CS 61A Lecture 11

Announcements

Dictionaries

{'Dem': 0}

Limitations on Dictionaries

Dictionaries are **unordered** collections of key-value pairs

Dictionary keys do have two restrictions:

• A key of a dictionary **cannot be** a list or a dictionary (or any *mutable type*)

• Two keys cannot be equal; There can be at most one value for a given key

This first restriction is tied to Python's underlying implementation of dictionaries

The second restriction is part of the dictionary abstraction

If you want to associate multiple values with a key, store them all in a sequence value

Box-and-Pointer Notation

The Closure Property of Data Types

- A method for combining data values satisfies the *closure property* if: The result of combination can itself be combined using the same method
- Closure is powerful because it permits us to create hierarchical structures
- Hierarchical structures are made up of parts, which themselves are made up of parts, and so on

Lists can contain lists as elements (in addition to anything else)

Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element Each box either contains a primitive value or points to a compound value



pair = [1, 2]

Interactive Diagram

Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element Each box either contains a primitive value or points to a compound value



Slicing

Slicing Creates New Values



Interactive Diagram

Processing Container Values

Sequence Aggregation

Several built-in functions take iterable arguments and aggregate them into a value

```
• sum(iterable[, start]) -> value
```

Return the sum of an iterable of numbers (NOT strings) plus the value of parameter 'start' (which defaults to 0). When the iterable is empty, return start.

```
• max(iterable[, key=func]) -> value
max(a, b, c, ...[, key=func]) -> value
```

With a single iterable argument, return its largest item. With two or more arguments, return the largest argument.

```
• all(iterable) -> bool
```

Return True if bool(x) is True for all values x in the iterable. If the iterable is empty, return True.

Trees

Tree Abstraction



Recursive description (wooden trees): A tree has a root value and a list of branches Each branch is a tree A tree with zero branches is called a leaf

Relative description (family trees):
Each location in a tree is called a node
Each node has a value
One node can be the parent/child of another

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People often refer to values by their locations: "each parent is the sum of its children"

Implementing the Tree Abstraction

```
def tree(root, branches=[]):
    return [root] + branches

def root(tree):
    return tree[0]

def branches(tree):
    return tree[1:]
```



Implementing the Tree Abstraction



Tree Processing

Tree Processing Uses Recursion

```
Processing a leaf is often the base case of a tree processing function
The recursive case typically makes a recursive call on each branch, then aggregates
```

```
def count_leaves(t):
    """Count the leaves of a tree."""
    if is_leaf(t):
        return 1
    else:
        branch_counts = [count_leaves(b) for b in branches(t)]
        return sum(branch_counts)
```

Discussion Question

Implement leaves, which returns a list of the leaf values of a tree

Hint: If you sum a list of lists, you get a list containing the elements of those lists

```
>>> sum([ [1], [2, 3], [4] ], [])
                                      def leaves(tree):
[1, 2, 3, 4]
                                          """Return a list containing the leaves of tree.
>>> sum([ [1] ], [])
                                          >>> leaves(fib tree(5))
[1]
>>> sum([ [[1]], [2] ], [])
                                          [1, 0, 1, 0, 1, 1, 0, 1]
                                          IIII II
[[1], 2]
                                          if is leaf(tree):
                                              return [root(tree)]
                                          else:
                                              return sum(List of leaves for each branch, []))
     branches(tree)
                                                 [b for b in branches(tree)]
     leaves(tree)
                                                 [s for s in leaves(tree)]
     [branches(b) for b in branches(tree)]
                                                 [branches(s) for s in leaves(tree)]
     [leaves(b) for b in branches(tree)]
                                                 [leaves(s) for s in leaves(tree)]
```

Creating Trees

A function that creates a tree from another tree is typically also recursive

```
def increment_leaves(t):
    """Return a tree like t but with leaf values incremented."""
    if is_leaf(t):
        return tree(root(t) + 1)
    else:
        bs = [increment_leaves(b) for b in branches(t)]
        return tree(root(t), bs)

def increment(t):
    """Return a tree like t but with all node values incremented."""
    return tree(root(t) + 1, [increment(b) for b in branches(t)])
```

Example: Printing Trees