61A Lecture 8

Wednesday, September 17

Announcements

- Project 1 is due Thursday 9/18 @ 11:59pm; Early bonus point for submitting on Wednesday!
- Project Party in Stern Main Lounge (Stern Hall in Unit 4) 8pm-10pm on Wednesday 9/17
- •Midterm 1 is on Monday 9/22 from 7pm to 9pm
- *2 review sessions on Saturday 9/20 3pm-4:30pm and 4:30pm-6pm in 1 Pimentel
- *HKN review session moved to Sunday 9/21, time/location TBD
- •Includes topics up to and including this lecture
- *Closed book/note exam, except for one page of hand-written notes and a study guide
- "Cannot attend? Fill out the conflict form by Wednesday 9/17 @ 5pm!
- *Optional Hog strategy contest ends Wednesday 10/1 @ 11:59pm

Hog Contest Rules

- Up to two people submit one entry; Max of one entry per person
- Your score is the number of entries against which you win more than 50% of the time
- All strategies must be deterministic, pure functions of the current player scores
- All winning entries will receive 2 points of extra credit
- The real prize: honor and glory

Fall 2011 Winners

Kaylee Mann Yan Duan & Ziming Li Brian Prike & Zhenghao Qian Parker Schuh & Robert Chatham

Fall 2012 Winners

Chenyang Yuan Joseph Hui

Fall 2013 Winners

Paul Bramsen Sam Kumar & Kangsik Lee Kevin Chen

Fall 2014 Winners

YOUR NAME COULD BE HERE... FOREVER!

Order of Recursive Calls

```
The Cascade Function
                                                      (Demo)
       1 def cascade(n):
                                       Global frame
                                                                         > func cascade(n) [parent=Global]
              if n < 10:
print(n)
              else:
                                       f1: cascade [parent=Global]
                  print(n)
cascade(n//10)
                                                          n 123
                 print(n)
                                       f2: cascade [parent=Global]

    Each cascade frame is from a
different call to cascade.

                                                         n 12
       9 cascade(123)
                                                      Return value None
                                                                     *Until the Return value appears, that call has not completed.
   Program output:
   • Any statement can appear before or after the recursive call.
                                           Interactive Diagram
```

Two Definitions of Cascade

(Demo)

```
def cascade(n):
    if n < 10:
        print(n)
    else:
        print(n)</pre>
                          cascade(n//10)
print(n)
```

def cascade(n):
 print(n)
 if n >= 10:
 cascade(n//10)
 print(n)

- · If two implementations are equally clear, then shorter is usually better
- · In this case, the longer implementation is more clear (at least to me)
- · When learning to write recursive functions, put the base cases first
- $\boldsymbol{\cdot}$ Both are recursive functions, even though only the first has typical structure

Example: Inverse Cascade

Inverse Cascade

Write a function that prints an inverse cascade:

```
def inverse_cascade(n):
    grow(n)
1
12
                       print(n)
123
                       shrink(n)
1234
123
                  def f_then_g(f, g, n):
    if n:
       f(n)
12
                            g(n)
                   grow = lambda n: f_then_g(
                   shrink = lambda n: f_then_g(
```

Tree Recursion

Tree Recursion

```
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35
fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465
```

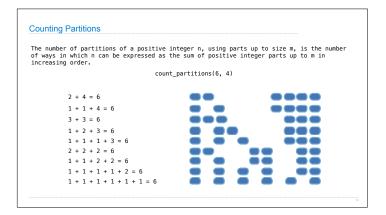
def fib(n):
 if n == 0:
 return 0
 elif n == 1:
 return 1
 else:
 return fib(n-2) + fib(n-1)



http://en.wikipedia.org/wiki/File:Fibonacci.jpg

A Tree-Recursive Process The computational process of fib evolves into a tree structure fib(5) fib(3) o fib(4) fib(1) fib(2) fib(2) 🗨 fib(3) fib(0) fib(1) fib(1) fib(1) fib(2) fib(0) (Demo)

Example: Counting Partitions



Counting Partitions The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order. count_partitions(6, 4) Recursive decomposition: finding simpler instances of the problem. Explore two possibilities: Use at least one 4 Don't use any 4 Solve two simpler problems: count_partitions(2, 4) -- count_partitions(6, 3) Tree recursion often involves exploring different choices.

Counting Partitions