61A Lecture 24

Wednesday, October 29

Announcements

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- CS 61A flash mob Wednesday 3:03pm–3:09pm in Memorial Glade

Scheme

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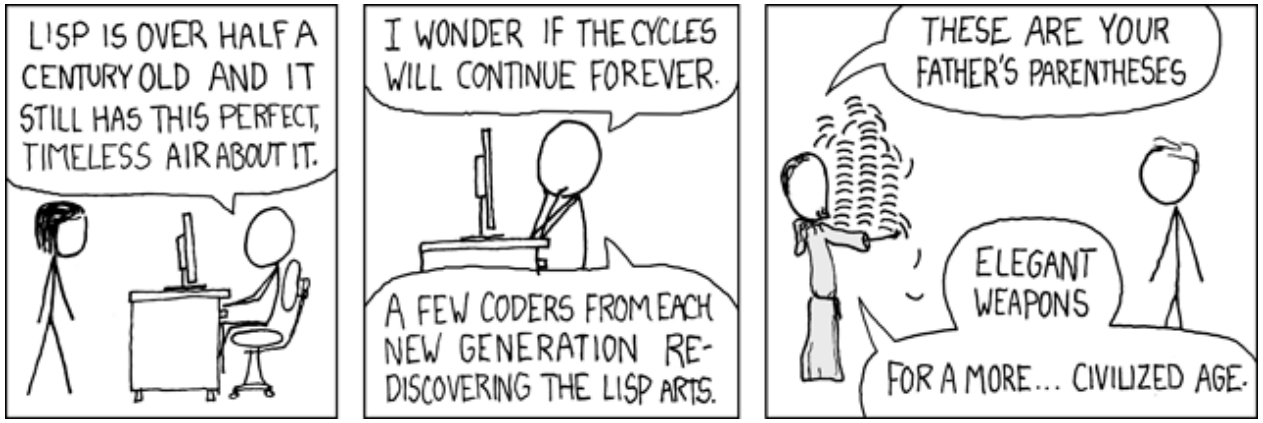

http://imgs.xkcd.com/comics/lisp_cycles.png

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Scheme Interpreters

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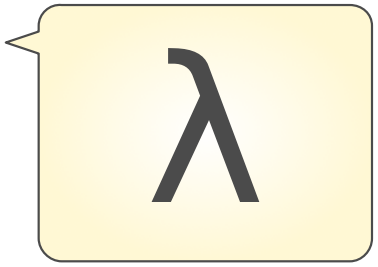

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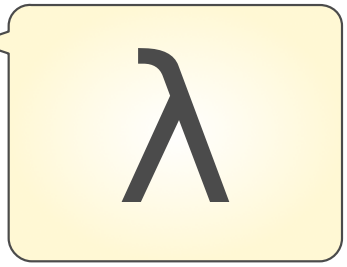

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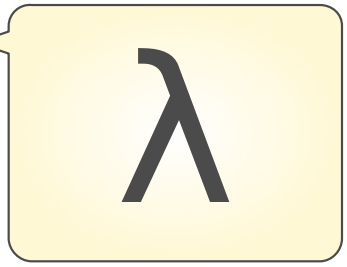

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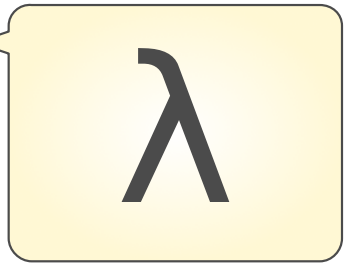

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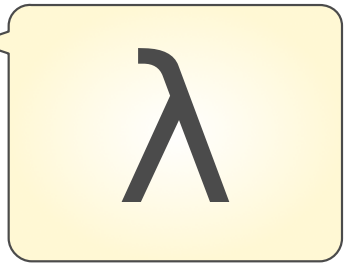

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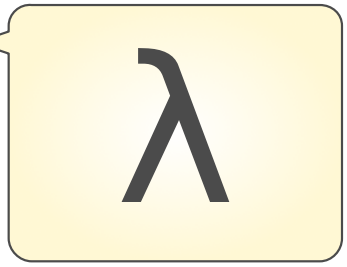

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Pairs and Lists

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(Demo)

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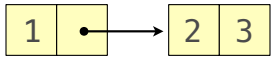

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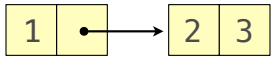

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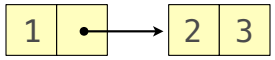

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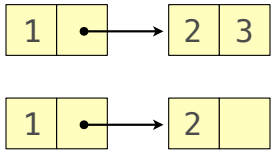

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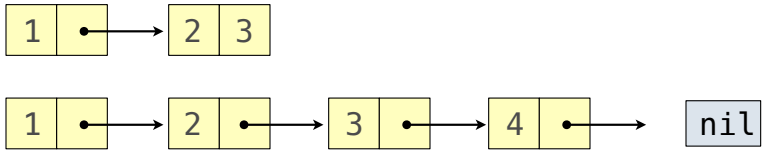

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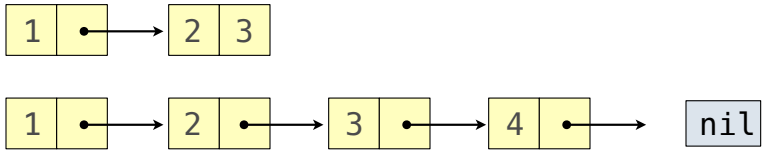

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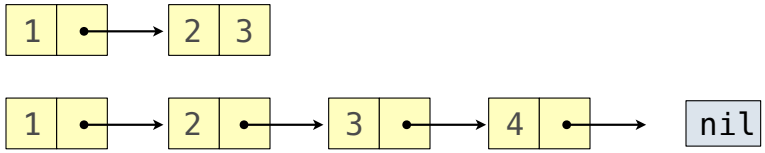

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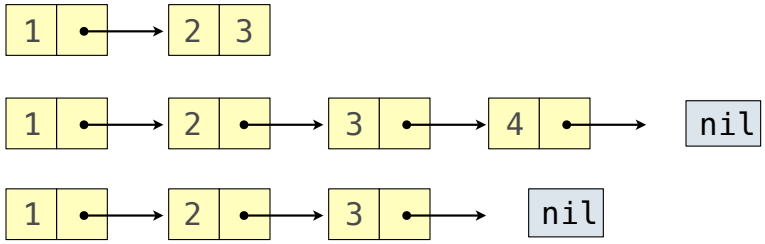

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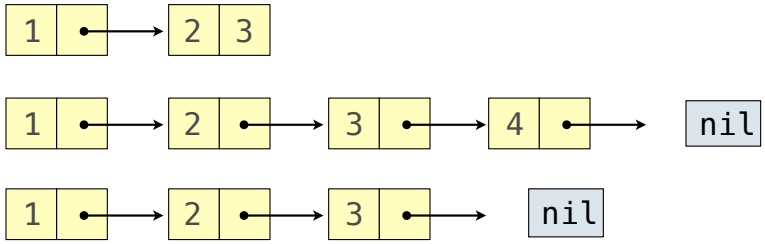

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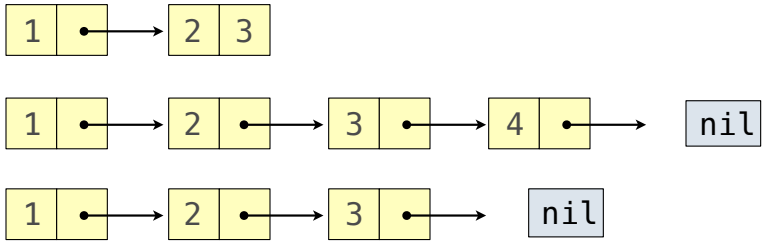

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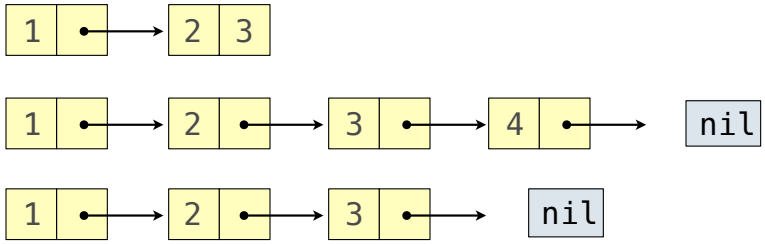

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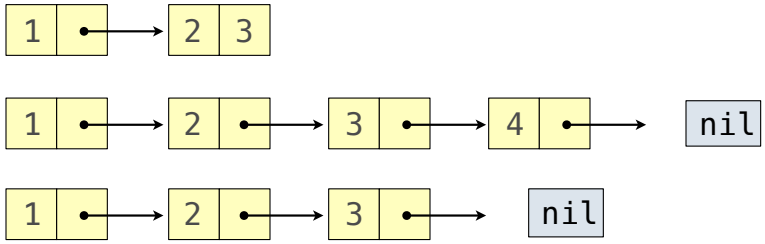

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Sierpinski's Triangle

(Demo)