

61A Lecture 2

Announcements

Names, Assignment, and User-Defined Functions

(Demo)

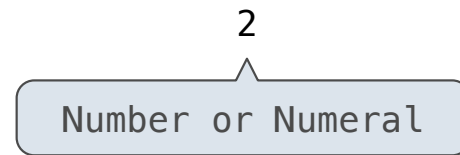
Types of Expressions

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Primitive expressions:

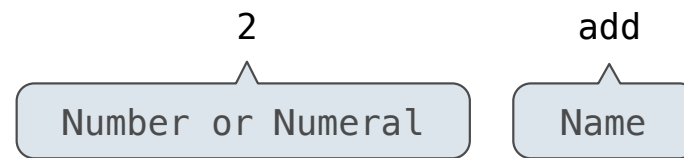
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Call expressions:

Types of Expressions

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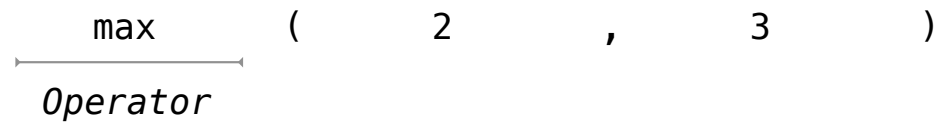
max (2 , 3)

Types of Expressions

Primitive expressions:



Call expressions:

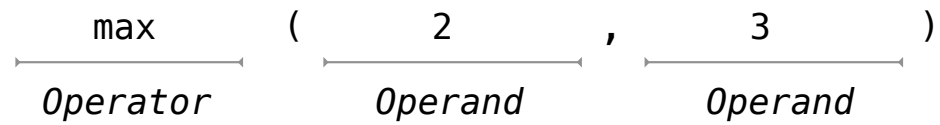


Types of Expressions

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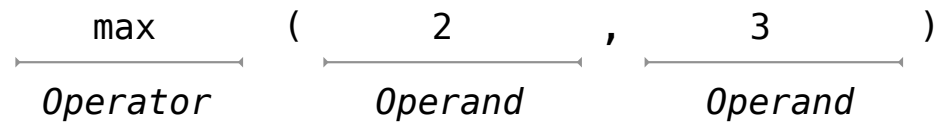


Types of Expressions

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Call expressions:



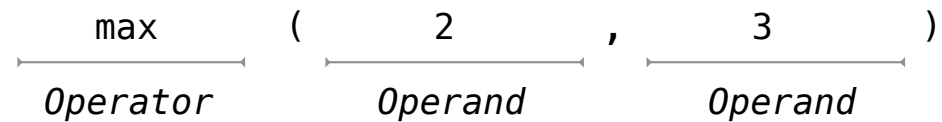
`max(min(pow(3, 5), -4), min(1, -2))`

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Call expressions:

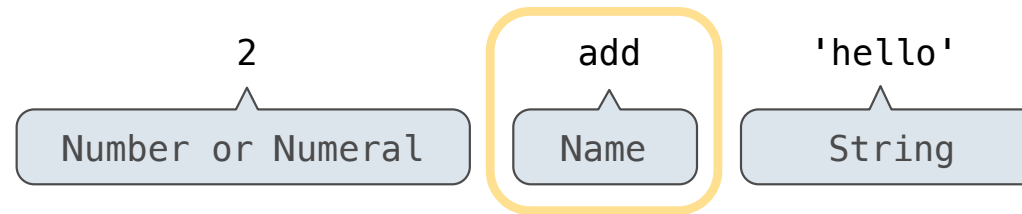


An operand can also be a call expression

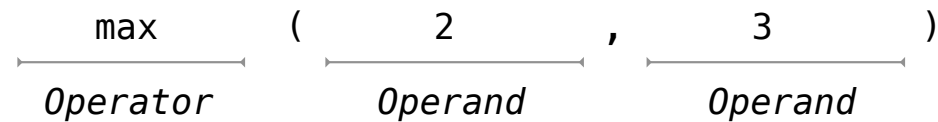
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Discussion Question 1

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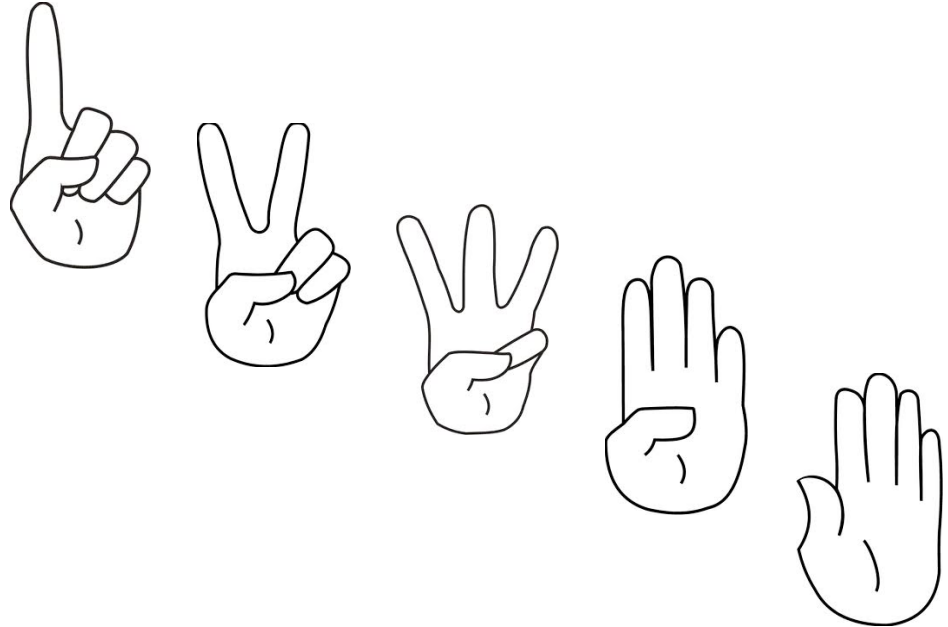
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Environment Diagrams

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Environment diagrams visualize the interpreter's process.

Interactive Diagram

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```
→ 1 from math import pi  
→ 2 tau = 2 * pi
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[Interactive Diagram](#)

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Global frame  
pi 3.1416
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[Interactive Diagram](#)

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Code (left):

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Global frame  
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Frames (right):

[Interactive Diagram](#)

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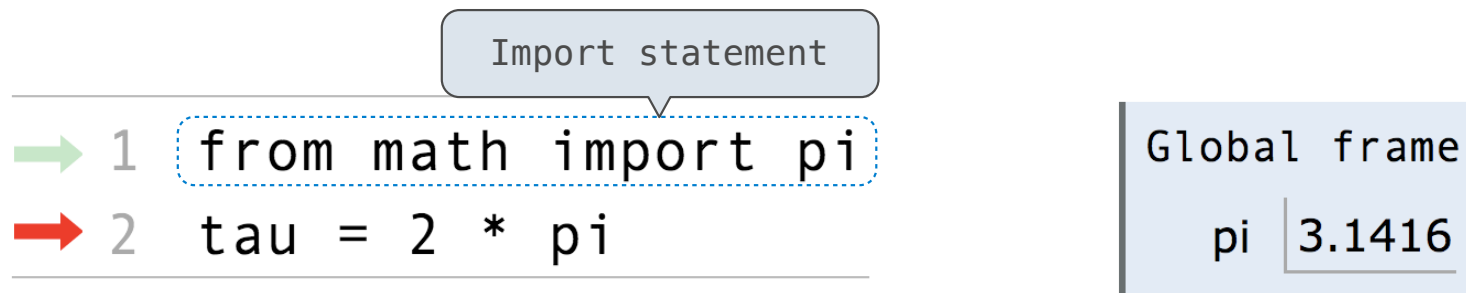
Statements and expressions

Frames (right):

[Interactive Diagram](#)

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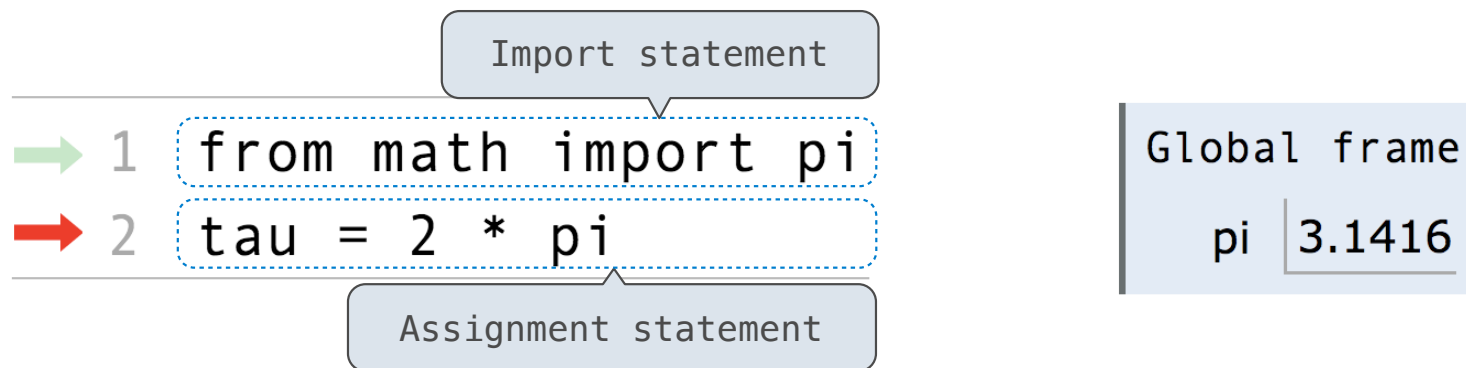
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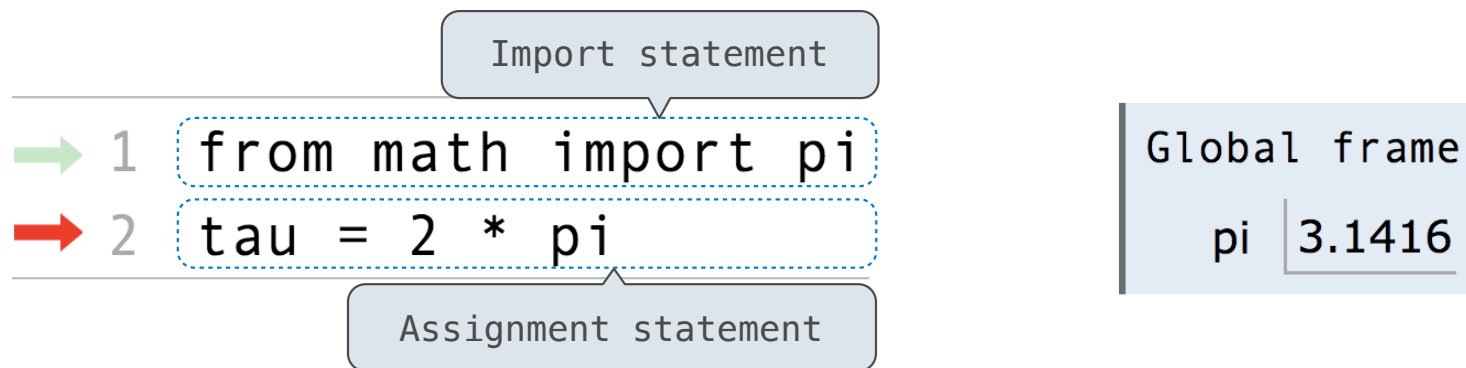
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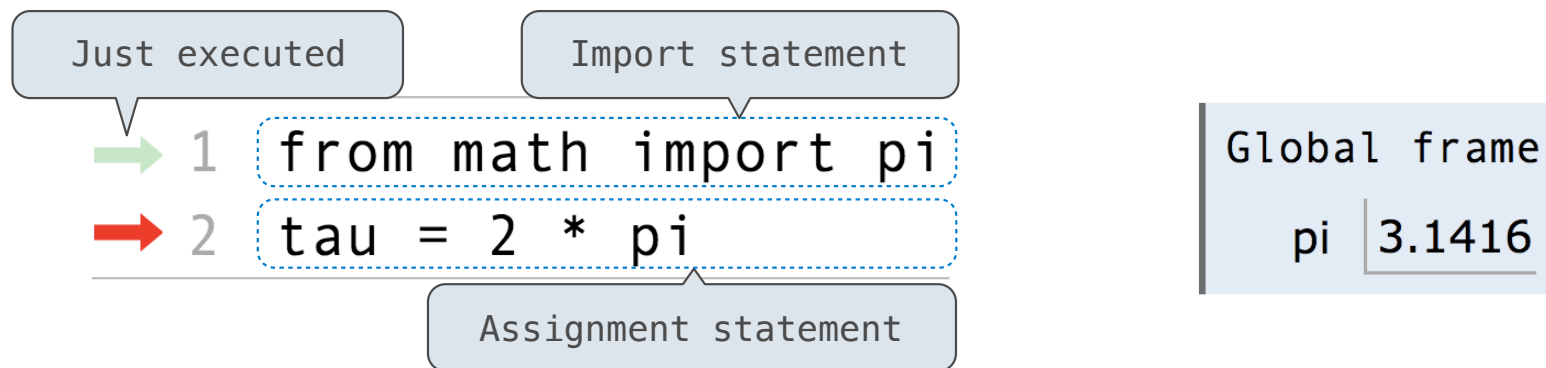
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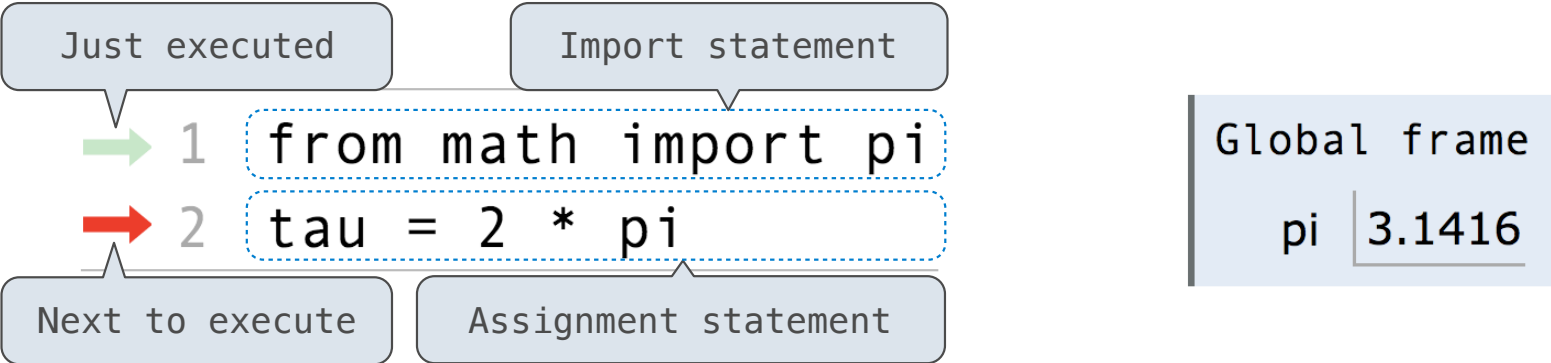
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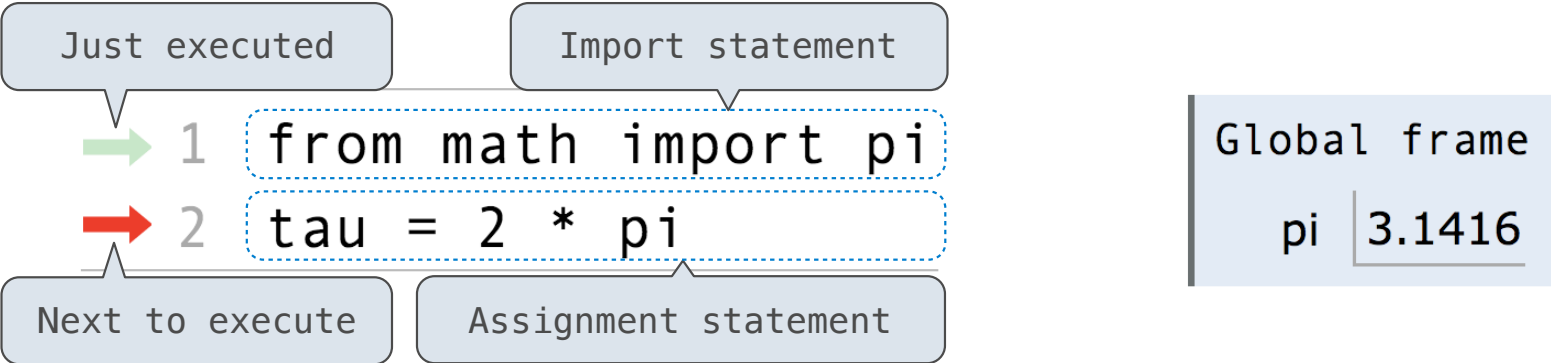
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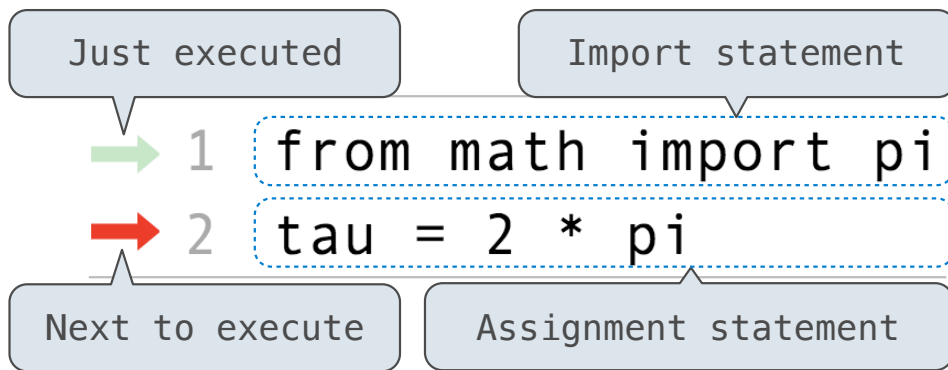
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Frames (right):

Each name is bound to a value

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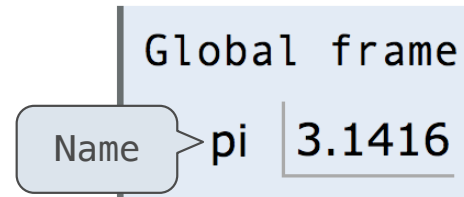
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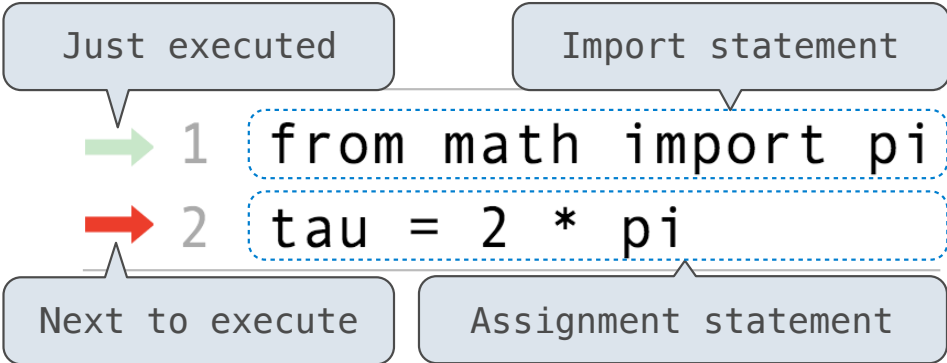
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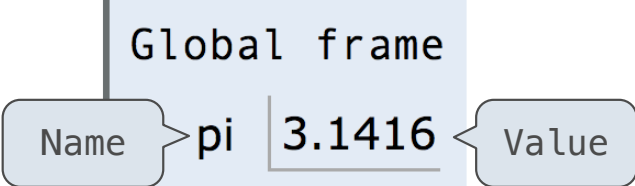
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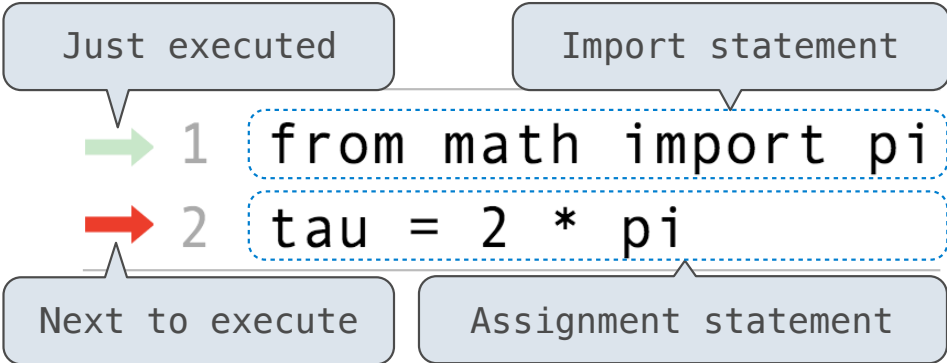


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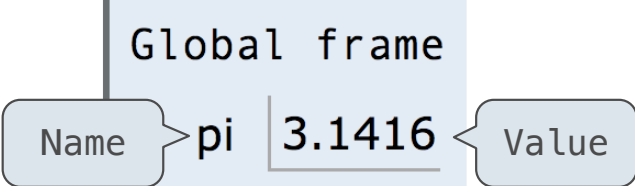
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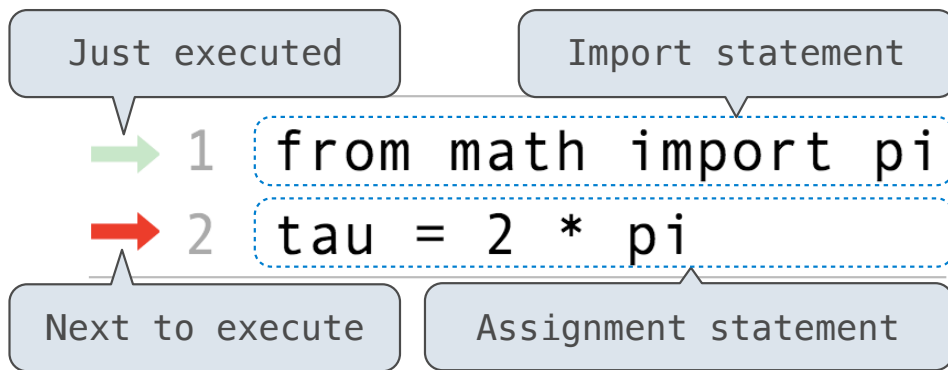
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Each name is bound to a value

Within a frame, a name cannot be repeated

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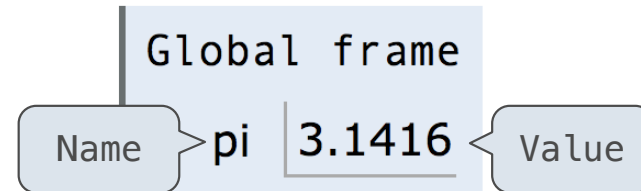
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(Demo)

[Interactive Diagram](#)

Assignment Statements

Interactive Diagram

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```
1 a = 1
→ 2 b = 2
→ 3 b, a = a + b, b
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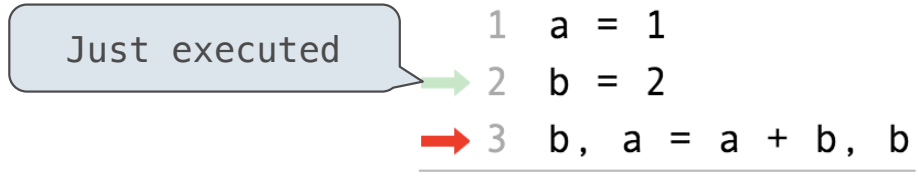
Global frame

a | 1

b | 2

Interactive Diagram

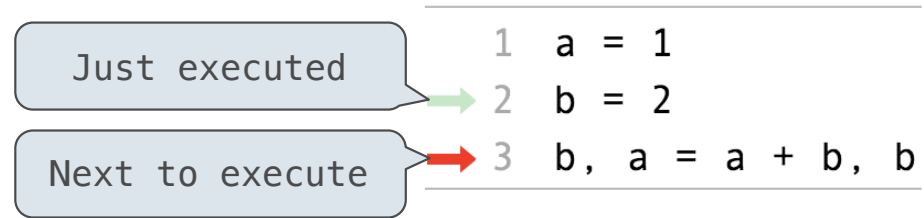
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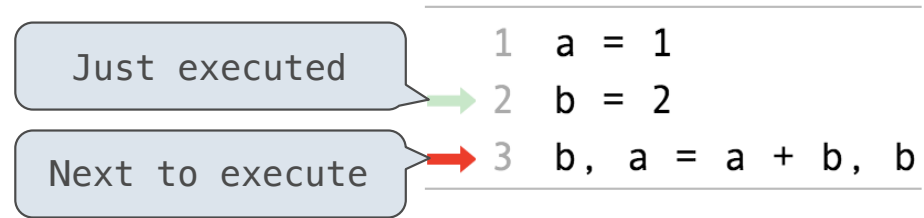


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Assignment Statements



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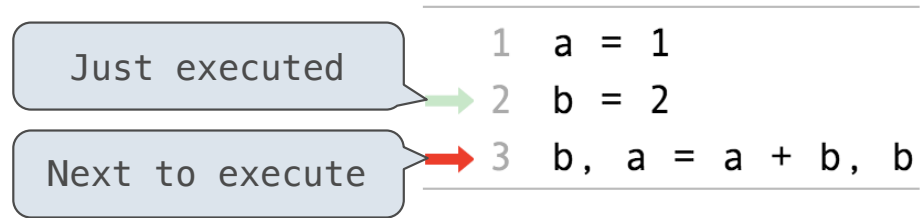
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Execution rule for assignment statements:

Interactive Diagram

Assignment Statements



Global frame

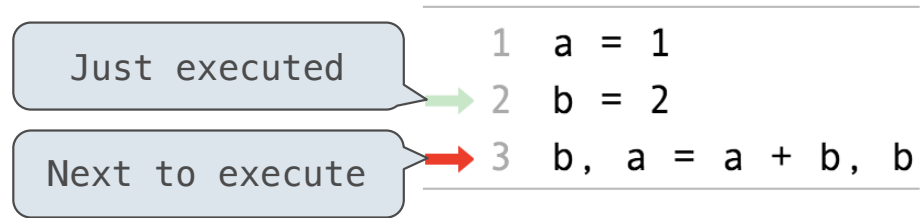
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Execution rule for assignment statements:

1. Evaluate all expressions to the right of = from left to right.

[Interactive Diagram](#)

Assignment Statements



Global frame

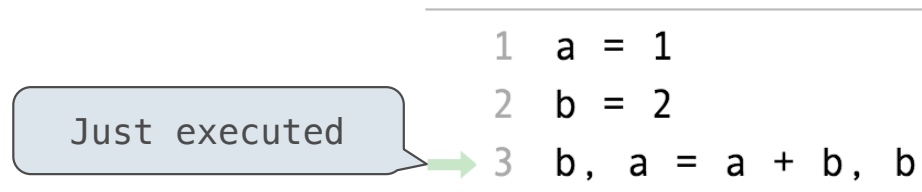
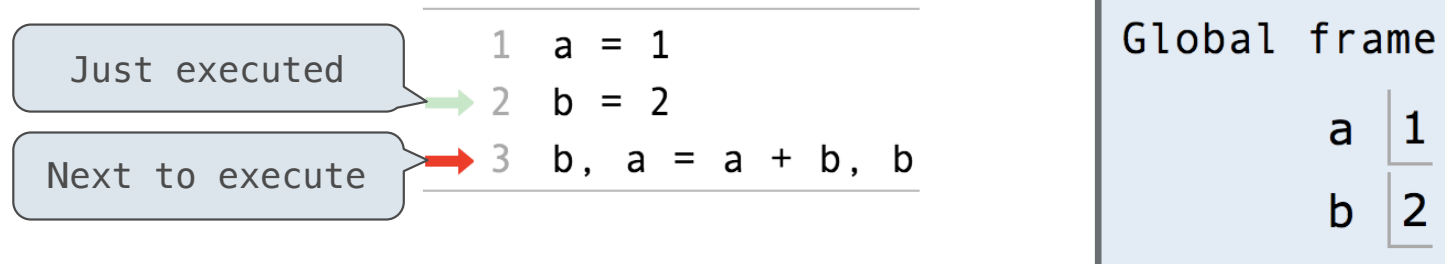
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[Interactive Diagram](#)

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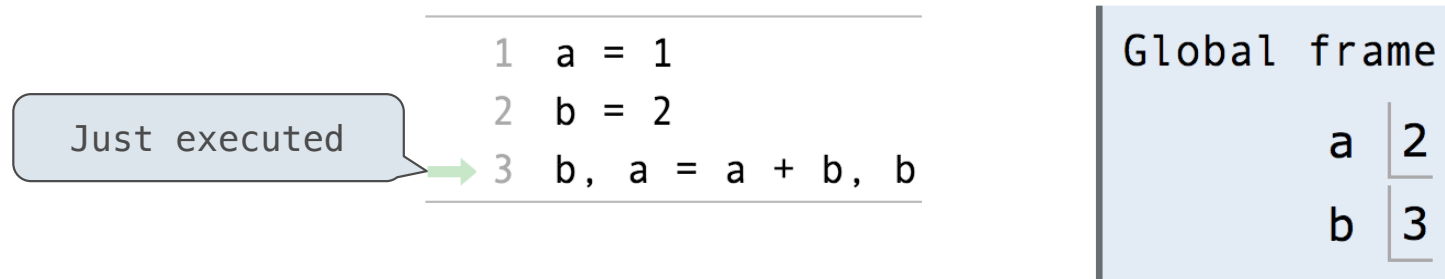
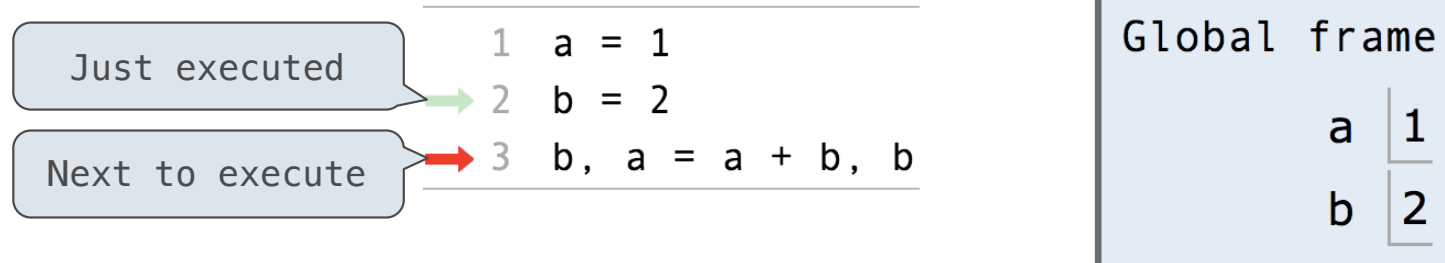


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Discussion Question 1 Solution

(Demo)

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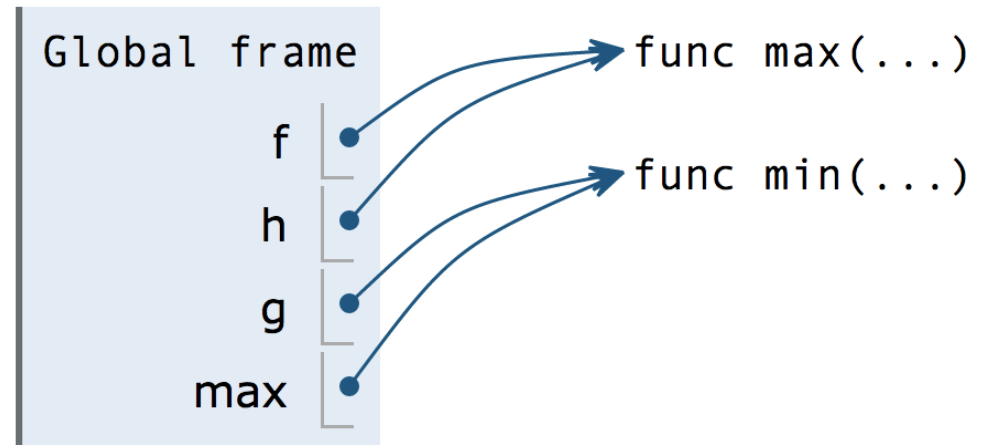
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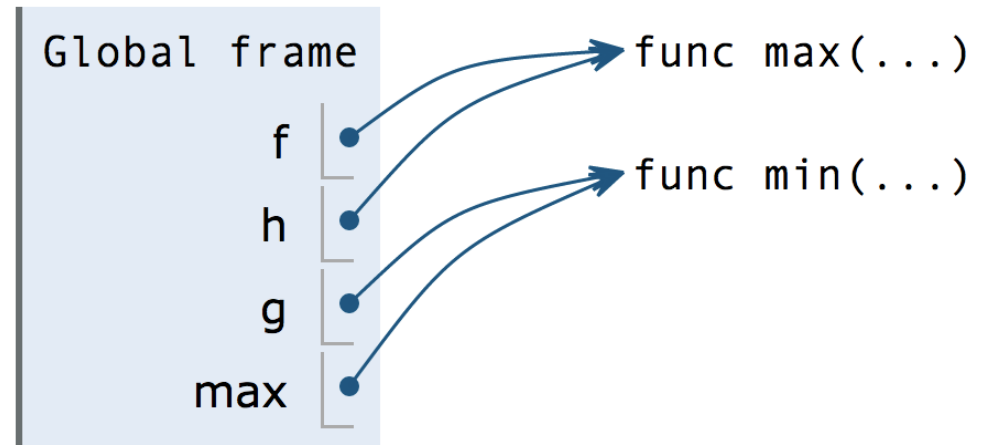


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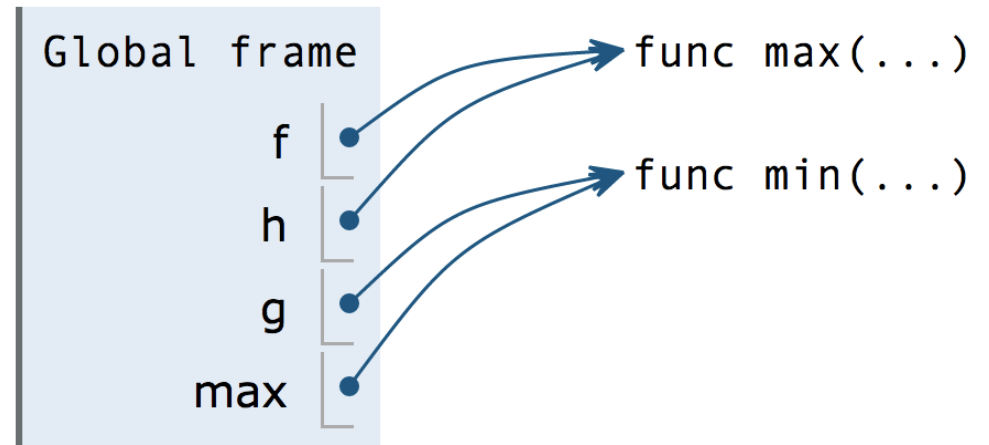
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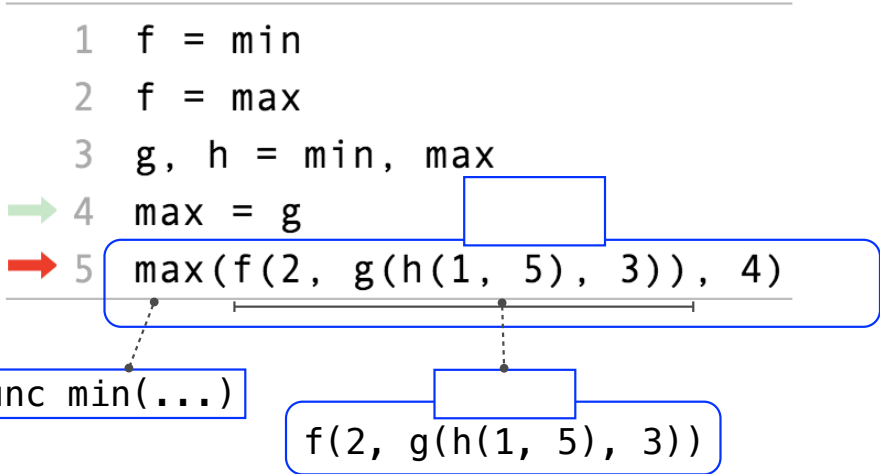
`func min(...)`

(Demo)

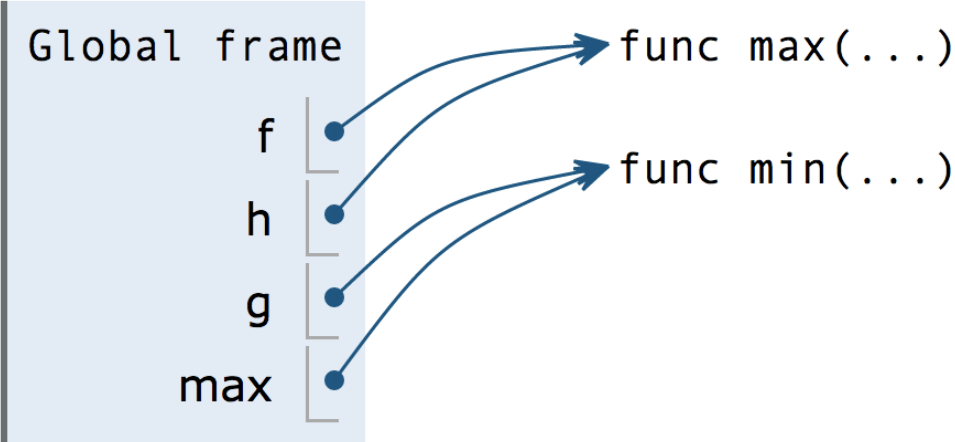


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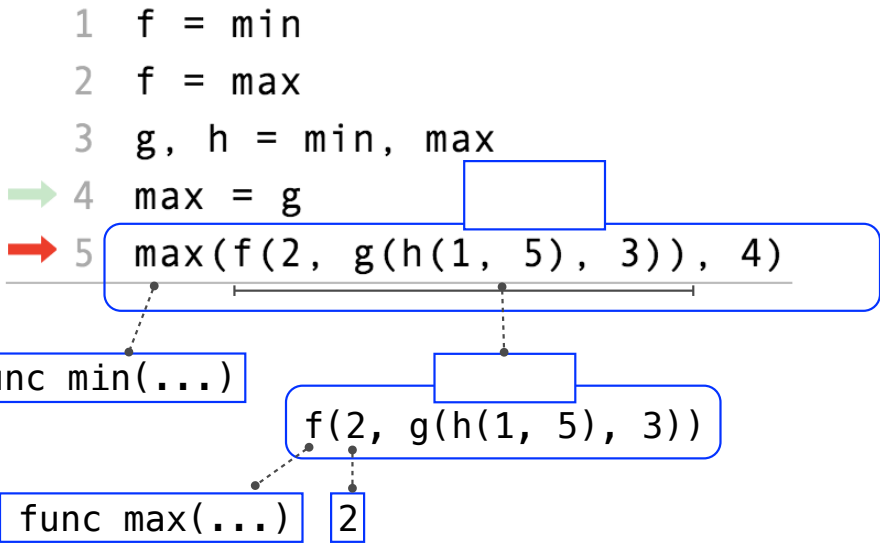
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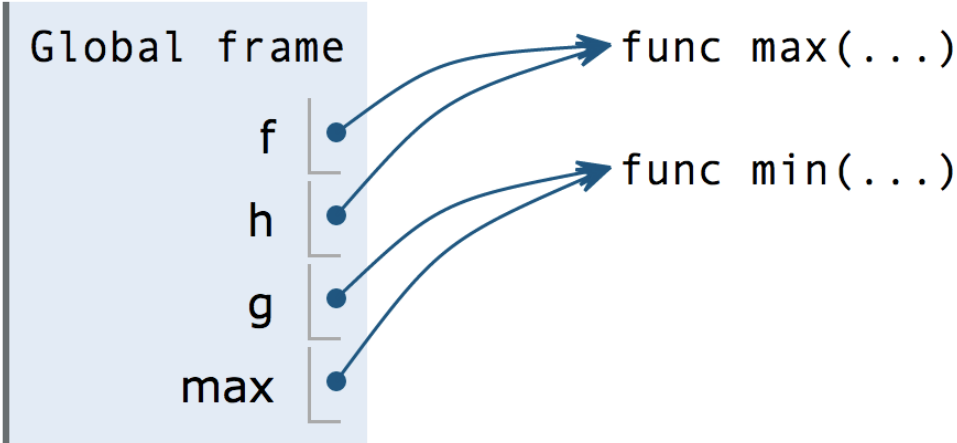
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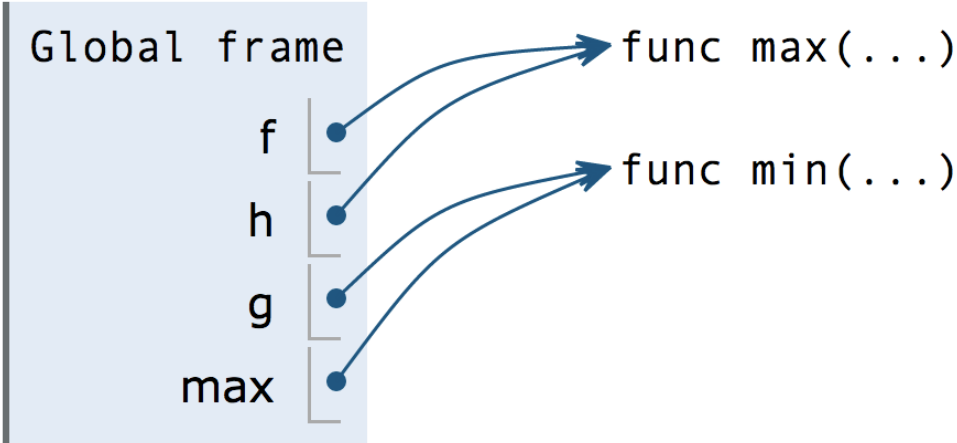
f(2, g(h(1, 5), 3))

func max(...)

2

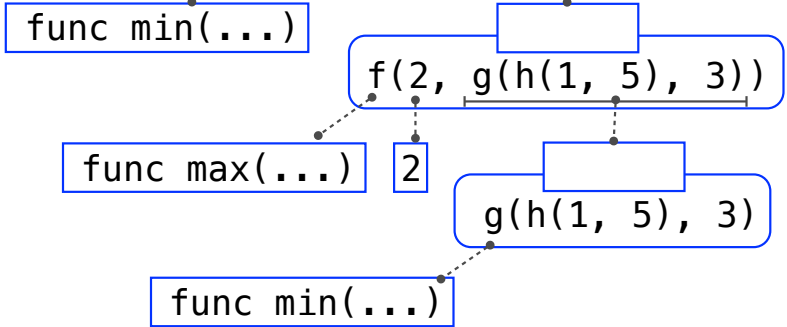
g(h(1, 5), 3)

(Demo)

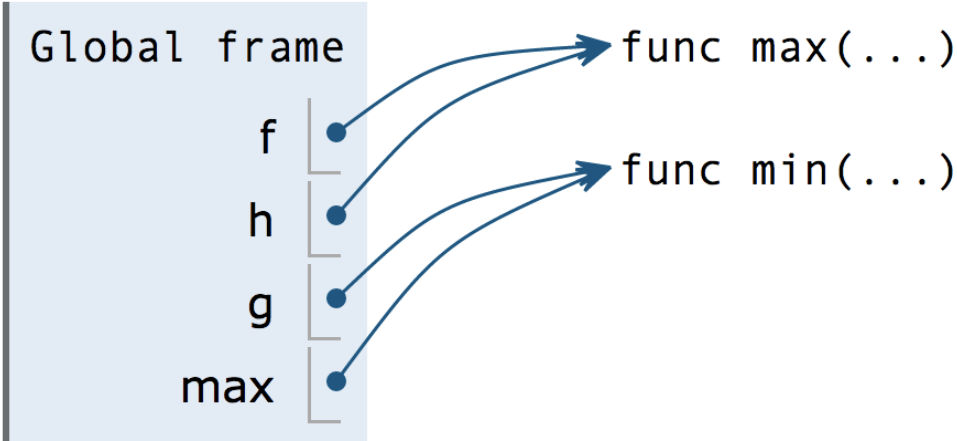


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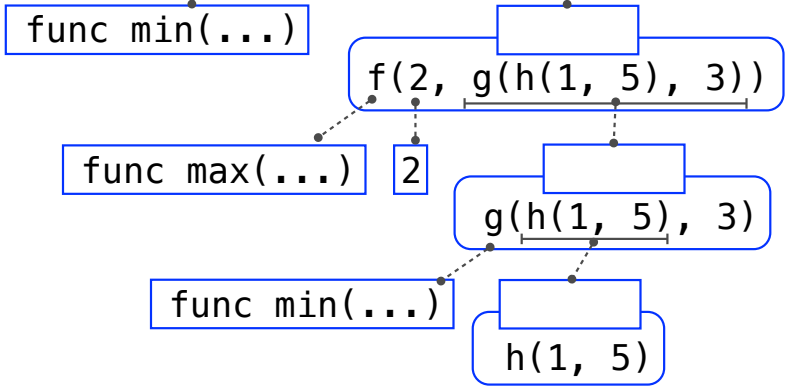


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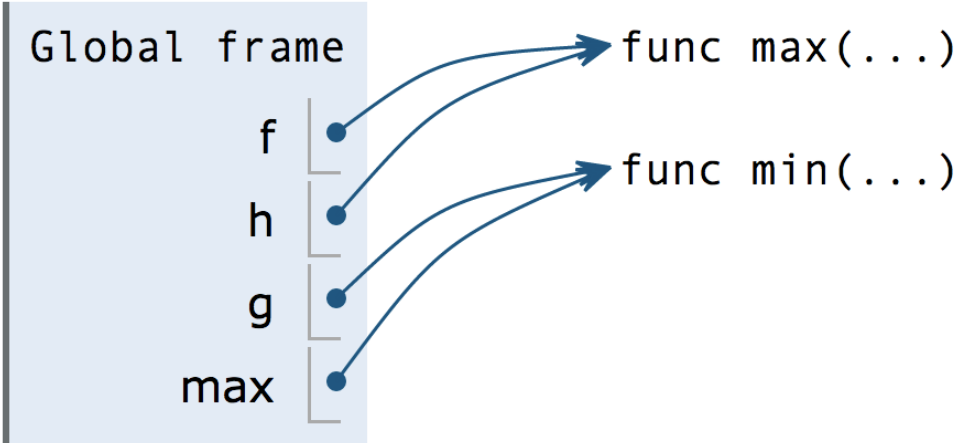


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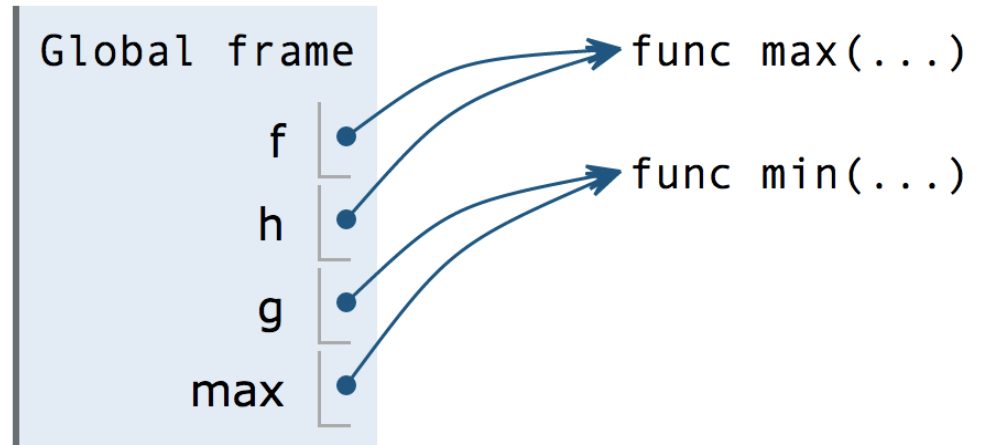
h(1, 5)

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5

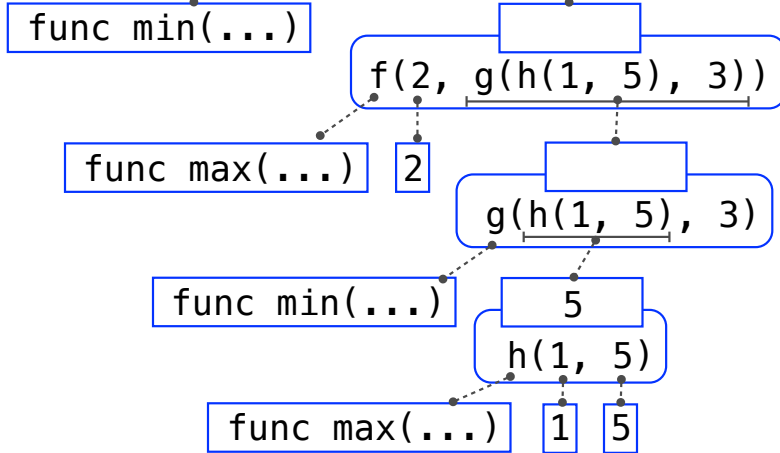
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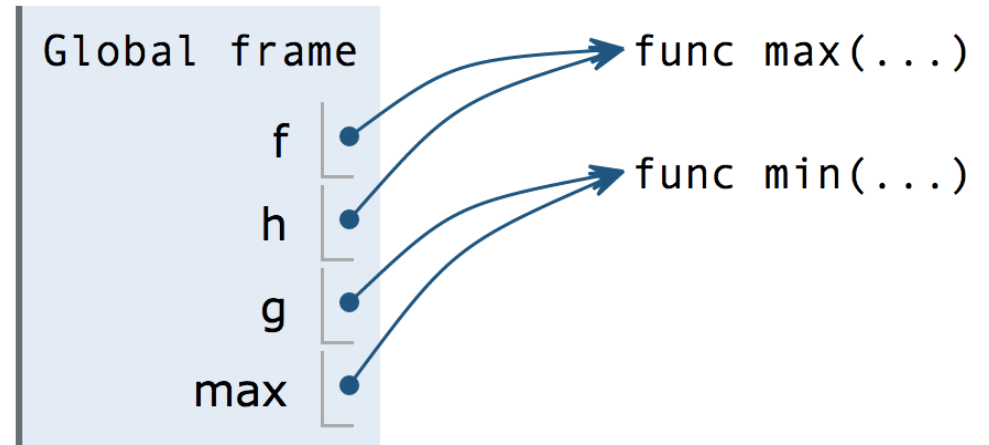
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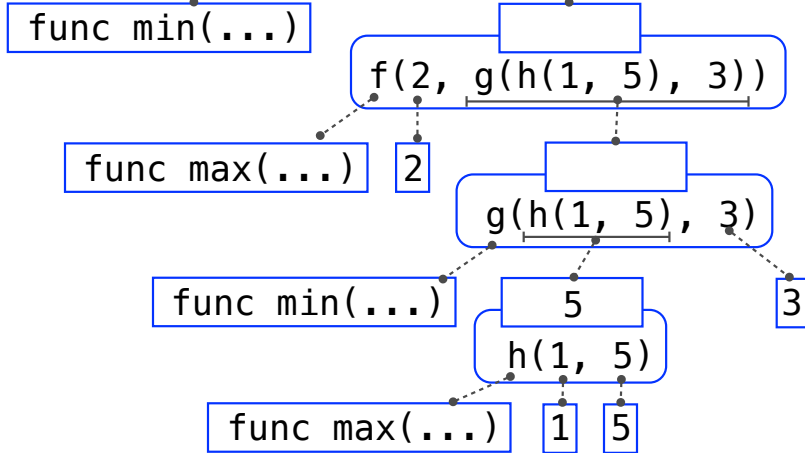
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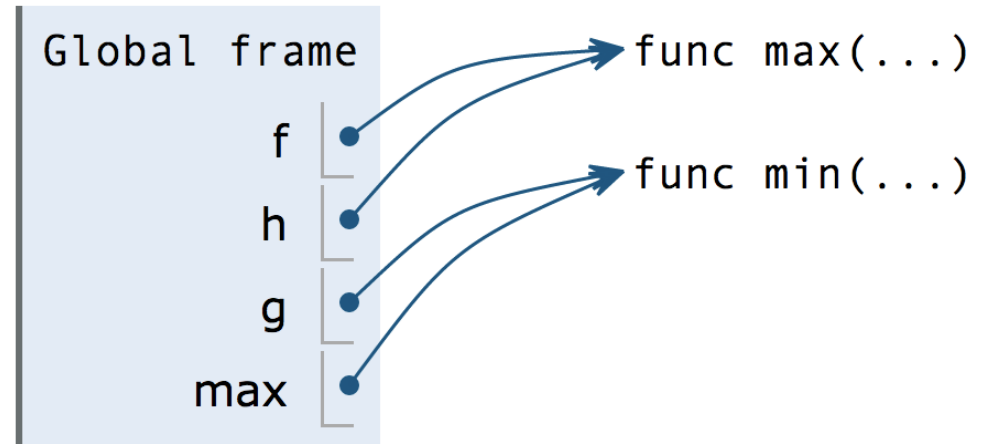
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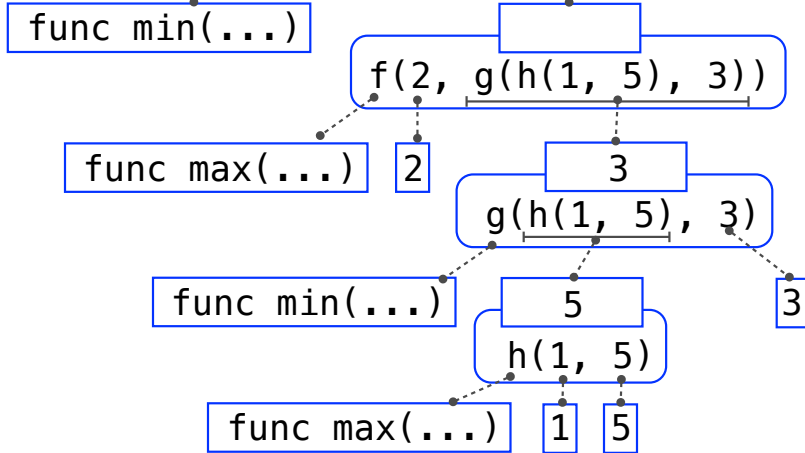
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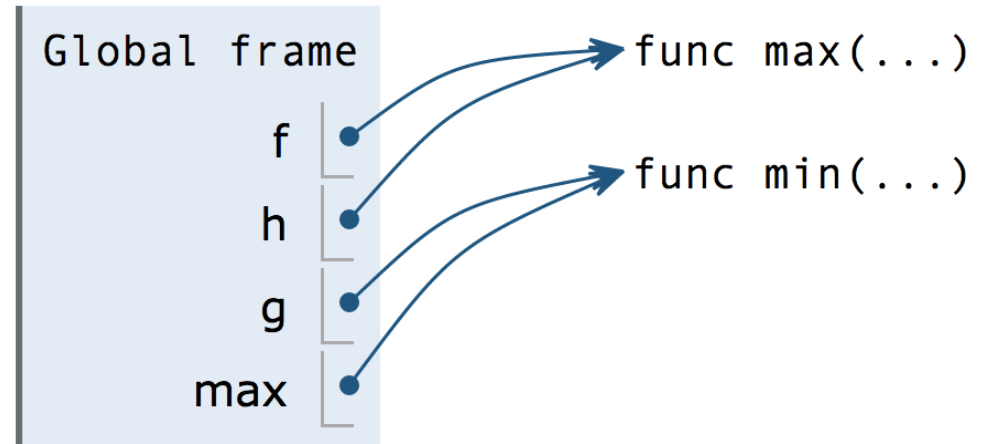
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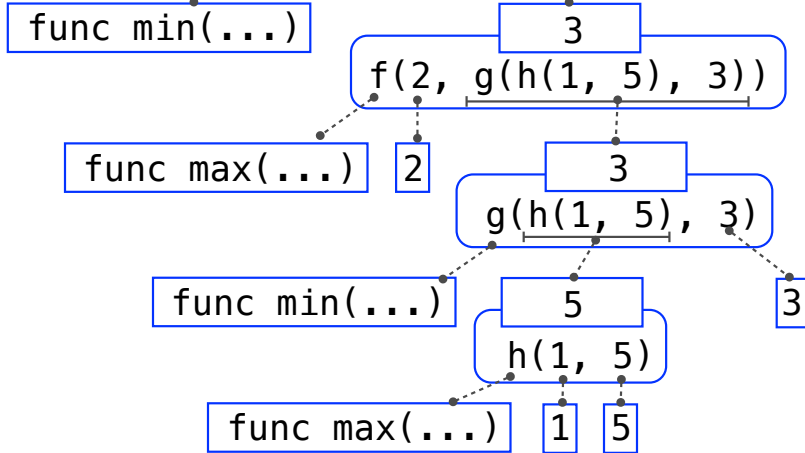
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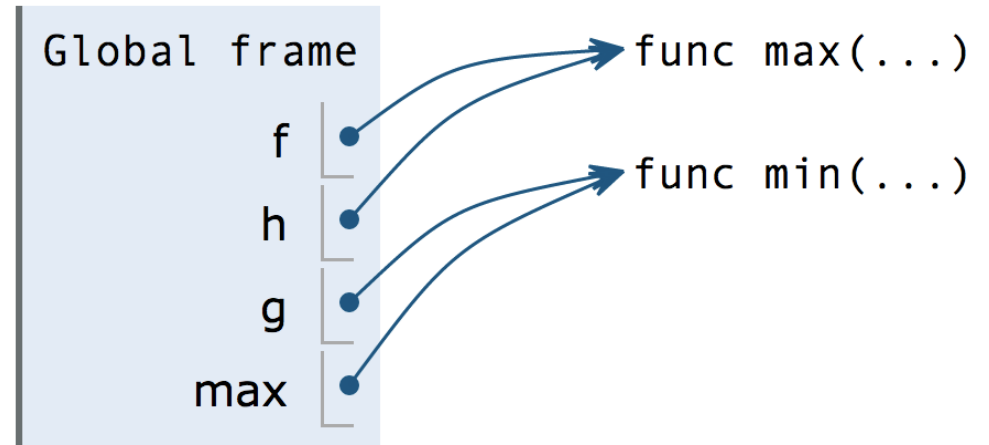
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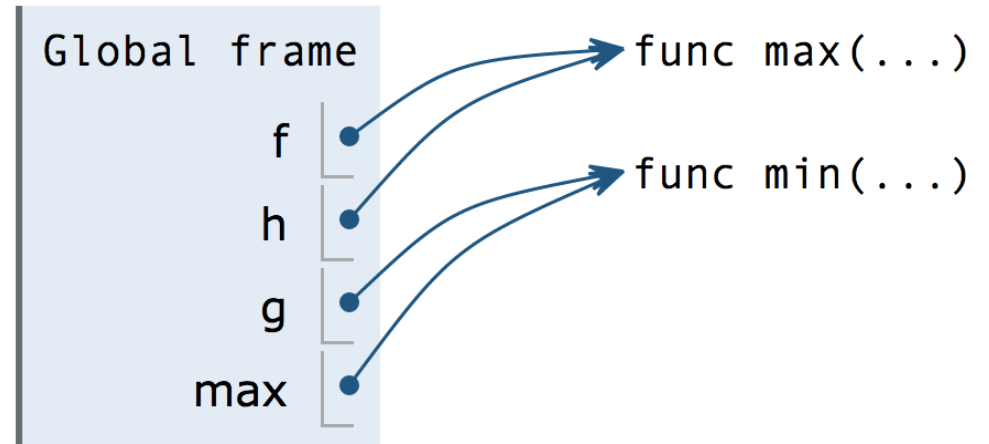
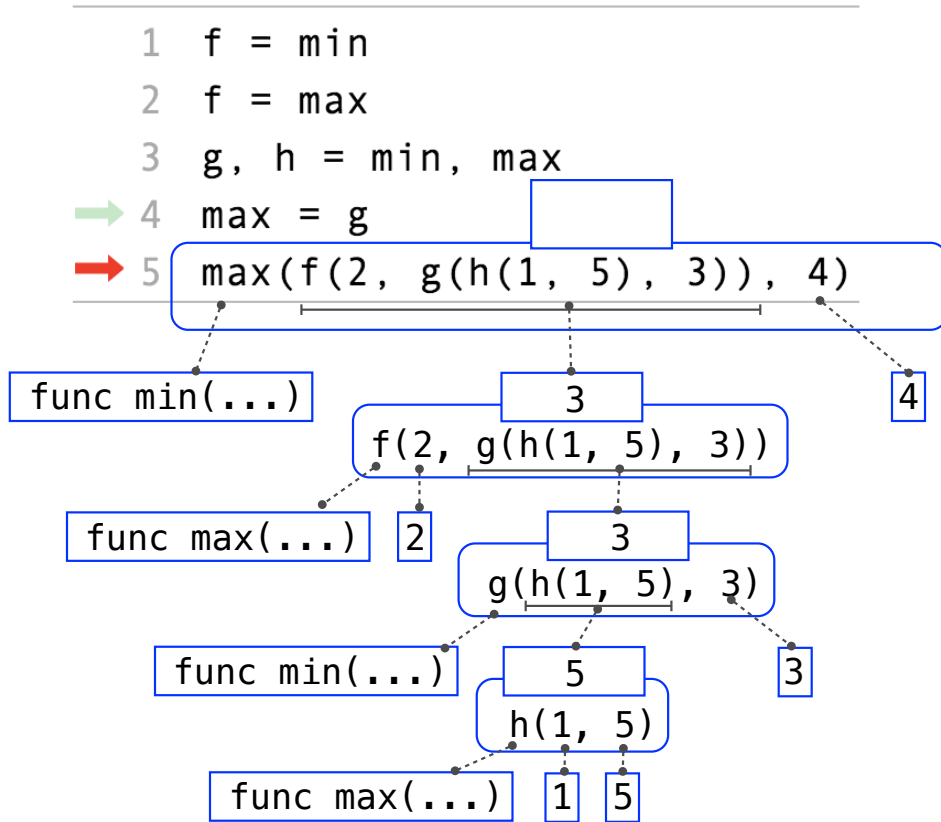
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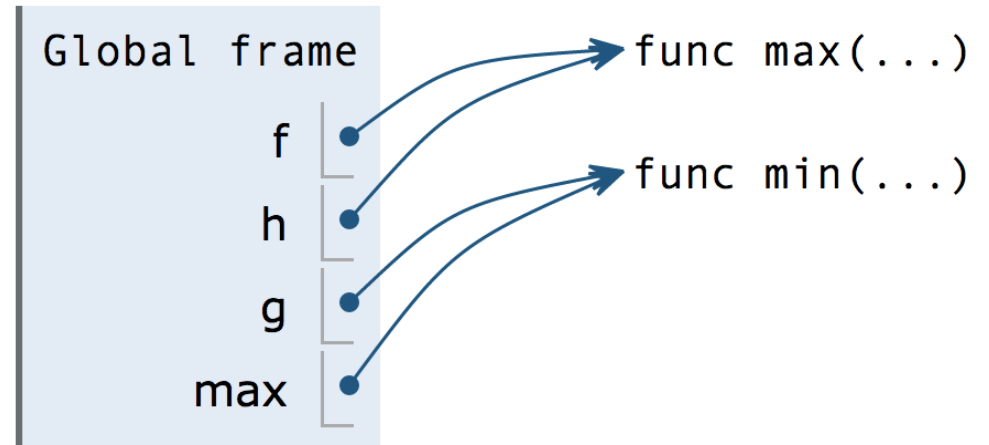
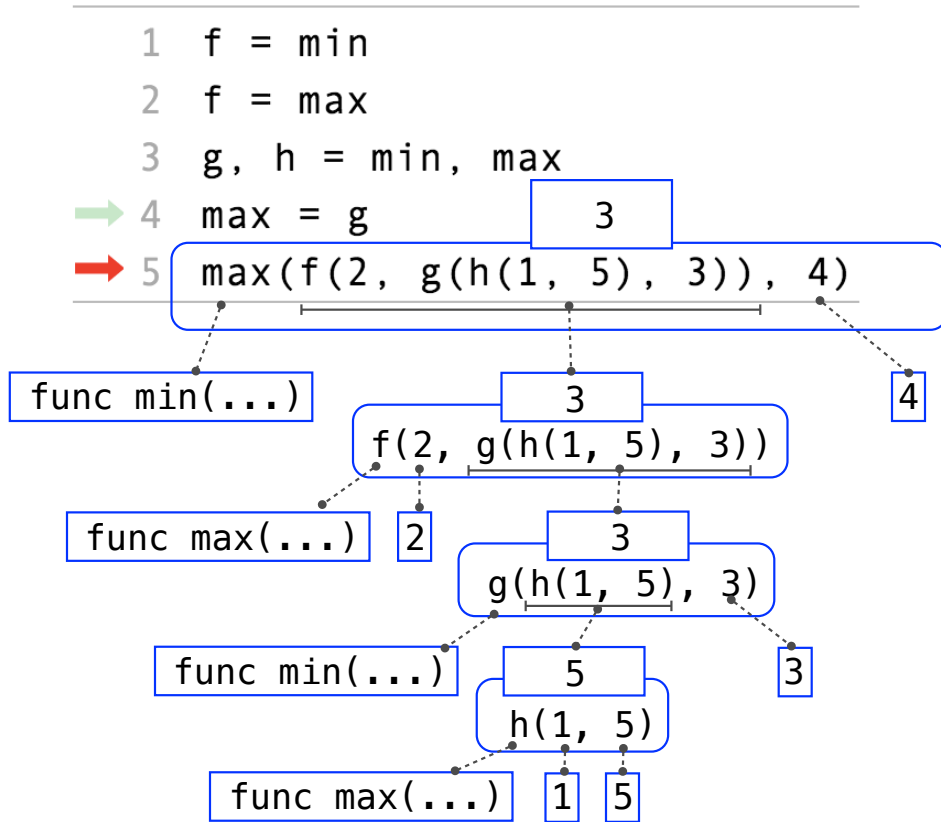
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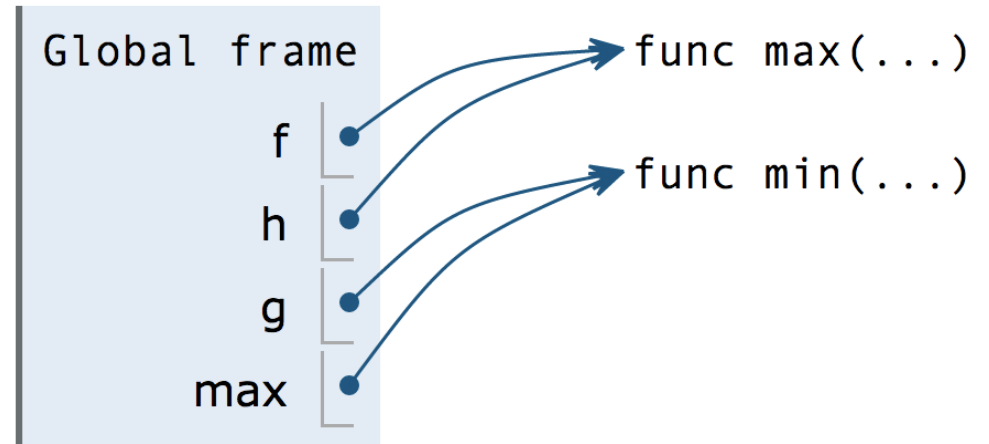
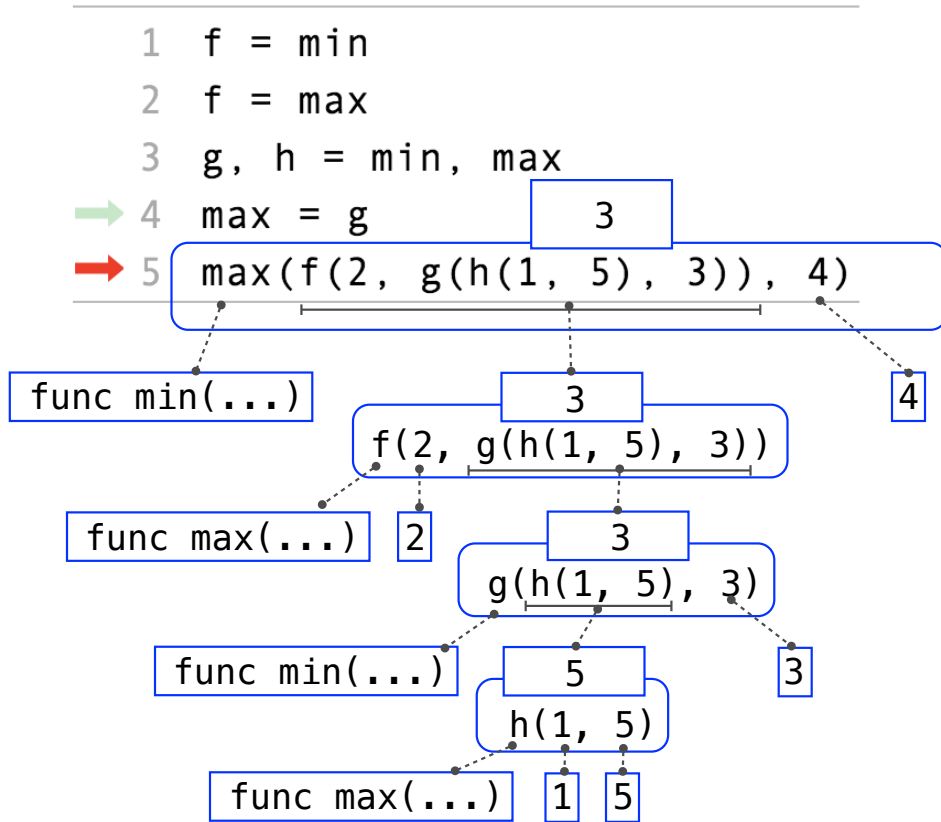
(Demo)



Interactive Diagram

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(Demo)



3

Interactive Diagram

Defining Functions

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Function definition is a more powerful means of abstraction: binds names to expressions

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Assignment is a simple means of abstraction: binds names to values

Function definition is a more powerful means of abstraction: binds names to expressions

Function *signature* indicates how many arguments a function takes

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Interactive Diagram

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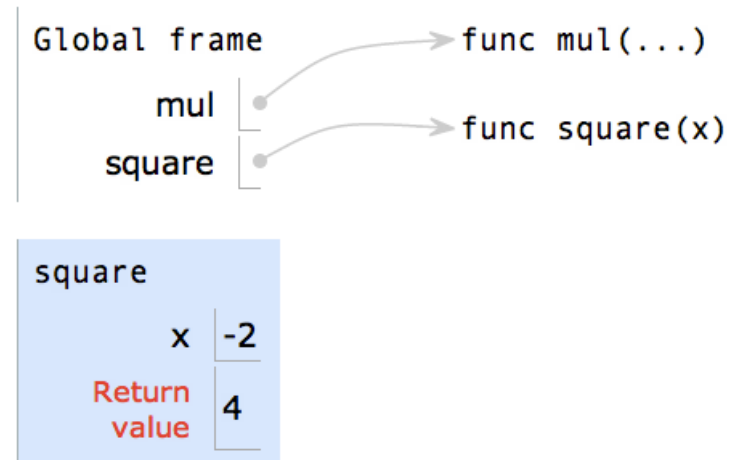
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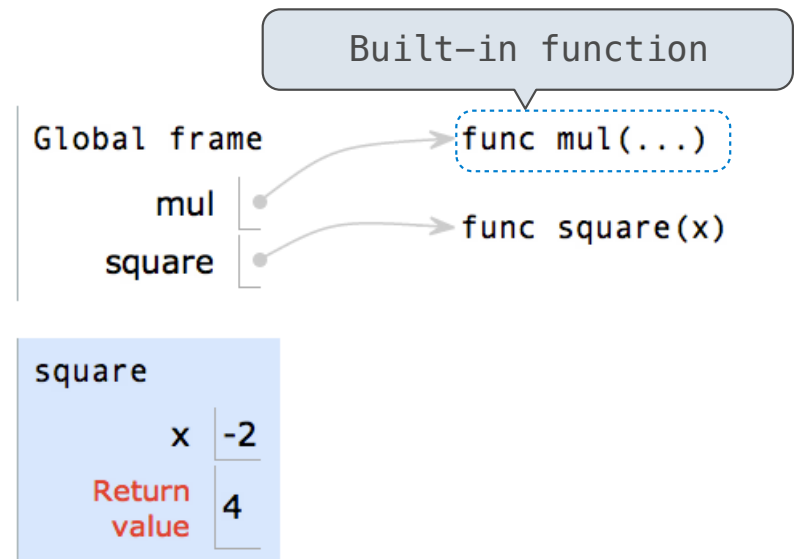
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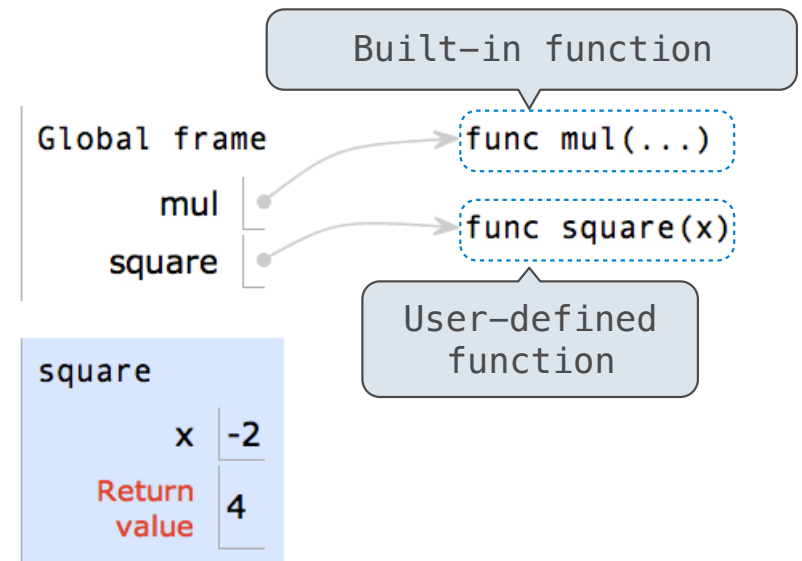
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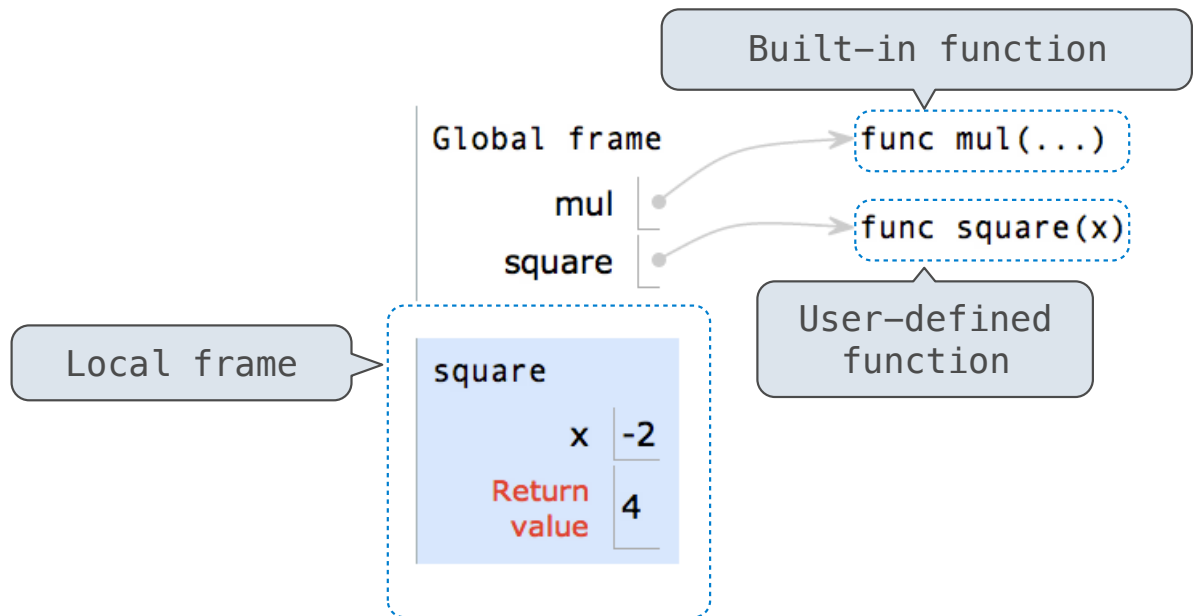
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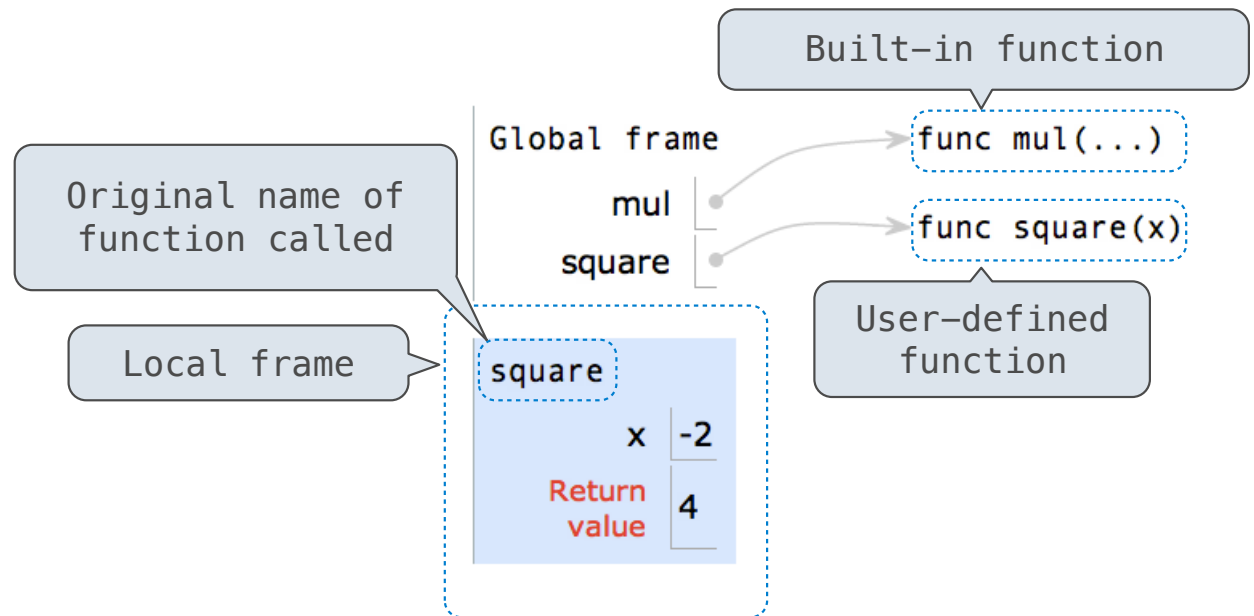
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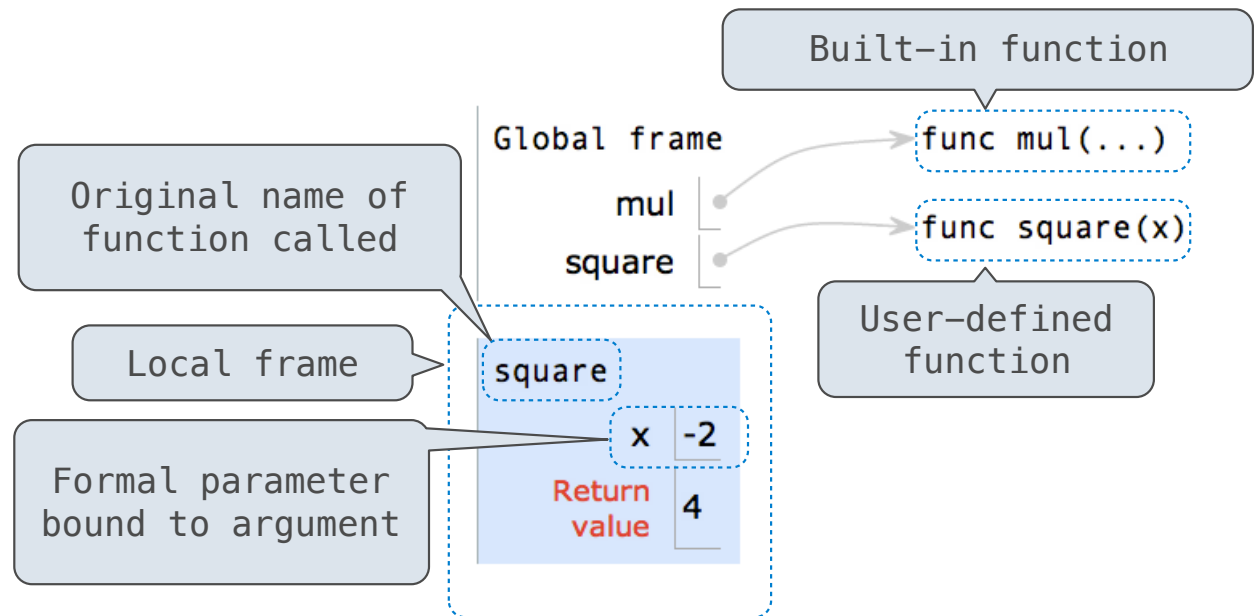
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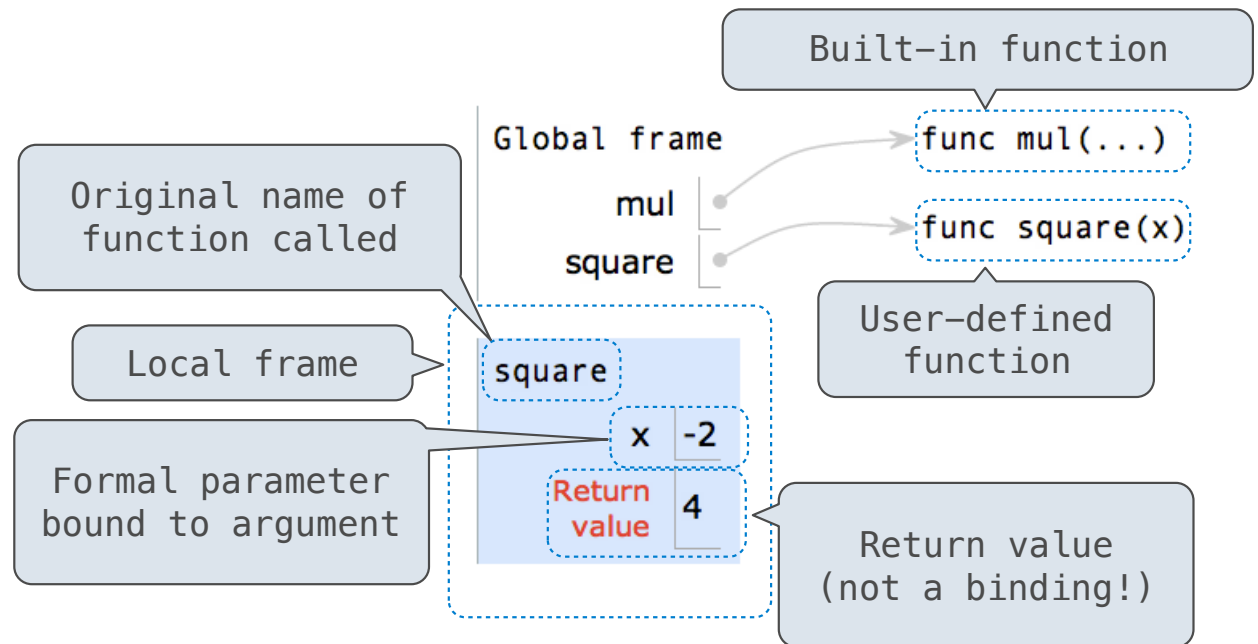
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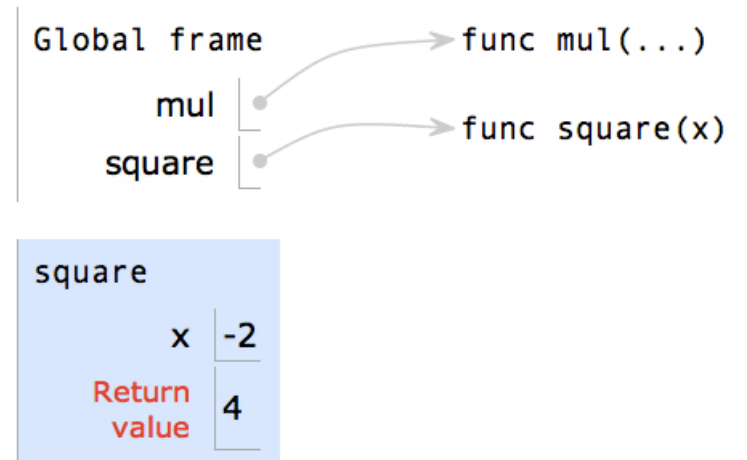
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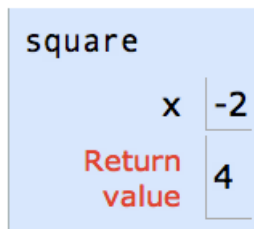
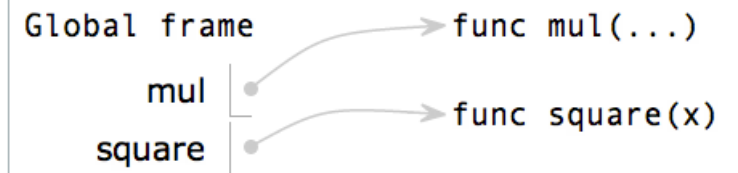
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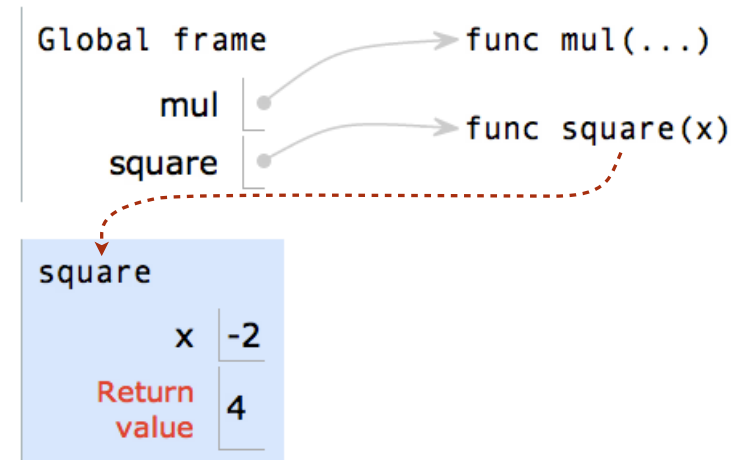
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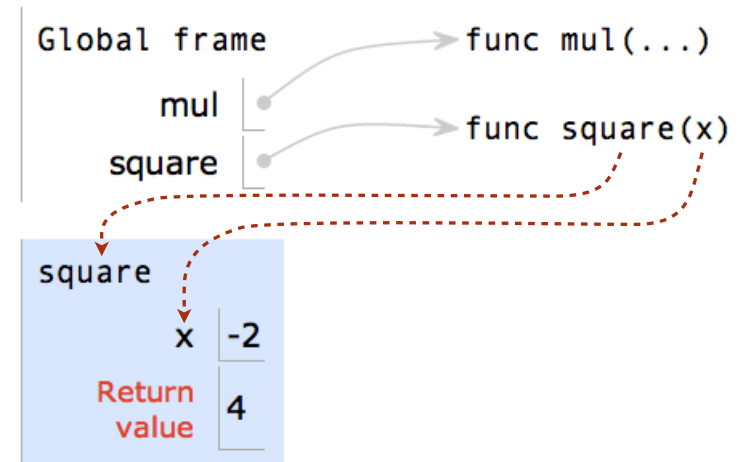
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(Demo)