Warmup: Wordle as a CSP

- Guess the 5-letter word in 6 tries
- What are the:
  - Variables?
  - Domain?
  - Constraints?
CS 188: Artificial Intelligence

Constraint Satisfaction Problems

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[Slides adapted from Nicholas Tomlin, Dan Klein, Pieter Abbeel, and Anca Dragan]
Reminder: CSPs

- CSPs:
  - Variables
  - Domains
  - Constraints
    - Implicit (provide code to compute)
    - Explicit (provide a list of all legal tuples)
    - Unary / Binary / N-ary

- Goals:
  - Here: find any solution
  - But also: find all solutions, best solution, etc.
**Backtracking Search**

```
function Backtracking-Search(csp) returns solution/failure
    return Recursive-Backtracking({}, csp)

function Recursive-Backtracking(assignment, csp) returns soln/failure
    if assignment is complete then return assignment
    var ← Select-Unassigned-Variable(VARIABLES[csp], assignment, csp)
    for each value in Order-Domain-Values(var, assignment, csp) do
        if value is consistent with assignment given CONSTRAINTS[csp] then
            add \{var = value\} to assignment
            result ← Recursive-Backtracking(assignment, csp)
            if result ≠ failure then return result
            remove \{var = value\} from assignment
        return failure
```
Improving Backtracking

- General-purpose ideas bring huge gains in speed
  - ...but it’s all still NP-hard

- Filtering: can we detect inevitable failure early?

- Ordering:
  - Which variable should be assigned next?
  - In what order should its values be tried?

- Structure: can we exploit the structure of the problem/constraint graph?
Reminder: Forward Checking

- Filtering: Keep track of domains for unassigned variables and cross off bad options
- Forward checking: Cross off values that violate a constraint when added to the existing assignment
Reminder: Arc Consistency

- An arc $X \rightarrow Y$ is **consistent** iff for *every* $x$ in the tail there is *some* $y$ in the head which could be assigned without violating a constraint.

**Forward checking?**

Enforcing consistency of arcs pointing to each new assignment.
Reminder: Arc Consistency

- A simple form of propagation makes sure all arcs are consistent:

- Important: If X loses a value, neighbors of X need to be rechecked!
- Arc consistency detects failure earlier than forward checking
- Can be run as a preprocessor or after each assignment
- What’s the downside of enforcing arc consistency?

Remember: Delete from the tail!
Ordering
Ordering: Minimum Remaining Values

- Variable Ordering: Minimum remaining values (MRV):
  - Choose the variable with the fewest legal values left in its domain

- Why min rather than max?
- Also called “most constrained variable”
- “Fail-fast” ordering
Ordering: Least Constraining Value

- Value Ordering: Least Constraining Value
  - Given a choice of variable, choose the least constraining value
  - I.e., the one that rules out the fewest values in the remaining variables
  - Note that it may take some computation to determine this! (E.g., rerunning filtering)

- Why least rather than most?

- Combining these ordering ideas makes 1000 queens feasible
Problem Structure

- Extreme case: independent subproblems
  - Example: Tasmania and mainland do not interact

- Independent subproblems are identifiable as connected components of constraint graph

- Suppose a graph of $n$ variables can be broken into subproblems of only $c$ variables:
  - Worst-case solution cost is $O((n/c)(d^c))$, linear in $n$
  - E.g., $n = 80$, $d = 2$, $c = 20$
  - $2^{80} = 4$ billion years at 10 million nodes/sec
  - $(4)(2^{20}) = 0.4$ seconds at 10 million nodes/sec
Tree-Structured CSPs

- Theorem: if the constraint graph has no loops, the CSP can be solved in $O(n d^2)$ time
  - Compare to general CSPs, where worst-case time is $O(d^n)$

- This property also applies to probabilistic reasoning (later): an example of the relation between syntactic restrictions and the complexity of reasoning
Tree-Structured CSPs

- Algorithm for tree-structured CSPs:
  - Order: Choose a root variable, order variables so that parents precede children
  - Remove backward: For $i = n : 2$, apply \( \text{RemoveInconsistent}(\text{Parent}(X_i), X_i) \)
  - Assign forward: For $i = 1 : n$, assign $X_i$ consistently with $\text{Parent}(X_i)$

- Runtime: $O(n \, d^2)$ (why?)
Tree-Structured CSPs

- Claim 1: After backward pass, all root-to-leaf arcs are consistent
  - Proof: Each $X \rightarrow Y$ was made consistent at one point and $Y$’s domain could not have been reduced thereafter (because $Y$’s children were processed before $Y$)

- Claim 2: If root-to-leaf arcs are consistent, forward assignment will not backtrack
  - Proof: Induction on position

- Note: we’ll see this basic idea again with Bayes’ nets
Improving Structure
Nearly Tree-Structured CSPs

- Conditioning: instantiate a variable, prune its neighbors' domains
- Cutset conditioning: instantiate (in all ways) a set of variables such that the remaining constraint graph is a tree
- Cutset size $c$ gives runtime $O(d^c(n-c)d^2)$, very fast for small $c$
Cutset Conditioning

- Choose a cutset
- Instantiate the cutset (all possible ways)
- Compute residual CSP for each assignment
- Solve the residual CSPs (tree structured)
Cutset Quiz

- Find the smallest cutset for the graph below.
Bonus: Tree Decomposition

- Idea: create a tree-structured graph of mega-variables
- Each mega-variable encodes part of the original CSP
- Subproblems overlap to ensure consistent solutions

\[ \{(WA=r,SA=g,NT=b), (WA=b,SA=r,NT=g), \ldots\} \]
\[ \{(NT=r,SA=g,Q=b), (NT=b,SA=g,Q=r), \ldots\} \]
\[ \{(WA=g,SA=g,NT=g), (NT=g,SA=g,Q=g), \ldots\} \]
Iterative Improvement
Local Search

- Tree search keeps unexplored alternatives on the fringe (ensures completeness)

- Local search: improve a single option until you can’t make it better (no fringe!)

- New successor function: local changes

- Generally much faster and more memory efficient (but incomplete and suboptimal)
Iterative Algorithms for CSPs

- Local search methods typically work with “complete” states, i.e., all variables assigned.
- To apply to CSPs:
  - Take an assignment with unsatisfied constraints
  - Operators *reassign* variable values
  - No fringe! Live on the edge.
- Algorithm: While not solved,
  - Variable selection: randomly select any conflicted variable
  - Value selection: min-conflicts heuristic:
    - Choose a value that violates the fewest constraints
    - I.e., hill climb with $h(x) =$ total number of violated constraints
Example: 4-Queens

- States: 4 queens in 4 columns ($4^4 = 256$ states)
- Operators: move queen in column
- Goal test: no attacks
- Evaluation: $c(n) = \text{number of attacks}$
Performance of Min-Conflicts

- Given random initial state, can solve n-queens in almost constant time for arbitrary n with high probability (e.g., n = 10,000,000)!

- The same appears to be true for any randomly-generated CSP except in a narrow range of the ratio

\[
R = \frac{\text{number of constraints}}{\text{number of variables}}
\]
Hill Climbing

- Simple, general idea:
  - Start wherever
  - Repeat: move to the best neighboring state
  - If no neighbors better than current, quit

- What’s bad about this approach?
- What’s good about it?
Hill Climbing Diagram

- Objective function
- Global maximum
- Shoulder
- Local maximum
- "Flat" local maximum
- Current state
- State space
Hill Climbing Quiz

Starting from X, where do you end up?

Starting from Y, where do you end up?

Starting from Z, where do you end up?
Simulated Annealing

- **Idea:** Escape local maxima by allowing downhill moves
  - But make them rarer as time goes on

```python
def SIMULATED-ANNEALING(problem, schedule) returns a solution state
    inputs: problem, a problem
             schedule, a mapping from time to “temperature”
    local variables: current, a node
                     next, a node
                     T, a “temperature” controlling prob. of downward steps
    current ← MAKE-NODE(INITIAL-STATE[problem])
    for t ← 1 to ∞ do
        T ← schedule[t]
        if T = 0 then return current
        next ← a randomly selected successor of current
        ΔE ← VALUE[next] – VALUE[current]
        if ΔE > 0 then current ← next
        else current ← next only with probability e^{Δ E/T}
```
Simulated Annealing

- **Theoretical guarantee:**
  - Stationary distribution: \( p(x) \propto e^{\frac{E(x)}{kT}} \)
  - If T decreased slowly enough, will converge to optimal state!

- **Is this an interesting guarantee?**

- **Sounds like magic, but reality is reality:**
  - The more downhill steps you need to escape a local optimum, the less likely you are to ever make them all in a row
  - People think hard about *ridge operators* which let you jump around the space in better ways
Gradient Descent as Simulated Annealing

- Q: Can we do better than randomly guessing?
- A: Yes, if the function is continuous and differentiable.

```plaintext
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        schedule, a mapping from time to “temperature”
local variables: current, a node
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    if ΔE > 0 then current ← next
        else current ← next only with probability $e^{\Delta E / T}$
```
Genetic Algorithms

- Genetic algorithms use a natural selection metaphor
  - Keep best $N$ hypotheses at each step (selection) based on a fitness function
  - Also have pairwise crossover operators, with optional mutation to give variety

- Possibly the most misunderstood, misapplied (and even maligned) technique around
Example: N-Queens

- Why does crossover make sense here?
- When wouldn’t it make sense?
- What would mutation be?
- What would a good fitness function be?
Bonus: Weighted CSPs

- In the real world, many constraints are soft:
  - Scheduling:
    - With enough people attending a meeting, no times will work
    - Solution: some conflicts are more important than others, make sacrifices where necessary
  - Travel planning:
    - Budget: would like to keep things cheap, but willing to spend more if it’s worth it
    - Distance: want to avoid long walks, but can make exceptions for really interesting places
  - Running example: crosswords!
  
- Different set of algorithms often used for WCSPs

“Automated crossword solving.” Eric Wallace, Nicholas Tomlin, Albert Xu, Kevin Yang, Eshaan Pathak, Matthew Ginsberg, Dan Klein
Example Crossword

Example Crossword

Across
1  Regarding
6  Take back, in a way
10  Start of an aside
14  Omega competitor
15  Something hitting a nerve?
16  Papyrus, e.g.
17  "Take me with you!"
18  Begin flirting with someone, so to speak
20  Assign
21  Hoth, in "Star Wars"
22  ___ rule
23  They don’t hold water
24  Feudal figure
26  Panegyric, e.g.
27  Sci-fi enemy collective, perhaps
31  Ones born beginning in the early 2010s
37  They might cut to the chase
38  Electrically balanced, in chemistry
42  Leaders at the Kaaba

Down
1  Home to 41-Down
2  Convince
3  "I wanna know all the details"
4  Start of a modern inquiry
5  Drink similar to sarsaparilla
6  Co-star of 1984’s "Ghostbusters"
7  Right on
8  Aces with aces?
9  Like some households
10  Designer with an eponymous hotel in the Burj Khalifa
11  Currency units in West Africa
12  Grievous
13  "Golden Boy" playwright
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30 It can be found right on a clock
32 "100 Years ... 100 Stars” and others, in brief
33 The world’s largest desert capital, after Cairo, Egypt

Crosswords as a Weighted CSP

- Variables: entries in the grid
- Domains: all possible words (??)
- Constraints:
  - Hard constraints: intersecting words match
  - Scoring function: match the clues
- Questions:
  - Where does the scoring function come from?
  - What’s the search algorithm?
Scoring Function

14. Omega competitor

○
14. Omega competitor

Scoring Function

Domain

\[
\begin{array}{cccccc}
A & B & A & S & E \\
A & B & A & T & E \\
A & B & B & E & Y \\
A & B & I & D & E \\
A & B & O & U & T \\
A & B & Y & S & S \\
Z & O & O & M & S \\
\end{array}
\]
14. Omega competitor
14. Omega competitor

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Scoring Function
14. Omega competitor

Scoring Function

- Domain:
  - ROLEX
  - SEIKO
  - ALPHA
  - APPLE

- Apple competitor:
  - SKUNK
14. Omega competitor

Scoring Function

Domain

Rolex

Seiko

Alpha

Apple

Enemy

Skunk
Search Algorithm for Crosswords

- Our approach:
  - Use QA model to get probability distribution over answers
  - Belief propagation (we’ll talk more about this later in the class)
  - Initialize solution with greedy search
  - Iterative improvement on individual letters
### Across

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1. Beloved, in Arabic
2. [Make it quick!]
3. Masthead listings, for short
4. Italian herbal liqueur
5. “Please, please, please?”
6. People calling the shots at the zoo?
7. Not radical
8. Drink with a dome-shaped lid
9. Where to find the Egyptian Temple of Dendur, with “the”
10. Crush, as a test
11. Cry from a survivor
12. Clara in the National Women’s Hall of Fame
13. Stuffed oneself with, facetiously
14. Newswoman Roberts
15. Recipe amt.
16. Doesn’t stay natural?
17. Fell off, as laughter
18. Place

### Down

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1. Soccer star on a 1999 Wheaties box
2. Bloblike
3. Ill-advised opinions
4. Fury
5. Feeling on a lo-o-ong car trip
6. Lab workers
7. Performer with the hit 2006 album "HIp Hop Is Dead"
8. Voting no
9. ___ Beach, Calif.
10. Satan, with “the”
11. Crack, as a secret message
12. Shorthand writers, for short
13. Dated
14. Cpl. or sgt.
15. Expand
16. Purge (of)
17. Atlanta-based health org.
18. Long fur scarfs
Iterative Improvement

Iterative Improvement

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10  Start of an aside
14  Omega competitor
15  Something hitting a nerve?
16  Papyrus, e.g.
17  "Take me with you!"
18  Begin flirting with someone, so to speak
20  Assign
21  Hoth, in "Star Wars"
22  ___ rule
23  They don't hold water
24  Feudal figure
26  Panegyric, e.g.
27  Sci-fi enemy collective, perhaps
28  Ones born beginning in the early 2010s
29  They might cut to the chase
30  Electrically balanced, in chemistry
35  Leaders at the Kaaba
36  ___ noticed ...
41  Home to 41-Down
46  Convince
47  "I wanna know all the details"
48  Start of a modern inquiry
49  Drink similar to sarsaparilla
50  Co-star of 1984’s "Ghostbusters"
51  Right on
52  Aces with aces?
53  Like some households
54  Designer with an eponymous hotel in the Burj Khalifa
55  Currency units in West Africa
56  Grievous
57  "Golden Boy" playwright
58  Actress Shawkat of "Arrested Development"
59  Assignment for an anchor
60  ___ noticed ...
61  Great Hindu sage
62  Late-Triassic flier

Down
1  Home to 41-Down
2  Convince
3  "I wanna know all the details"
4  Start of a modern inquiry
5  Drink similar to sarsaparilla
6  Co-star of 1984’s "Ghostbusters"
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Bonus: Fortuitous Search Errors

- Scoring function can be *incorrectly calibrated*

- **Example: decoding from language models**
  - Language models assign probabilities to strings of words
  - Decoding uses greedy or beam search
  - But what if you searched over all possible strings (exponentially many) and chose the highest scoring one?
  - Answer: you often end up generating the empty string, or “The the the the the…”
Summary: CSPs

- CSPs are a special kind of search problem:
  - States are partial assignments
  - Goal test defined by constraints
- Basic solution: backtracking search
- Speed-ups:
  - Ordering
  - Filtering
  - Structure – trees are easy!
- Local search often effective in practice