

CONTROL AND HIGHER ORDER FUNCTIONS 2

COMPUTER SCIENCE 61A

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1 Control

Control structures direct the flow of logic in a program. This can mean skipping a portion of code (*conditionals*) or repeating a portion of code multiple times (*iteration*).

1.1 Conditional Statements

Conditional statements let programs execute different lines of code depending certain conditions. The conditional statement in Python is an **if-elif-else** block:

```
if <conditional expression>:
    <suite of statements>
elif <conditional expression>:
    <suite of statements>
else:
    <suite of statements>
```

Some notes:

- The `else` and `elif` statements are optional.
- You can have any number of `elif` statements.
- A **conditional expression** is a Python expression. All that matters for control is whether its value is a true value or a false value.
- The code that is executed is the **suite** that is indented under the first `if/elif` that has a true **conditional expression**. If none are true, then the `else` suite is executed.
- Once one suite is executed, the rest are skipped.

Note: in Python, there are a few things that are treated as false values:

- The boolean `False`
- The integer `0`
- The value `None`
- And more... (we will learn about these later in the semester)

Python also includes **boolean operators** `and`, `or`, and `not`. These operators are used to combine and manipulate boolean values.

- `not True` evaluates to `False`, and `not False` evaluates to `True`.
- `True and True` evaluates to `True`, but a false value on either side makes it `False`.
- `False or False` evaluates to `False`, but a true value on either side makes it `True`.

1.2 Question

1. It's lecture time! However, whether you go depends on certain conditions about timing, seats, and laziness. Write a simple function `which_lecture` that takes in inputs `time`, `seats_left`, `is_lazy` and prints out your decision.

- `which_lecture` should print "go to lecture" if time is before 2:00pm, there are seats, and you are not lazy.
- `which_lecture` should print "go to alt lecture" if time is after 2:00pm or there are no seats, and you are not lazy.
- `which_lecture` should print "watch videos" if you feel lazy.

`time` is in military format; e.g 2:20pm is 1420. `seats_left` is a non-negative integer. `is_lazy` is a boolean variable.

```
def which_lecture(time, seats_left, is_lazy):
```

1.3 Iteration

Iteration lets a program repeat statements multiple times. A common iterative block of code is the `while` loop:

```
while <conditional clause>:  
    <body of statements>
```

This block of code states: “while the conditional clause is still `True`, continue executing the indented body of statements.” Here is an example:

```
>>> def countdown(x):  
...     while x > 0:  
...         print(x)  
...         x = x - 1  
...     print("Blastoff!")  
...  
>>> countdown(3)  
3  
2  
1  
Blastoff!
```

1.4 Questions

1. Fill in the `is_prime` function, which returns `True` if `n` is a prime number and `False` otherwise.

Hint: use the `%` operator: `x % y` returns the remainder of `x` is divided by `y`.

```
def is_prime(n):
```

2. Fill in the `choose` function, which returns the number of ways to choose k items from n items. Mathematically, `choose(n, k)` is defined as:

$$\frac{n \times (n - 1) \times (n - 2) \times \cdots \times (n - k + 1)}{k \times (k - 1) \times (k - 2) \times \cdots \times 2 \times 1}$$

```
def choose(n, k):  
    """Returns the number of ways to choose K items from  
       N items.  
  
    >>> choose(5, 2)  
    10  
    >>> choose(20, 6)  
    38760  
    """
```

2 Higher Order Functions

A function that manipulates other functions is called a *higher order function* (HOF). A HOF can be a function that takes functions as arguments, returns a function, or both.

2.1 Functions as Argument Values

Suppose we want to *square* or *double* every natural number from 1 to n and print the result as we go. Fill in the functions `square_every_number` and `double_every_number` by using the `square` and `double` functions we have defined.

```
def square(x):
    return x * x
def square_every_number(n):
    """Prints out the square of every integer from 1 to n.
    >>> square_every_number(3)
    1
    4
    9
    """
```

```
def double(x):
    return 2 * x
def double_every_number(n):
    """Prints out the double of every integer from 1 to n.
    >>> double_every_number(3)
    2
    4
    6
    """
```

The only difference between `square_every_number` and `double_every_number` is the function called before printing (either `square` or `double`). Everything else is the same!

It would be nice to have a generalized function (let's call it the `every` function) that took care of the `while` loop and the incrementing for us. That way, we could `triple_every_number` or `cube_every_number` without repeating so much code:

```
def square_every_number(n):  
    every(square, n)
```

```
def double_every_number(n):  
    every(double, n)
```

```
def cube(x):  
    return x * x * x
```

```
def cube_every_number(n):  
    every(cube, n)
```

2.2 Questions

1. Implement the function `every` that takes in a function `func` and a number `n`, and prints the result of applying that function to each of the first `n` natural numbers.

```
def every(func, n):  
    """Prints out all integers from 1 to n with func applied  
    on them.
```

```
>>> def square(x):  
...     return x * x  
>>> every(square, 3)  
1  
4  
9  
"""
```

2. Similarly, implement a function `keep`, which takes in a function `cond` and a number `n`, and only prints a number from 1 to `n` to the screen if calling `cond` on that number returns `True`:

```
def keep(cond, n):
```

```
"""Prints out all integers from 1 to n that return True
when called with cond.

>>> def is_even(x):
...     # Even numbers have remainder 0 when divided by 2.
...     return x % 2 == 0
>>> keep(is_even, 5)
2
4
"""
```

2.3 Functions as Return Values

Often, we will need to write a function that returns another function. One way to do this is to *define a function inside of a function*:

```
def outer(x):
    def inner(y):
        ...
    return inner
```

Note two things:

1. The return value of the `outer` function is `inner`! This is where *a function returns a function*.
2. In this case, the `inner` function is defined inside of the `outer` function. This is a common pattern, but it is not necessary — we could have defined `inner` outside of the `outer` and still keep the `return` statement the same.

2.4 Moar Questions

1. Write a function `and_add` that takes a function `f` (such that `f` is a function of one argument) and a number `n` as arguments. It should return a function that takes one argument, and does the same thing as the function `f`, except also adds `n` to the result.

```
def and_add(f, n):
    """Returns a new function. This new function takes an
       argument
       x and returns f(x) + n.

    >>> def square(x):
    ...     return x * x
    >>> new_square = and_add(square, 3)
    >>> new_square(4)    # 4 * 4 + 3
    19
    """
```

2. The following code has been loaded into the python interpreter:

```
def skipped(f):
    def g():
        return f
    return g
def composed(f, g):
    def h(x):
        return f(g(x))
    return h
def added(f, g):
    def h(x):
        return f(x) + g(x)
    return h
def square(x):
    return x*x
def two(x):
    return 2
```

What will python output when the following lines are evaluated?

```
>>> composed(square, two) (7)
```

```
>>> skipped(added(square, two)) () (3)
```



```
>>> composed(two, square) (2)
```

3. Draw the environment diagram that results from running the following code.

```
n = 7
def f(x):
    n = 8
    return x + 1
def g(x):
    n = 9
    return x + 3
def f(f, x):
    return f(f(x+2))
m = f(g, n)
```

4. Draw the environment diagram for the following code:

```
from operator import add
def curry2(h):
    def f(x):
        def g(y):
            return h(x,y)
        return g
    return f
```

```
make_adder = curry2(add)
add_three = make_adder(3)
five = add_three(2)
```