

Announcements

- Homework 3 due Tuesday 10/1 @ 11:59pm
- Optional Hog Contest entries due Thursday 10/3 @ 11:59pm
- Composition scores will be assigned this week (perhaps by Monday).
 - 3/3 is very rare on the first project.
 - You can gain back any points you lose on the first project by revising it (November).

61A Lecture 10

Wednesday, September 25

Data

Data Types

Every value has a type

(demo)

Properties of native data types:

1. There are primitive expressions that evaluate to values of these types.
2. There are built-in functions, operators, and methods to manipulate those values.

Numeric types in Python:

```
>>> type(2)
<class 'int'>
```

Represents integers exactly

```
>>> type(1.5)
<class 'float'>
```

Represents real numbers approximately

```
>>> type(1+1j)
<class 'complex'>
```

Objects

- Objects represent information.
- They consist of data and behavior, bundled together to create **abstractions**.
- Objects can represent things, but also properties, interactions, & processes.
- A type of object is called a class; classes are first-class values in Python.
- Object-oriented programming:
 - A metaphor for organizing large programs
 - Special syntax that can improve the composition of programs
- In Python, every value is an object.
 - All objects have attributes.
 - A lot of data manipulation happens through *object methods*.
 - Functions do one thing; objects do many related things.

(Demo)

Data Abstraction

Data Abstraction

- Compound objects combine objects together
- A date: a year, a month, and a day
- A geographic position: latitude and longitude
- An *abstract data type* lets us manipulate compound objects as units
- Isolate two parts of any program that uses data:
 - How data are represented (as parts)
 - How data are manipulated (as units)
- Data abstraction: A methodology by which functions enforce an abstraction barrier between *representation* and *use*

All Programmers

Great Programmer

Rational Numbers

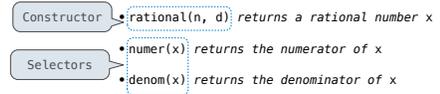
$$\frac{\text{numerator}}{\text{denominator}}$$

Exact representation of fractions

A pair of integers

As soon as division occurs, the exact representation may be lost!

Assume we can compose and decompose rational numbers:



Rational Number Arithmetic

$$\frac{3}{2} * \frac{3}{5} = \frac{9}{10}$$

$$\frac{3}{2} + \frac{3}{5} = \frac{21}{10}$$

Example

$$\frac{nx}{dx} * \frac{ny}{dy} = \frac{nx*ny}{dx*dy}$$

$$\frac{nx}{dx} + \frac{ny}{dy} = \frac{nx*dy + ny*dx}{dx*dy}$$

General Form

Rational Number Arithmetic Implementation

```
def mul_rational(x, y):
    return rational(numer(x) * numer(y),
                   denom(x) * denom(y))
```



$$\frac{nx}{dx} * \frac{ny}{dy} = \frac{nx*ny}{dx*dy}$$

```
def add_rational(x, y):
    nx, dx = numer(x), denom(x)
    ny, dy = numer(y), denom(y)
    return rational(nx * dy + ny * dx, dx * dy)
```

$$\frac{nx}{dx} + \frac{ny}{dy} = \frac{nx*dy + ny*dx}{dx*dy}$$

```
def equal_rational(x, y):
    return numer(x) * denom(y) == numer(y) * denom(x)
```

- `rational(n, d)` returns a rational number `x`
- `numer(x)` returns the numerator of `x`
- `denom(x)` returns the denominator of `x`

These functions implement an abstract data type for rational numbers

Pairs

Pairs as Tuples

```
>>> pair = (1, 2)
>>> pair
(1, 2)
```

A tuple literal:
Comma-separated expression

```
>>> x, y = pair
>>> x
1
>>> y
2
```

"Unpacking" a tuple

```
>>> pair[0]
1
>>> pair[1]
2
>>> from operator import getitem
>>> getitem(pair, 0)
1
>>> getitem(pair, 1)
2
```

Element selection

More tuples next lecture

Representing Rational Numbers

```
def rational(n, d):
    """Construct a rational number x that represents n/d."""
    return (n, d)

from operator import getitem

def numer(x):
    """Return the numerator of rational number x."""
    return getitem(x, 0)

def denom(x):
    """Return the denominator of rational number x."""
    return getitem(x, 1)
```

Construct a tuple

Select from a tuple

Reducing to Lowest Terms

Example:

$$\frac{3}{2} * \frac{5}{3} = \frac{5}{2}$$

$$\frac{2}{5} + \frac{1}{10} = \frac{1}{2}$$

$$\frac{15}{6} * \frac{1/3}{1/3} = \frac{5}{2}$$

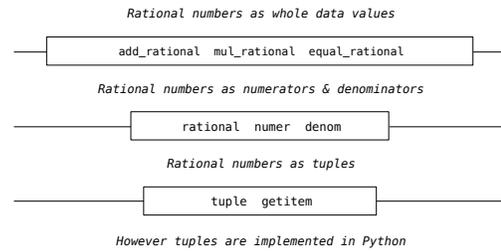
$$\frac{25}{50} * \frac{1/25}{1/25} = \frac{1}{2}$$

```
from fractions import gcd
def rational(n, d):
    """Construct a rational number x that represents n/d."""
    g = gcd(n, d)
    return (n//g, d//g)
```

Greatest common divisor

Abstraction Barriers

Abstraction Barriers



Violating Abstraction Barriers

```
add_rational((1, 2), (1, 4))

def divide_rational(x, y):
    return (x[0] * y[1], x[1] * y[0])
```

Does not use constructors

Twice!

No selectors!

And no constructor!

Data Representations

What is Data?

- We need to guarantee that constructor and selector functions work together to specify the right behavior.
- Behavior condition:** If we construct rational number x from numerator n and denominator d , then $\text{numer}(x)/\text{denom}(x)$ must equal n/d .
- An abstract data type is some collection of selectors and constructors, together with some behavior condition(s).
- If behavior conditions are met, then the representation is valid.

You can recognize abstract data types by their behavior, not by their class

Behavior Conditions of a Pair

To implement our rational number abstract data type, we used a two-element tuple. But is that the only way to make pairs of values? *No!*

Constructors, selectors, and behavior conditions:

- If a pair p was constructed from elements x and y , then
- `getitem_pair(p, 0)` returns x , and
 - `getitem_pair(p, 1)` returns y .

Together, selectors are the inverse of the constructor
Generally true of *container types*.

Not true for rational numbers because of GCD

(Demo)

Functional Pair Implementation

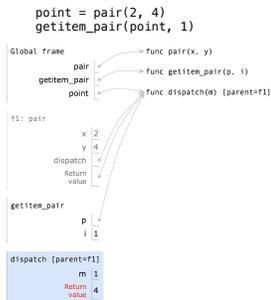
```
def pair(x, y):
    """Return a functional pair."""
    def dispatch(m):
        if m == 0:
            return x
        elif m == 1:
            return y
        return dispatch
    return dispatch
```

This function represents a pair

Constructor is a higher-order function

```
def getitem_pair(p, i):
    """Return the element at index i of pair p."""
    return p(i)
```

Selector defers to the object itself



Example: <http://goo.gl/9Hv98F>

Using a Functionally Implemented Pair

```
>>> p = pair(1, 2)
>>> getitem_pair(p, 0)
1
>>> getitem_pair(p, 1)
2
```

As long as we do not violate the abstraction barrier, we don't need to know that pairs are just functions

- If a pair p was constructed from elements x and y , then
- `getitem_pair(p, 0)` returns x , and
 - `getitem_pair(p, 1)` returns y .

This pair representation is valid!