

Problem 4. (3 / 6 points): It was a dark and mysterious recursion...

Consider the recursive procedure `gather` that takes a sentence of at least two single-character words (i.e., letters such as 'a', 'b', etc.):

```
;; sent-of-ltrs is a sentence of at least 2 words that are single
;; letters
(define (gather sent-of-ltrs)
  (cond ((empty? sent-of-ltrs) '())
        ((empty? (bf sent-of-ltrs))
         (se (first sent-of-ltrs)))
        ((equal? (first (first sent-of-ltrs))
                  (first (bf sent-of-ltrs)))
         (gather (se (word (first sent-of-ltrs)
                           (first (bf sent-of-ltrs)))
                     (bf (bf sent-of-ltrs)))))
        (else
         (se (first sent-of-ltrs)
             (gather (bf sent-of-ltrs))))))
```

Part A (3 points). What will `(gather ' (a b b b c d d))` return?

Part B (6 points). Write `gather-hof`, which behaves the same as `gather` but uses no explicit recursion.

Problem 5. (9 points): Does money grow on tree recursions?

Consider a set of three coins: a penny, worth 1 cent; a nickel, worth 5 cents; and a dime, worth 10 cents. Write a procedure named `possible-amounts` which takes a number `n`, and returns a sentence of all the possible amounts that any `n` coins of these three types can make. For instance

<code>(possible-amounts 1)</code>	➔	<code>(1 5 10)</code>
<code>(possible-amounts 2)</code>	➔	<code>(2 6 11 10 15 20)</code> <i>(This includes two pennies, a penny and a nickel, a penny and a dime, two nickels, a nickel and a dime, and two dimes)</i>
<code>(possible-amounts 3)</code>	➔	<code>(3 7 12 11 16 21 15 20 25 30)</code>

Fill in the blanks to make the definition of `possible-amounts` work correctly:

```

(define *coin-amounts* _____)

(define (possible-amounts n)
  (pa-helper *coin-amounts* n))

(define (pa-helper coins n)

  (cond ((<= n 1) _____)                ;; base case 1

        ((empty? coins) _____)          ;; base case 2

        (else (se (add-coin-to-every         ;; recur case 1
                    (first coins)
                    (pa-helper coins (- n 1)))
                    (pa-helper               ;; recur case 2
                    _____
                    _____ ) ) ) ) )

;; add coin to each element of sent
(define (add-coin-to-every coin sent)
  (every (lambda (num)
            (+ coin num))
        sent))

```