



#### Sets

One more built-in Python container type

- Set literals are enclosed in braces
- Duplicate elements are removed on construction
- Sets have arbitrary order, just like dictionary entries

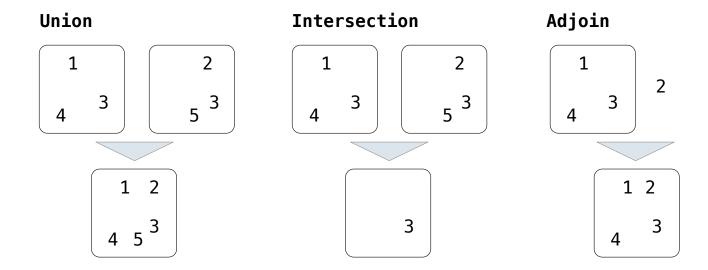
```
>>> s = {3, 2, 1, 4, 4}
>>> s
{1, 2, 3, 4}
>>> 3 in s
True
>>> len(s)
4
>>> s.union({1, 5})
{1, 2, 3, 4, 5}
>>> s.intersection({6, 5, 4, 3})
{3, 4}
>>> s
{1, 2, 3, 4}

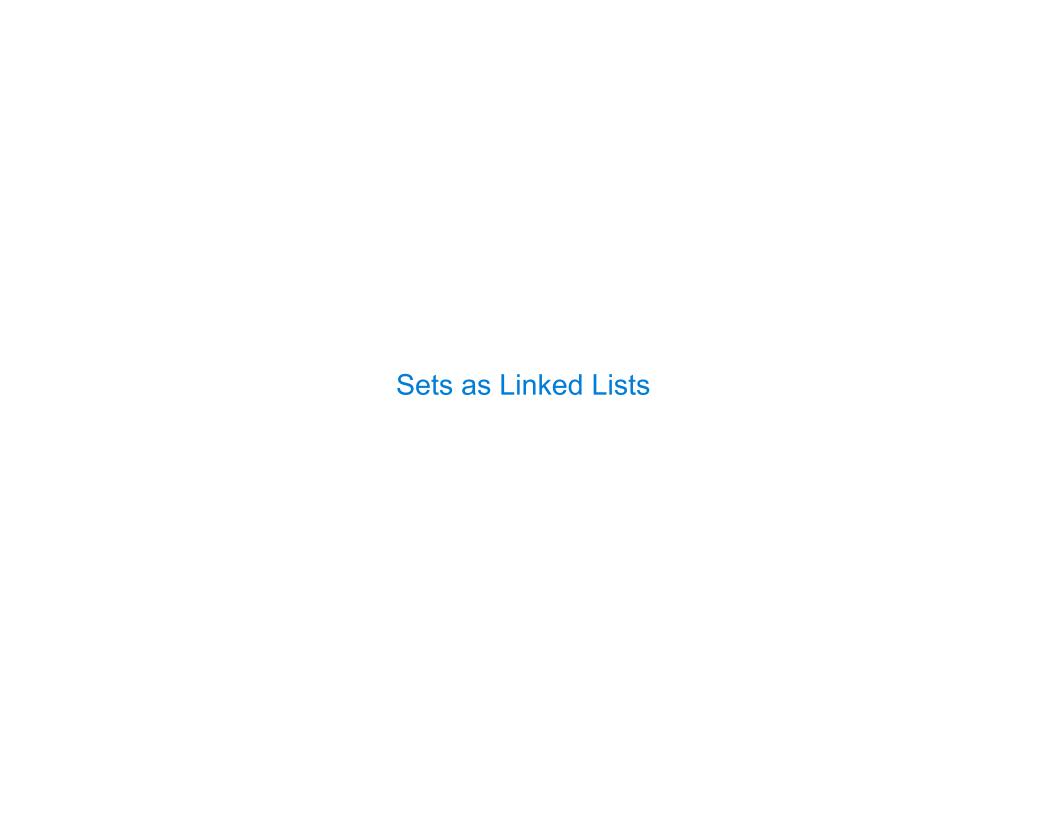
(Demo)
```

## Implementing Sets

What we should be able to do with a set:

- Membership testing: Is a value an element of a set?
- Union: Return a set with all elements in set1 or set2
- Intersection: Return a set with any elements in set1 and set2
- Adjoin: Return a set with all elements in s and a value v





### Sets as Unordered Sequences

Proposal 1: A set is represented by a linked list that contains no duplicate items.

#### Time order of growth

 $\Theta(1)$ 

Time depends on whether & where v appears in s

 $\Theta(n)$ 

Assuming v either does not appear in s

or

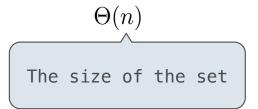
appears in a uniformly distributed random location

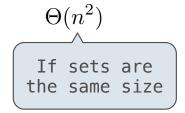
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## Sets as Unordered Sequences

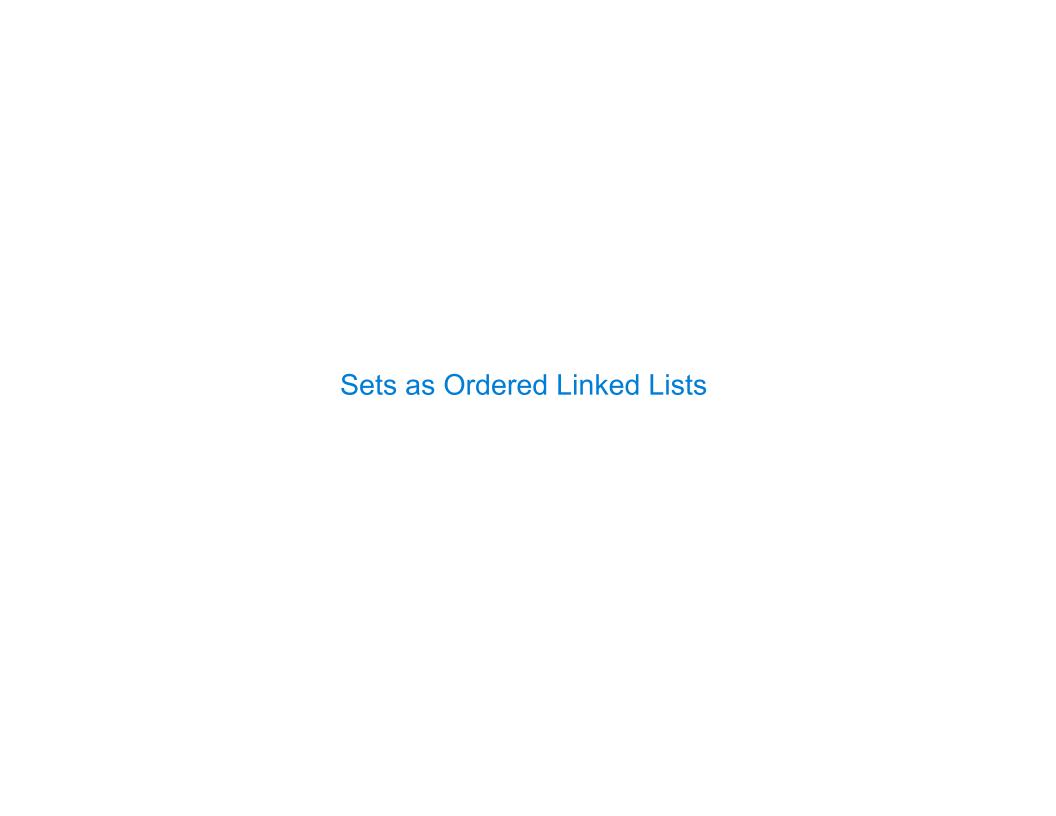
```
def adjoin(s, v):
    if contains(s, v):
        return s
    else:
        return Link(v, s)
def intersect(set1, set2):
    in set2 = lambda v: contains(set2, v)
    return filter_link(in_set2, set1)
        Return elements x for which
      in set2(x) returns a true value
def union(set1, set2):
    not in set2 = lambda v: not contains(set2, v)
    set1 not set2 = filter link(not in set2, set1)
    return extend link(set1 not set2, set2)
       Return a linked list containing all elements in
        set1 not set2 followed by all elements in set2
```

#### Time order of growth





$$\Theta(n^2)$$

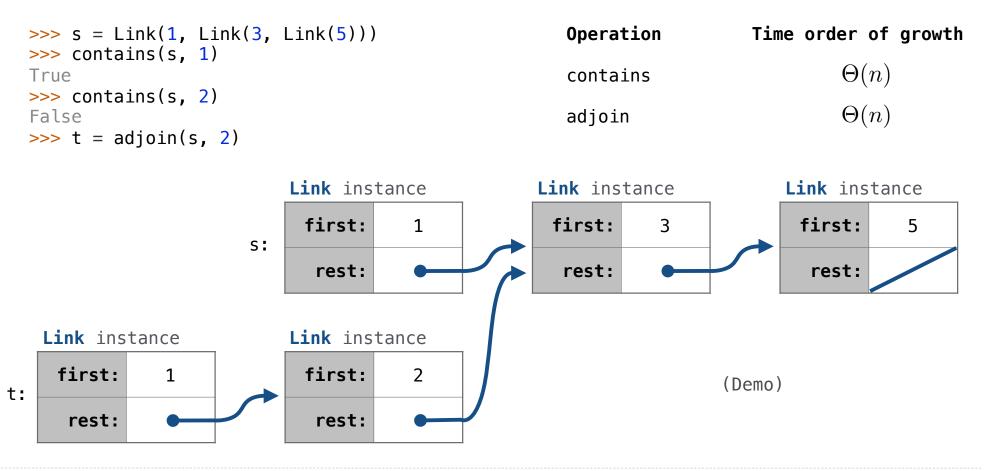


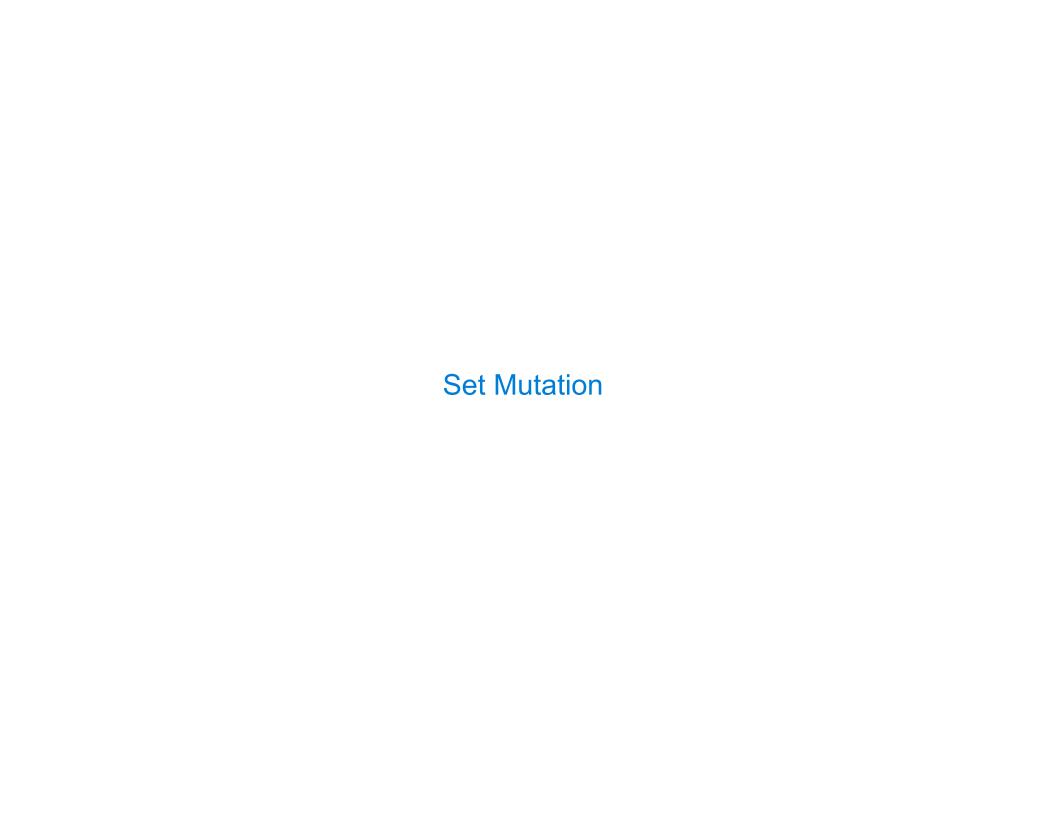
# Sets as Ordered Sequences

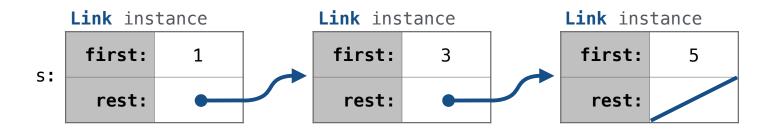
Parts of the program that	Assume that sets are	Using
Use sets to contain values	Unordered collections	empty, contains, adjoin, intersect, union
Implement set operations	Ordered linked lists	first, rest, <, >, ==

Different parts of a program may make different assumptions about data

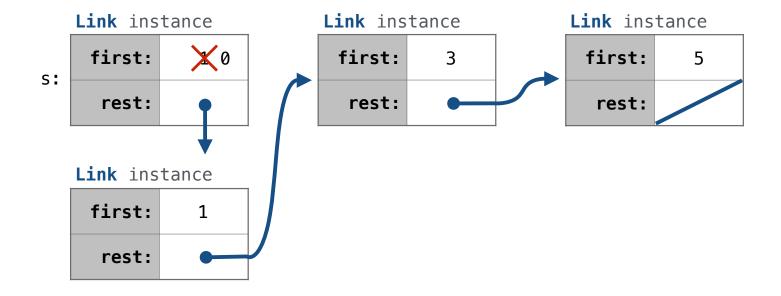
#### Searching an Ordered List





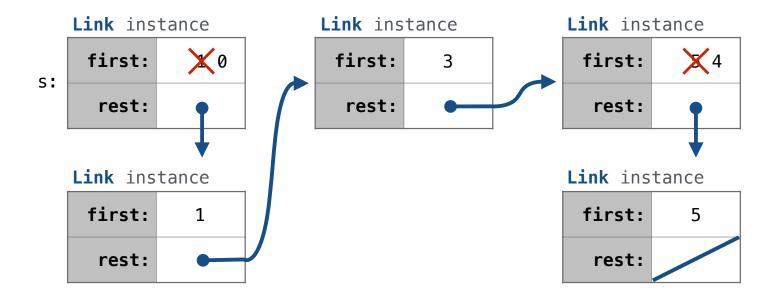


add(s, 0)

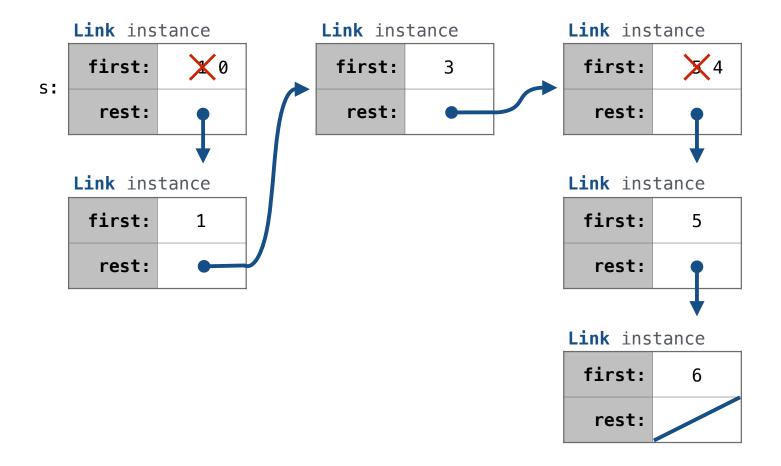


add(s, 3)

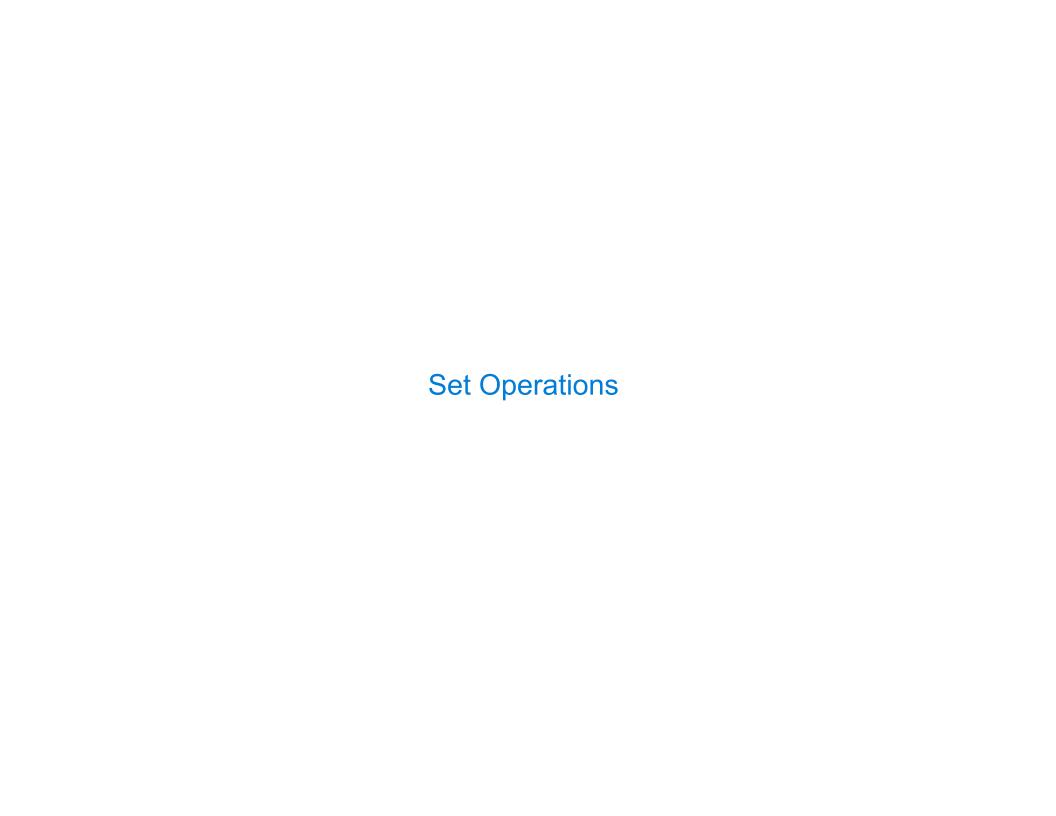
add(s, 4)



add(s, 6)



```
def add(s, v):
                                                            Link instance
                                                                            Link instance
                                                                                            Link instance
    """Add v to a set s and return s.
                                                             first:
                                                                             first:
                                                                                             first:
                                                         s:
    >>> s = Link(1, Link(3, Link(5)))
                                                                              rest:
                                                                                              rest:
                                                              rest:
    >>> add(s, 0)
    Link(0, Link(1, Link(3, Link(5))))
                                                            Link instance
                                                                                            Link instance
    >>> add(s, 3)
                                                             first:
                                                                    1
                                                                                             first:
    Link(0, Link(1, Link(3, Link(5))))
                                                              rest:
                                                                                              rest:
    >>> add(s, 4)
    Link(0, Link(1, Link(3, Link(4, Link(5)))))
                                                                                            Link instance
    >>> add(s, 6)
                                                                                             first:
    Link(0, Link(1, Link(3, Link(4, Link(5, Link(6)))))
                                                                                              rest:
    assert not empty(s), "Cannot add to an empty set."
    if s.first > v:
                                                                   Link(s.first, s.rest)
         s.first, s.rest =
    elif s.first < v and empty(s.rest):</pre>
                                                    Link(v, s.rest)
         s_rest =
    elif s.first < v:
                                                    add(s.rest, v)
    return s
```



### **Intersecting Ordered Linked Lists**

Proposal 2: A set is represented by a linked list with unique elements that is
ordered from least to greatest

```
def intersect(set1, set2):
    if empty(set1) or empty(set2):
        return Link.empty
    else:
        e1, e2 = set1.first, set2.first
        if e1 == e2:
            return Link(e1, intersect(set1.rest, set2.rest))
        elif e1 < e2:
            return intersect(set1.rest, set2)
        elif e2 < e1:
            return intersect(set1, set2.rest)

Order of growth? \Theta(n) (Demo)
```