### CS 188 Spring 2025 Artificial Intelligence

# Exam Prep 1

 $\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$ 

## Q1. Searching with Heuristics

Consider the A\* searching process on the connected undirected graph, with starting node S and the goal node G. Suppose the cost for each connection edge is **always positive**. We define  $h^*(X)$  as the shortest (optimal) distance to G from a node X.

Answer Questions (a). Question (b) is optional.

- (a) Suppose h is an admissible heuristic, and we conduct A\* tree search using heuristic h' and finally find a solution. Let C be the cost of the found path (directed by h', defined in part (a)) from S to G
  - (i) Choose one best answer for each condition below.
    - 1. If  $h'(X) = \frac{1}{2}h(X)$  for all Node X, then $\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$ 2. If  $h'(X) = \frac{h(X) + h^*(X)}{2}$  for all Node X, then $\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
    - 3. If  $h'(X) = h(X) + h^*(X)$  for all Node X, then  $\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
    - 4. If we define the set K(X) for a node X as all its neighbor nodes Y satisfying  $h^*(X) > h^*(Y)$ , and the following always holds

$$h'(X) \leq \begin{cases} \min_{Y \in K(X)} h'(Y) - h(Y) + h(X) & \text{if } K(X) \neq \emptyset \\ h(X) & \text{if } K(X) = \emptyset \end{cases}$$

then,

5. If *K* is the same as above, we have

$$h'(X) = \begin{cases} \min_{Y \in K(X)} h(Y) + cost(X, Y) & \text{if } K(X) \neq \emptyset \\ h(X) & \text{if } K(X) = \emptyset \end{cases}$$

where cost(X, Y) is the cost of the edge connecting X and Y, then,  $\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$ 

- 6. If  $h'(X) = \min_{Y \in K(X) + \{X\}} h(Y)$  (K is the same as above),  $\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
- (ii) In which of the conditions above, h' is still **admissible** and for sure to dominate h? Check all that apply. Remember we say  $h_1$  dominates  $h_2$  when  $h_1(X) \ge h_2(X)$  holds for all X.  $\Box$  1  $\Box$  2  $\Box$  3  $\Box$  4  $\Box$  5  $\Box$  6

#### (b) [Optional] Suppose h is an admissible heuristic, and we conduct A\* tree search using heuristic h' and finally find a solution.

If  $\epsilon > 0$ , and  $X_0$  is a node in the graph, and h' is a heuristic such that

$$h'(X) = \begin{cases} h(X) & \text{if } X = X_0\\ h(X) + \epsilon & \text{otherwise} \end{cases}$$

- Alice claims h' can be inadmissible, and hence  $C = h^*(S)$  does not always hold.
- Bob instead thinks the node expansion order directed by h' is the same as the heuristic h'', where

$$h''(X) = \begin{cases} h(X) - \epsilon & \text{if } X = X_0 \\ h(X) & \text{if otherwise} \end{cases}$$

Since h'' is admissible and will lead to  $C = h^*(S)$ , and so does h'. Hence,  $C = h^*(S)$  always holds.

The two conclusions (<u>underlined</u>) apparently contradict with each other, and **only exactly one of them are correct and the other is wrong**. Choose the **best** explanation from below - which student's conclusion is wrong, and why are they wrong?

 $\bigcirc$  Alice's conclusion is wrong, because the heuristic h' is always admissible.

 $\bigcirc$  Alice's conclusion is wrong, because an inadmissible heuristics does not necessarily always lead to the failure of the optimality when conducting A\* tree search.

○ Alice's conclusion is wrong, because of another reason that is not listed above.

 $\bigcirc$  Bob's conclusion is wrong, because the node visiting expansion ordering of h'' during searching might not be the same as h'.

 $\bigcirc$  Bob's conclusion is wrong, because the heuristic h'' might lead to an incomplete search, regardless of its optimally property.

O Bob's conclusion is wrong, because of another reason that is not listed above.

## Q2. Iterative Deepening Search

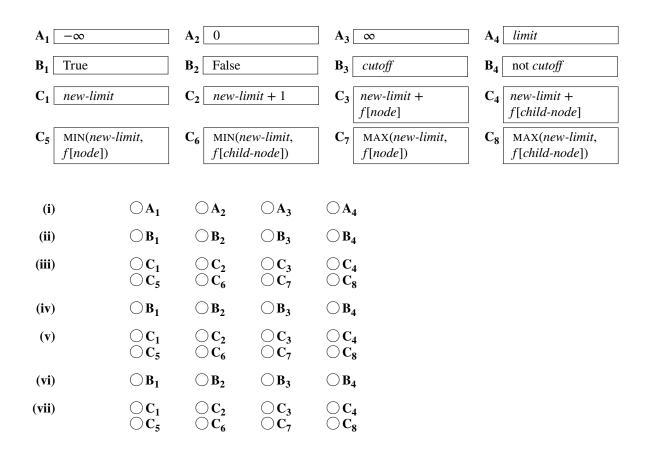
Pacman is performing search in a maze again! The search graph has a branching factor of b, a solution of depth d, a maximum depth of m, and edge costs that may not be integers. Although he knows breadth first search returns the solution with the smallest depth, it takes up too much space, so he decides to try using iterative deepening. As a reminder, in standard depth-first iterative deepening we start by performing a depth first search terminated at a maximum depth of one. If no solution is found, we start over and perform a depth first search to depth two and so on. This way we obtain the shallowest solution, but use only O(bd) space.

But Pacman decides to use a variant of iterative deepening called **iterative deepening**  $A^*$ , where instead of limiting the depth-first search by depth as in standard iterative deepening search, we can limit the depth-first search by the *f* value as defined in  $A^*$  search. As a reminder f[node] = g[node] + h[node] where g[node] is the cost of the path from the start state and h[node] is a heuristic value estimating the cost to the closest goal state.

In this question, all searches are tree searches and not graph searches.

(a) Complete the pseudocode outlining how to perform iterative deepening A\* by choosing the option from the next page that fills in each of these blanks. Iterative deepening A\* should return the solution with the lowest cost when given a consistent heuristic. (Note: Consistency is out of scope in this semester, but for the sake of this problem, remember that a consistent heuristic is one that makes sure you never have to revisit the same node multiple times in A\* search.) Note that cutoff is a boolean and new-limit is a number.

function Iterative-Deepening-Tree-Search(problem)	
$start-node \leftarrow MAKE-NODE(INITIAL-STATE[problem])$	
$limit \leftarrow f[start-node]$	
loop	
$fringe \leftarrow MAKE-STACK(start-node)$	
$new$ -limit $\leftarrow$ (i)	
$cutoff \leftarrow$ (ii)	
while <i>fringe</i> is not empty <b>do</b>	
$node \leftarrow \text{REMOVE-FRONT}(fringe)$	
if GOAL-TEST(problem, STATE[node]) then	
return node	
end if	
<b>for</b> <i>child-node</i> in EXPAND(STATE[ <i>node</i> ], <i>problem</i> ) <b>d</b>	0
if $f[child-node] \leq limit$ then	
$fringe \leftarrow \text{INSERT}(child-node, fringe)$	
$new$ -limit $\leftarrow$ (iii)	
$cutoff \leftarrow$ (iv)	
else	
<i>new-limit</i> $\leftarrow$ (v)	
$cutoff \leftarrow$ (vi)	
end if	
end for	
end while	
if not <i>cutoff</i> then	
return failure	
end if	
$limit \leftarrow$ (vii)	
end loop end function	



(b) Assuming there are no ties in *f* value between nodes, which of the following statements about the number of nodes that iterative deepening A\* expands is True? If the same node is expanded multiple times, count all of the times that it is expanded. If none of the options are correct, mark None of the above.

 $\bigcirc$  The number of times that iterative deepening A\* expands a node is greater than or equal to the number of times A\* will expand a node.

 $\bigcirc$  The number of times that iterative deepening A\* expands a node is less than or equal to the number of times A\* will expand a node.

• We don't know if the number of times iterative deepening A\* expands a node is more or less than the number of times A\* will expand a node.

 $\bigcirc$  None of the above