CS 61A Lecture 12

Monday, September 29

Announcements

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- Homework 3 due Wednesday 10/1 @ 11:59pm

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Box-and-Pointer Notation

The Closure Property of Data Types

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Lists can contain lists as elements

Box-and-Pointer Notation in Environment Diagrams

Interactive Diagram

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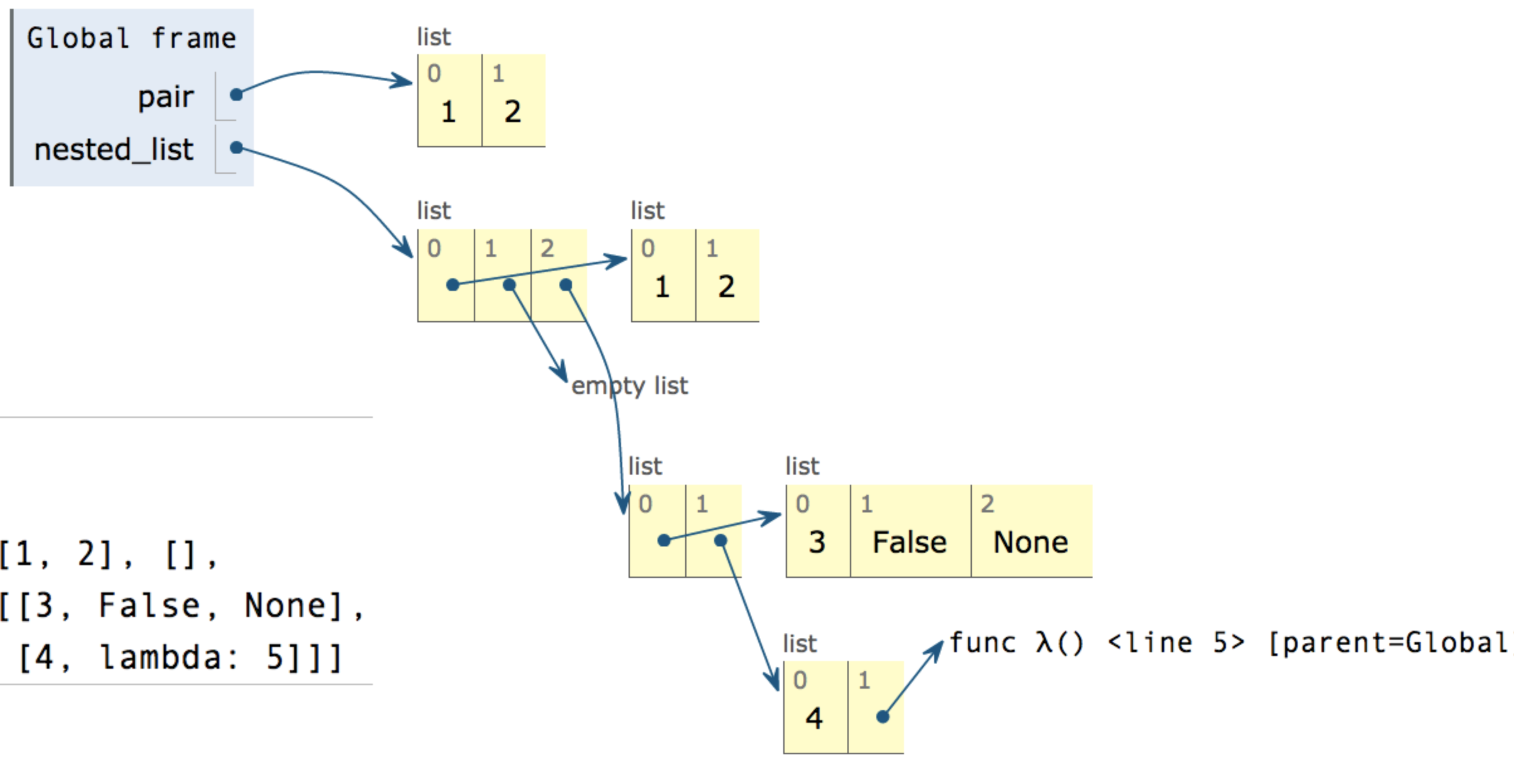


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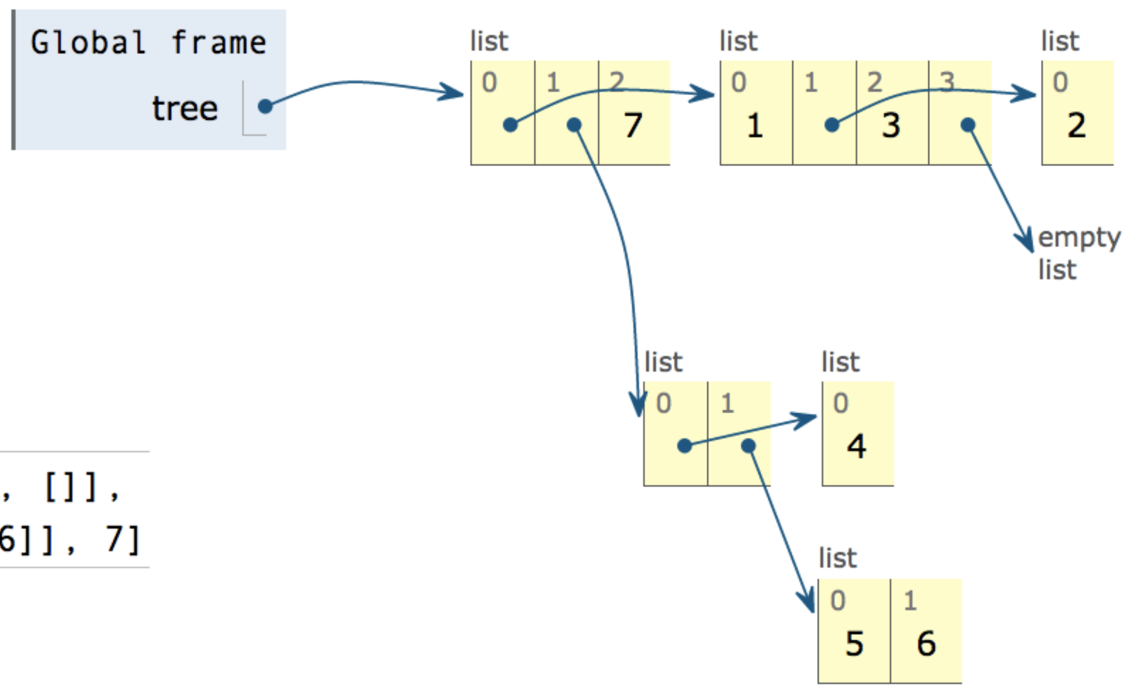


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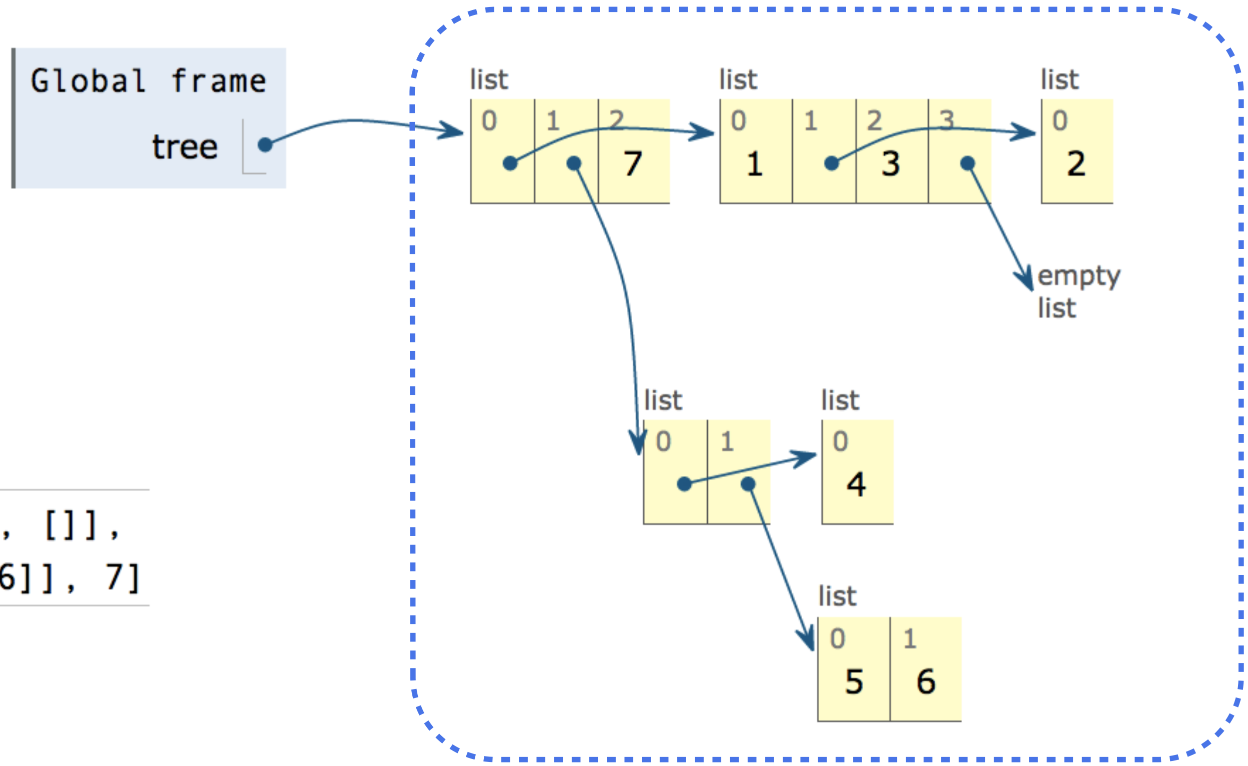


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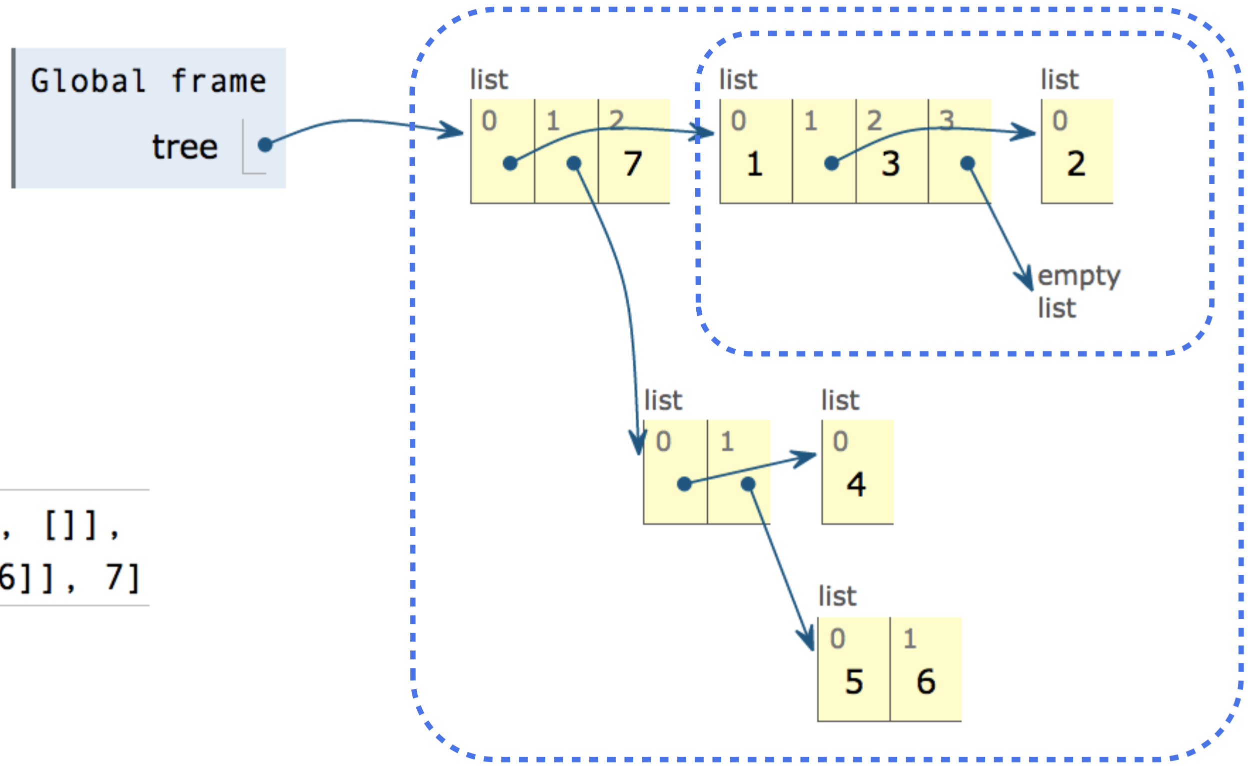


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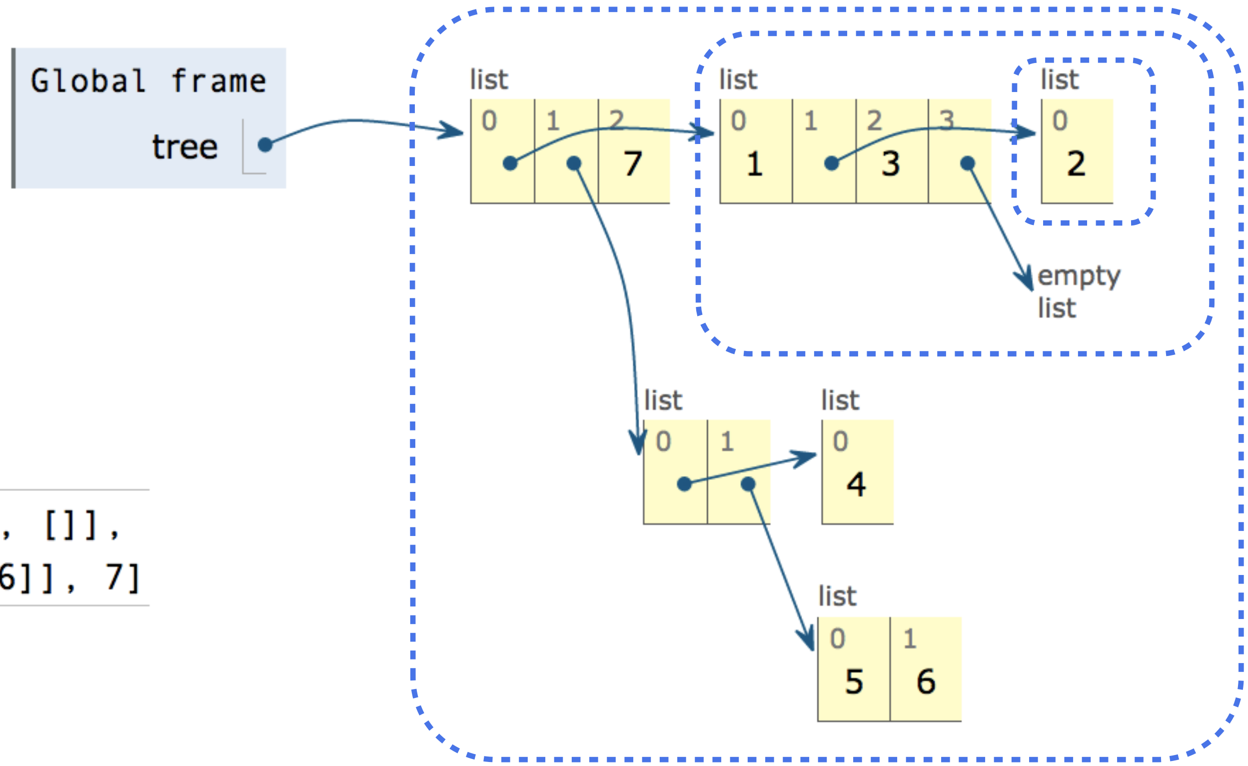


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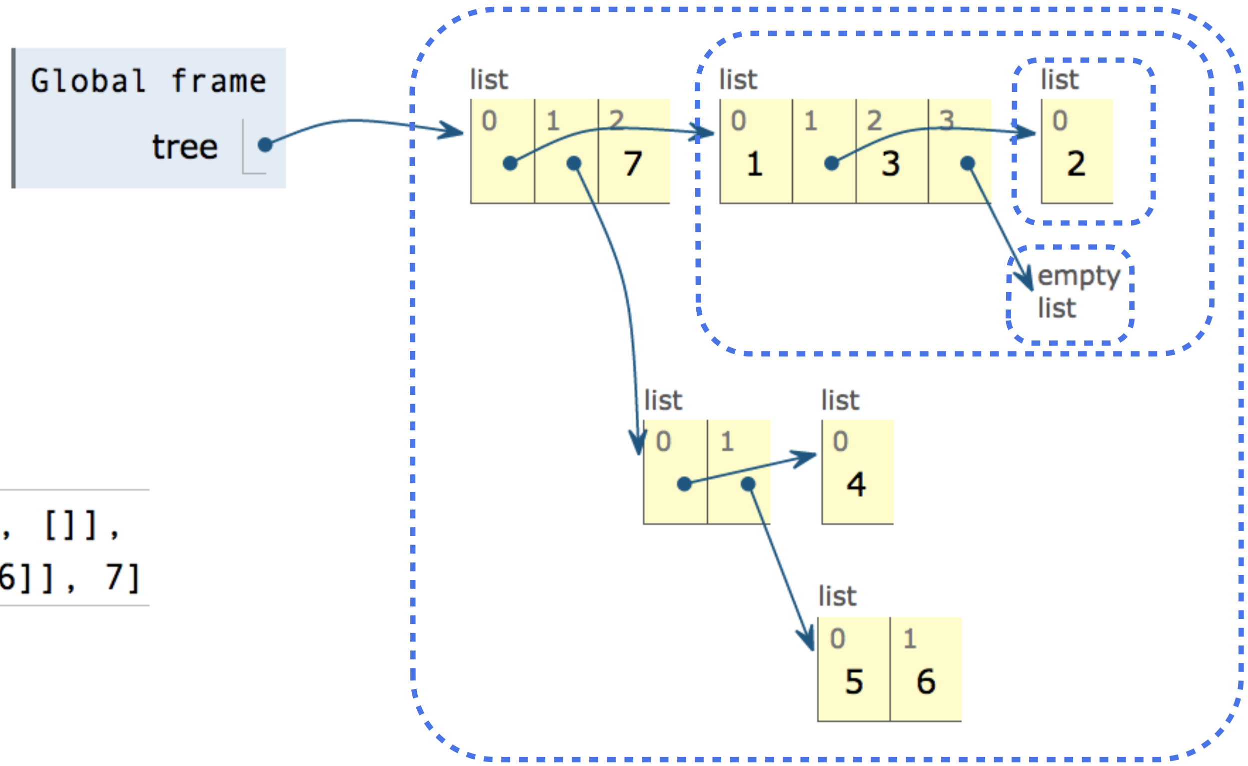


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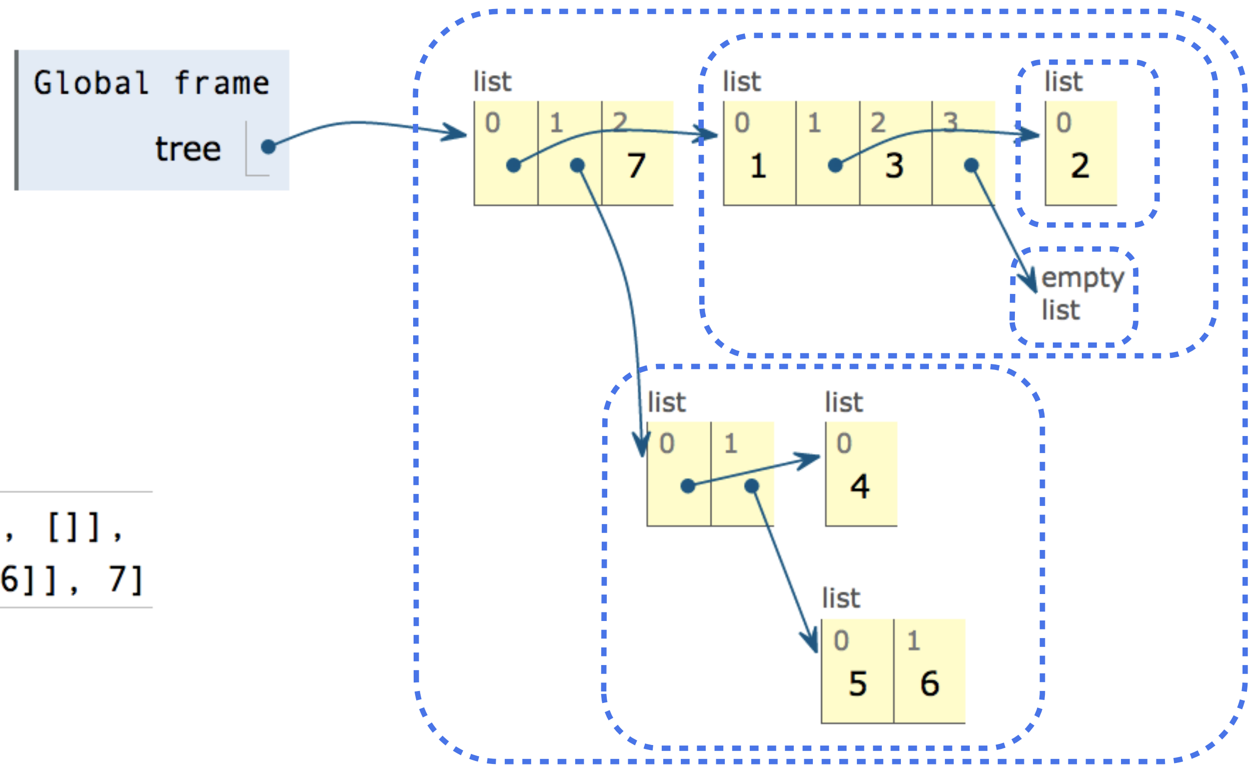


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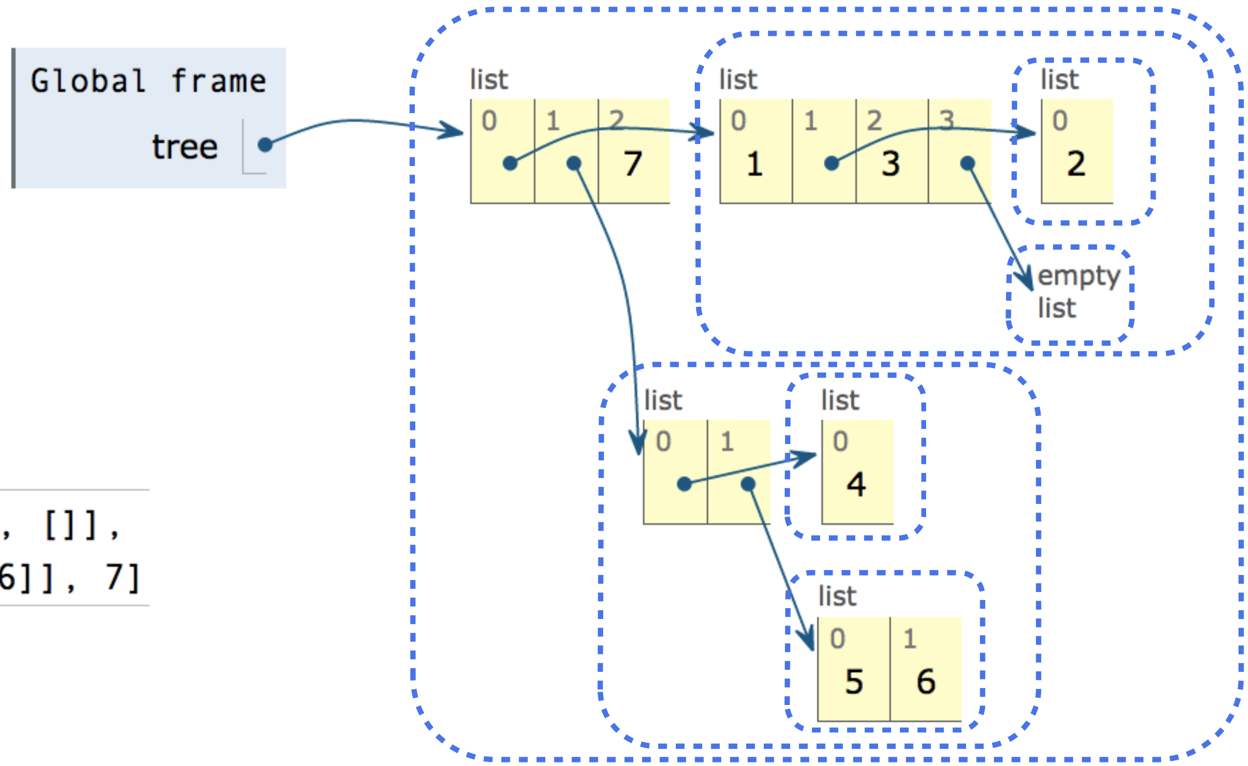


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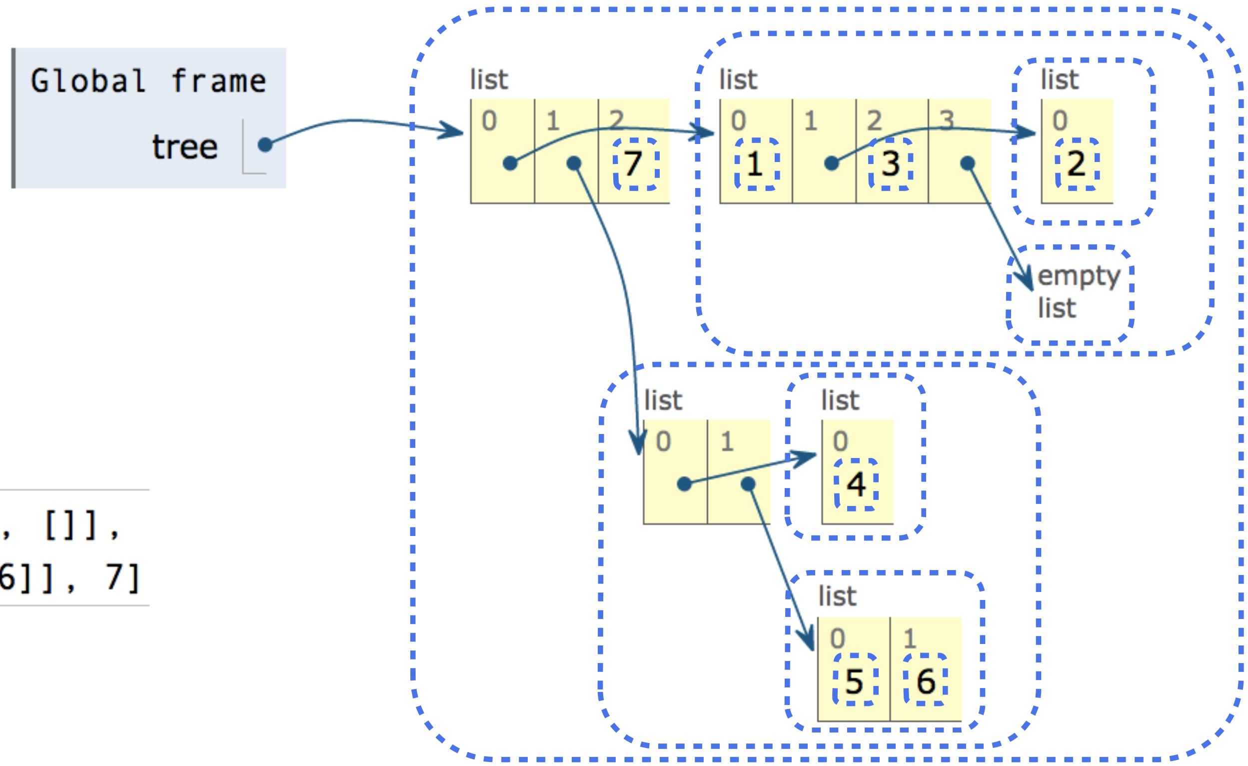


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Sequence Operations

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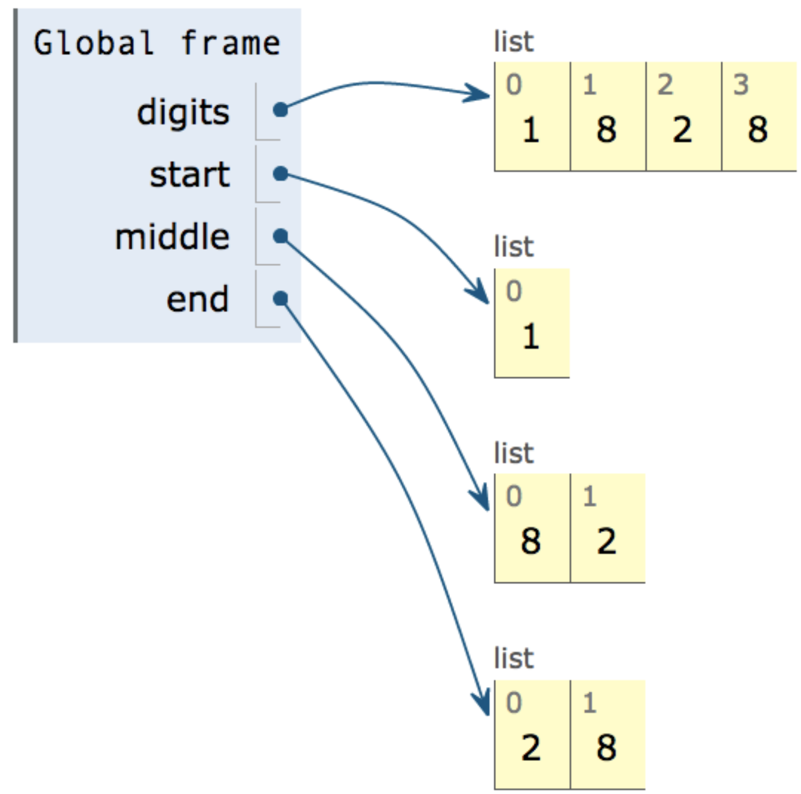

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"Line feed" character represents a new line

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>>> city = 'Berkeley'
>>> len(city)
8
>>> city[3]
'k'
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Length and element selection are similar to all sequences

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When working with strings, we usually care about whole words more than letters

Dictionaries

```
{'Dem': 0}
```

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If you want to associate multiple values with a key, store them all in a sequence value