61A Lecture 8

Wednesday, September 17

Announcements

- Project 1 is due Thursday 9/18 @ 11:59pm; Early bonus point for submitting on Wednesday!
 - Project Party in Stern Main Lounge (Stern Hall in Unit 4) 8pm-10pm on Wednesday 9/17
- Midterm 1 is on Monday 9/22 from 7pm to 9pm
 - "2 review sessions on Saturday 9/20 3pm-4:30pm and 4:30pm-6pm in 1 Pimentel
 - •HKN review session moved to Sunday 9/21, time/location TBD
 - •Includes topics up to and including this lecture
 - *Closed book/note exam, except for one page of hand-written notes and a study guide
 - •Cannot attend? Fill out the conflict form by Wednesday 9/17 @ 5pm!
- Optional Hog strategy contest ends Wednesday 10/1 @ 11:59pm

Hog Contest Rules

- Up to two people submit one entry;
 Max of one entry per person
- Your score is the number of entries against which you win more than 50% of the time
- All strategies must be deterministic, pure functions of the current player scores
- All winning entries will receive 2 points of extra credit
- The real prize: honor and glory

Fall 2011 Winners

Kaylee Mann Yan Duan & Ziming Li Brian Prike & Zhenghao Qian Parker Schuh & Robert Chatham

Fall 2012 Winners

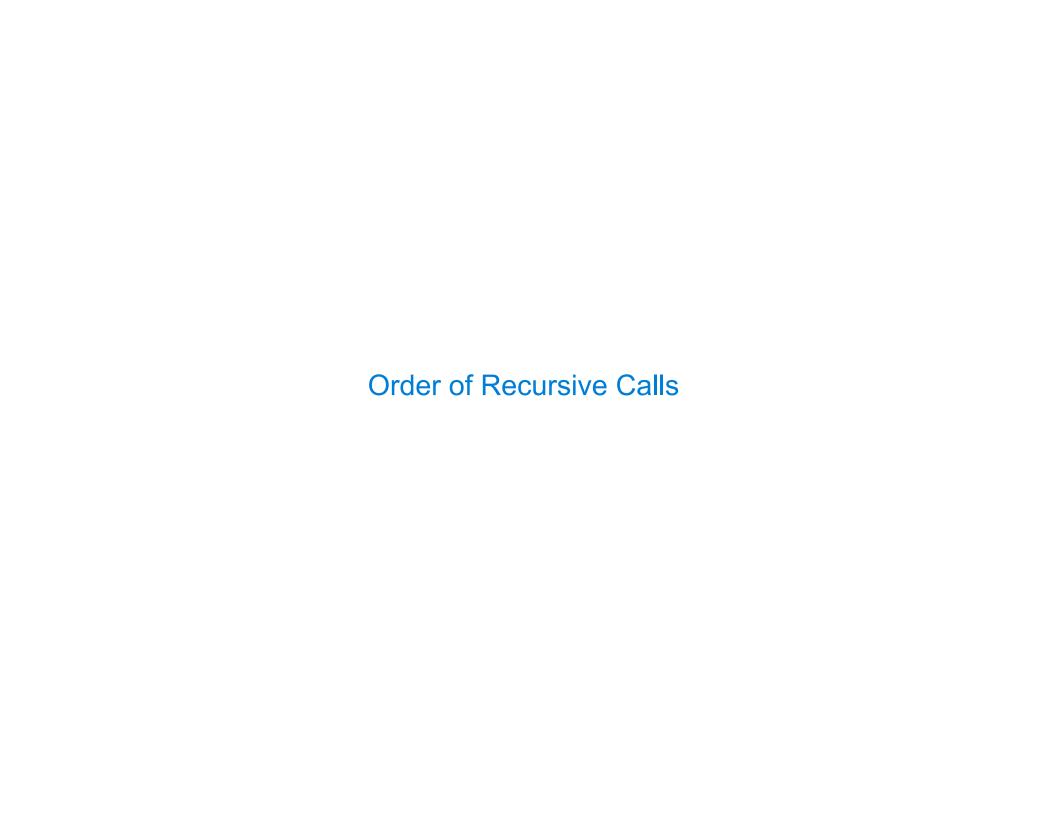
Chenyang Yuan Joseph Hui

Fall 2013 Winners

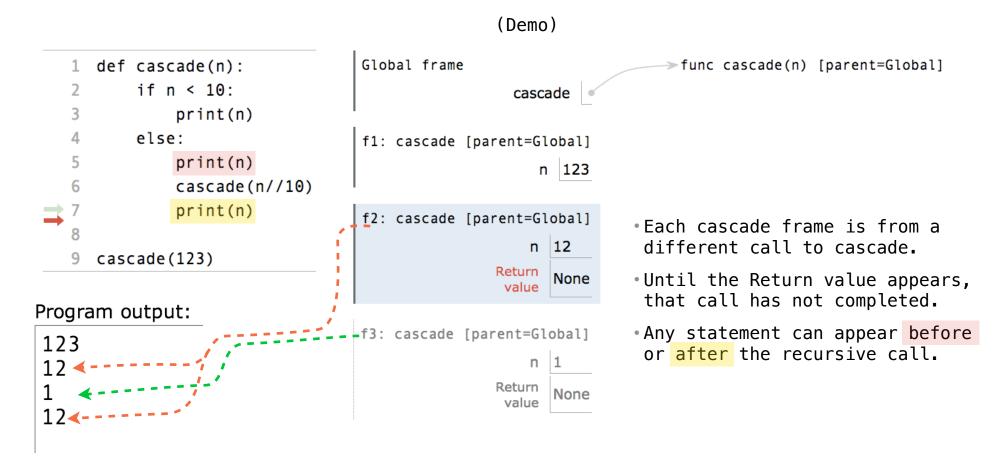
Paul Bramsen Sam Kumar & Kangsik Lee Kevin Chen

Fall 2014 Winners

YOUR NAME COULD BE HERE... FOREVER!



The Cascade Function



Two Definitions of Cascade

(Demo)

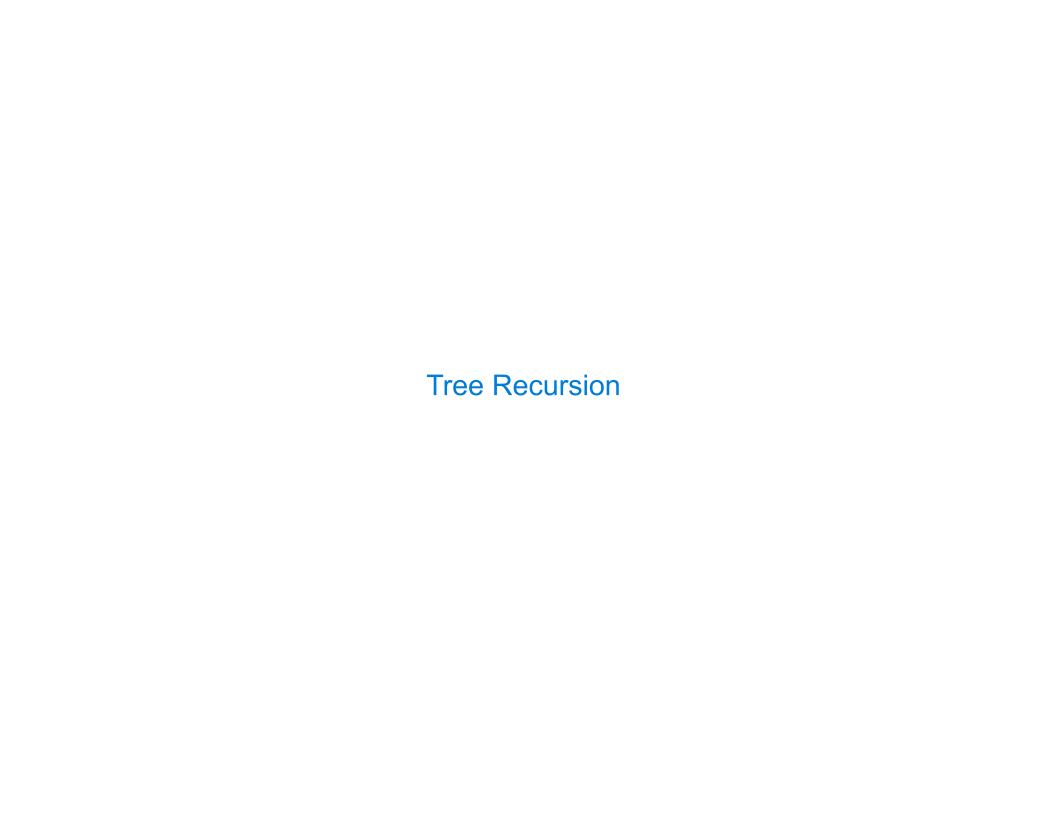
- If two implementations are equally clear, then shorter is usually better
- In this case, the longer implementation is more clear (at least to me)
- When learning to write recursive functions, put the base cases first
- Both are recursive functions, even though only the first has typical structure

Example: Inverse Cascade

Inverse Cascade

```
Write a function that prints an inverse cascade:
```

8



Tree Recursion

Tree-shaped processes arise whenever executing the body of a recursive function makes more than one call to that function.

```
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35

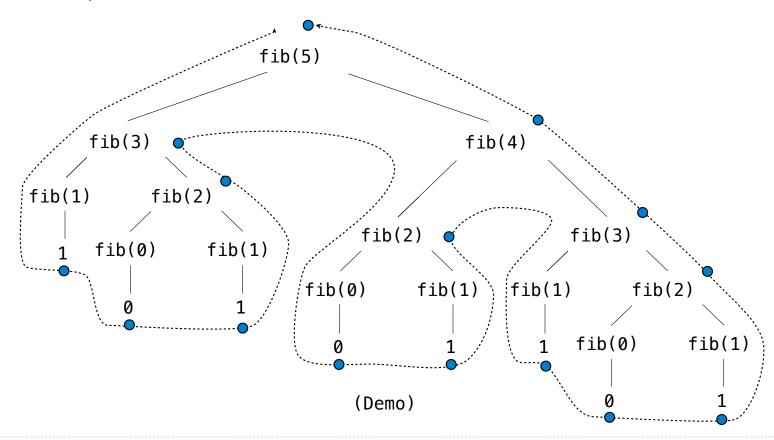
fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465
```

```
def fib(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return fib(n-2) + fib(n-1)
```



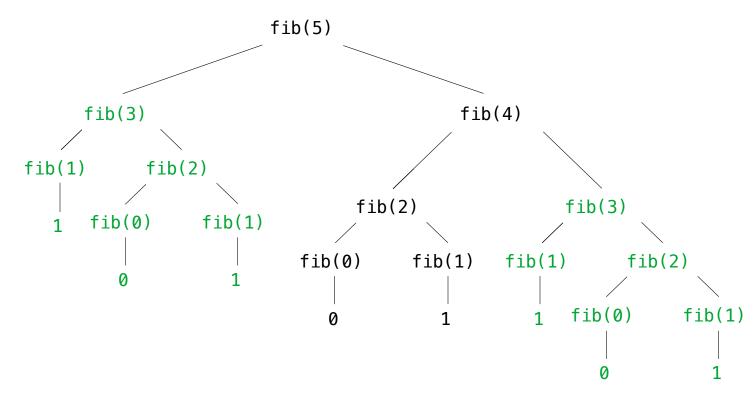
A Tree-Recursive Process

The computational process of fib evolves into a tree structure



Repetition in Tree-Recursive Computation

This process is highly repetitive; fib is called on the same argument multiple times.



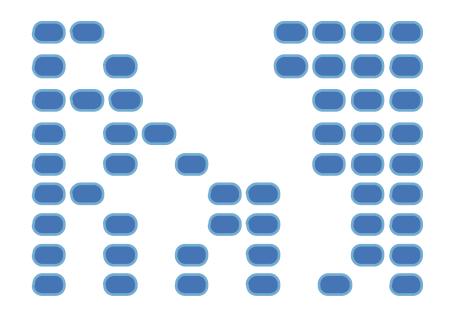
We can speed up this computation dramatically in a few weeks by remembering results.

Example: Counting Partitions

Counting Partitions

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

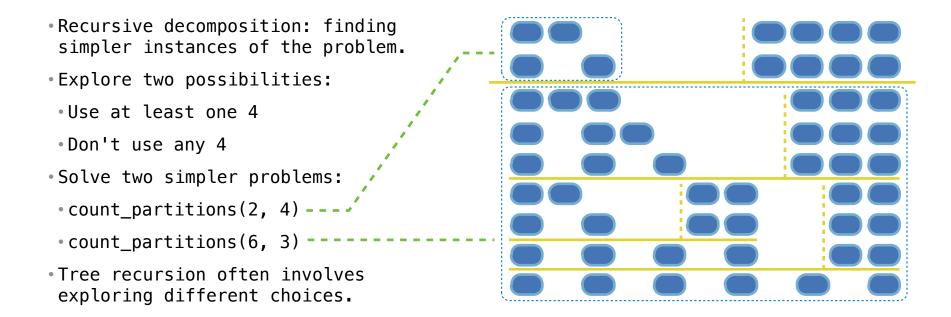
count_partitions(6, 4)



Counting Partitions

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

count_partitions(6, 4)



Counting Partitions

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

```
def count partitions(n, m):

    Recursive decomposition: finding

                                           if n == 0:
simpler instances of the problem.
                                              return 1
• Explore two possibilities:
                                           elif n < 0:
                                              return 0
•Use at least one 4
                                           elif m == 0:
Don't use any 4
                                              return 0
•Solve two simpler problems:
                                           else:
                                     • count partitions(2, 4) ----
                                               without m = count partitions(n, m-1)
•count_partitions(6, 3) -----
                                               return with m + without m

    Tree recursion often involves

exploring different choices.
                                      (Demo)
```

<u>Interactive Diagram</u>