directly to pick actions
  - (and about 100 other variations)
- Big missing pieces:
  - How to explore without too much regret?
  - How to scale this up to Tetris (10<sup>60</sup>), Go (10<sup>172</sup>), StarCraft (|A|=10<sup>26</sup>)?