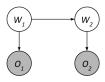
## Regular Discussion 8

## 1 Particle Filtering

Let's use Particle Filtering to estimate the distribution of  $P(W_2|O_1=a,O_2=b)$ . Here's the HMM again.  $O_1$  and  $O_2$  are supposed to be shaded.



$W_1$	$P(W_1)$
0	0.3
1	0.7

$W_t$	$W_{t+1}$	$P(W_{t+1} W_t)$
0	0	0.4
0	1	0.6
1	0	0.8
1	1	0.2

$W_t$	$O_t$	$P(O_t W_t)$
0	a	0.9
0	b	0.1
1	a	0.5
1	b	0.5

We start with two particles representing our distribution for  $W_1$ .

 $P_1:W_1=0$ 

 $P_2: W_1 = 1$ 

Use the following random numbers to run particle filtering:

[0.22, 0.05, 0.33, 0.20, 0.84, 0.54, 0.79, 0.66, 0.14, 0.96]

- (a) Observe: Compute the weight of the two particles after evidence  $O_1 = a$ .
- (b) Resample: Using the random numbers, resample  $P_1$  and  $P_2$  based on the weights.
- (c) **Predict**: Sample  $P_1$  and  $P_2$  from applying the time update.
- (d) Update: Compute the weight of the two particles after evidence  $O_2 = b$ .
- (e) Resample: Using the random numbers, resample  $P_1$  and  $P_2$  based on the weights.
- (f) What is our estimated distribution for  $P(W_2|O_1=a,O_2=b)$ ?

## 2 Decision Networks and VPI

A buyer is deciding whether to buy a certain used car. The car may be good quality (Q = +q) or bad quality (Q = -q). A test (T) costs \$50 and can help to figure out the quality of the car. There are only two outcomes for the test: T = pass or T = fail. The car costs \$1,500, and its market value is \$2,000 if it is good quality; if not, \$700 in repairs will be needed to make it good quality. The buyer's estimate is that the car has 70% chance of being good quality.



- 1. Calculate the expected net gain from buying the car, given no test.
- 2. Tests can be described by the probability that the car will pass or fail the test given that the car is in good or bad shape. We have the following information:

$$P(T = pass|Q = +q) = 0.9$$

$$P(T = \text{pass}|Q = \neg q) = 0.2$$

Calculate the probability that the car will pass (or fail) its test, and then the probability that it is in good (or bad) shape given each possible test outcome.

3. Calculate the optimal decisions given either a pass or a fail, and their expected utilities.

4. Calculate the value of (perfect) information of the test. Should the buyer pay for a test?