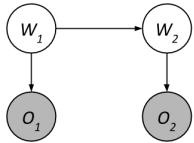


1 Particle Filtering

Let's use Particle Filtering to estimate the distribution of $P(W_2|O_1 = a, O_2 = b)$. Here's the HMM again. O_1 and O_2 are supposed to be shaded.



W_1	$P(W_1)$
0	0.3
1	0.7

W_t	W_{t+1}	$P(W_{t+1} W_t)$
0	0	0.4
0	1	0.6
1	0	0.8
1	1	0.2

W_t	O_t	$P(O_t W_t)$
0	a	0.9
0	b	0.1
1	a	0.5
1	b	0.5

We start with two particles representing our distribution for W_1 .

$P_1 : W_1 = 0$

$P_2 : W_1 = 1$

Use the following random numbers to run particle filtering:

[0.22, 0.05, 0.33, 0.20, 0.84, 0.54, 0.79, 0.66, 0.14, 0.96]

- (a) **Observe:** Compute the weight of the two particles after evidence $O_1 = a$.

- (b) **Resample:** Using the random numbers, resample P_1 and P_2 based on the weights.

- (c) **Predict:** Sample P_1 and P_2 from applying the time update.

- (d) **Update:** Compute the weight of the two particles after evidence $O_2 = b$.

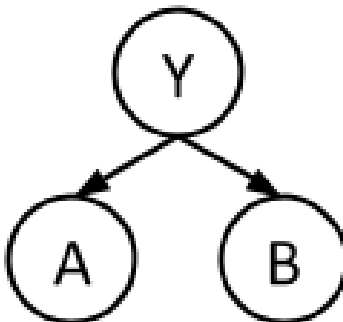
- (e) **Resample:** Using the random numbers, resample P_1 and P_2 based on the weights.

- (f) What is our estimated distribution for $P(W_2|O_1 = a, O_2 = b)$?

2 Naive Bayes

In this question, we will train a Naive Bayes classifier to predict class labels Y as a function of input features A and B . Y , A , and B are all binary variables, with domains 0 and 1. We are given 10 training points from which we will estimate our distribution.

A	1	1	1	1	0	1	0	1	1	1
B	1	0	0	1	1	1	1	0	1	1
Y	1	1	0	0	0	1	1	0	0	0



1. What are the maximum likelihood estimates for the tables $P(Y)$, $P(A|Y)$, and $P(B|Y)$?

Y	$P(Y)$
0	
1	

A	Y	$P(A Y)$
0	0	
1	0	
0	1	
1	1	

B	Y	$P(B Y)$
0	0	
1	0	
0	1	
1	1	

2. Consider a new data point ($A = 1, B = 1$). What label would this classifier assign to this sample?

3. Let's use Laplace Smoothing to smooth out our distribution. Compute the new distribution for $P(A|Y)$ given Laplace Smoothing with $k = 2$.

A	Y	$P(A Y)$
0	0	
1	0	
0	1	
1	1	