# 61A Lecture 22

Wednesday, October 22

#### Announcements

Project 3 is due Thursday 10/23 @ 11:59pm
Please submit two ways: the normal way and using python3 ok --submit!
You can view your ok submission on the ok website: http://ok.cs61a.org
Midterm 2 is on Monday 10/27 7pm-9pm
Review session on Saturday 10/25 3pm-6pm in 2050 VLSB
Conflict form submissions are due Wednesday 10/22!

Sets

#### Sets

One more built-in Python container type
Set literals are enclosed in braces
Duplicate elements are removed on construction
Sets are unordered, just like dictionary entries

```
>>> s = {3, 2, 1, 4, 4}
>>> s
{1, 2, 3, 4}
>>> 3 in s
True
>>> len(s)
4
>>> s.union({1, 5})
{1, 2, 3, 4, 5}
>>> s.intersection({6, 5, 4, 3})
{3, 4}
```

#### Implementing Sets

What we should be able to do with a set:

- Membership testing: Is a value an element of a set?
- Union: Return a set with all elements in set1 or set2
- Intersection: Return a set with any elements in set1 and set2
- Adjoin: Return a set with all elements in s and a value v



Sets as Unordered Sequences

#### Sets as Unordered Sequences

Proposal 1: A set is represented by a linked list that contains no duplicate items.

Time order of growth def empty(s):  $\Theta(1)$ return s is Link.empty def set contains(s, v): Time depends on whether """Return whether set s contains value v. & where v appears in s >>> s = Link(1, Link(2, Link(3)))  $\Theta(n)$ >>> set contains(s, 2) Assuming v either True ..... does not appear in s or if empty(s): appears in a uniformly return False distributed random location elif s.first == v: return True else: return set\_contains(s.rest, v) (Demo)

#### Sets as Unordered Sequences



Sets as Ordered Sequences

### Sets as Ordered Sequences

Proposal 2: A set is represented by a linked list with unique elements that is
ordered from least to greatest

Parts of the program that	Assume that sets are	Using
Use sets to contain values	Unordered collections	<pre>empty, set_contains, adjoin_set,     intersect_set, union_set</pre>
Implement set operations	Ordered linked lists	first, rest, <, >, ==

Different parts of a program may make different assumptions about data

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Sets as Ordered Sequences

Proposal 2: A set is represented by a linked list with unique elements that is
ordered from least to greatest

```
def intersect_set(set1, set2):
    if empty(set1) or empty(set2):
        return Link.empty
    else:
        el, e2 = set1.first, set2.first
        if e1 == e2:
            return Link(e1, intersect_set(set1.rest, set2.rest))
        elif e1 < e2:
            return intersect_set(set1.rest, set2)
        elif e2 < e1:
            return intersect_set(set1, set2.rest)
        Order of growth? Θ(n)</pre>
```

Sets as Binary Search Trees

### **Binary Search Trees**

Proposal 3: A set is represented as a Tree with two branches. Each entry is:
 Larger than all entries in its left branch and
 Smaller than all entries in its right branch



#### **Binary Tree Class**

A binary tree is a tree that has a left branch and a right branch

**Idea:** Fill the place of a missing left branch with an empty tree

Idea 2: An instance of BinaryTree
always has exactly two branches



```
class BinaryTree(Tree):
    empty = Tree(None)
    empty.is_empty = True
    def init (self, entry, left=empty, right=empty):
        Tree.__init__(self, entry, (left, right))
        self.is empty = False
    @property
    def left(self):
        return self.branches[0]
    @property
    def right(self):
        return self.branches[1]
Bin = BinaryTree
t = Bin(3, Bin(1),
           Bin(7, Bin(5),
                  Bin(9, Bin.empty,
                         Bin(11))))
```

## Membership in Binary Search Trees

#### set\_contains traverses the tree

If the element is not the entry, it can only be in either the left or right branchBy focusing on one branch, we reduce the set by about half with each recursive call

```
def set_contains(s, v):
    if s.is_empty:
        return False
    elif s.entry == v:
        return True
    elif s.entry < v:
        return set_contains(s.right, v)
    elif s.entry > v:
        return set_contains(s.left, v)
```



Order of growth?  $\Theta(h)$  on average  $\Theta(\log n)$  on average for a balanced tree

# Adjoining to a Tree Set

