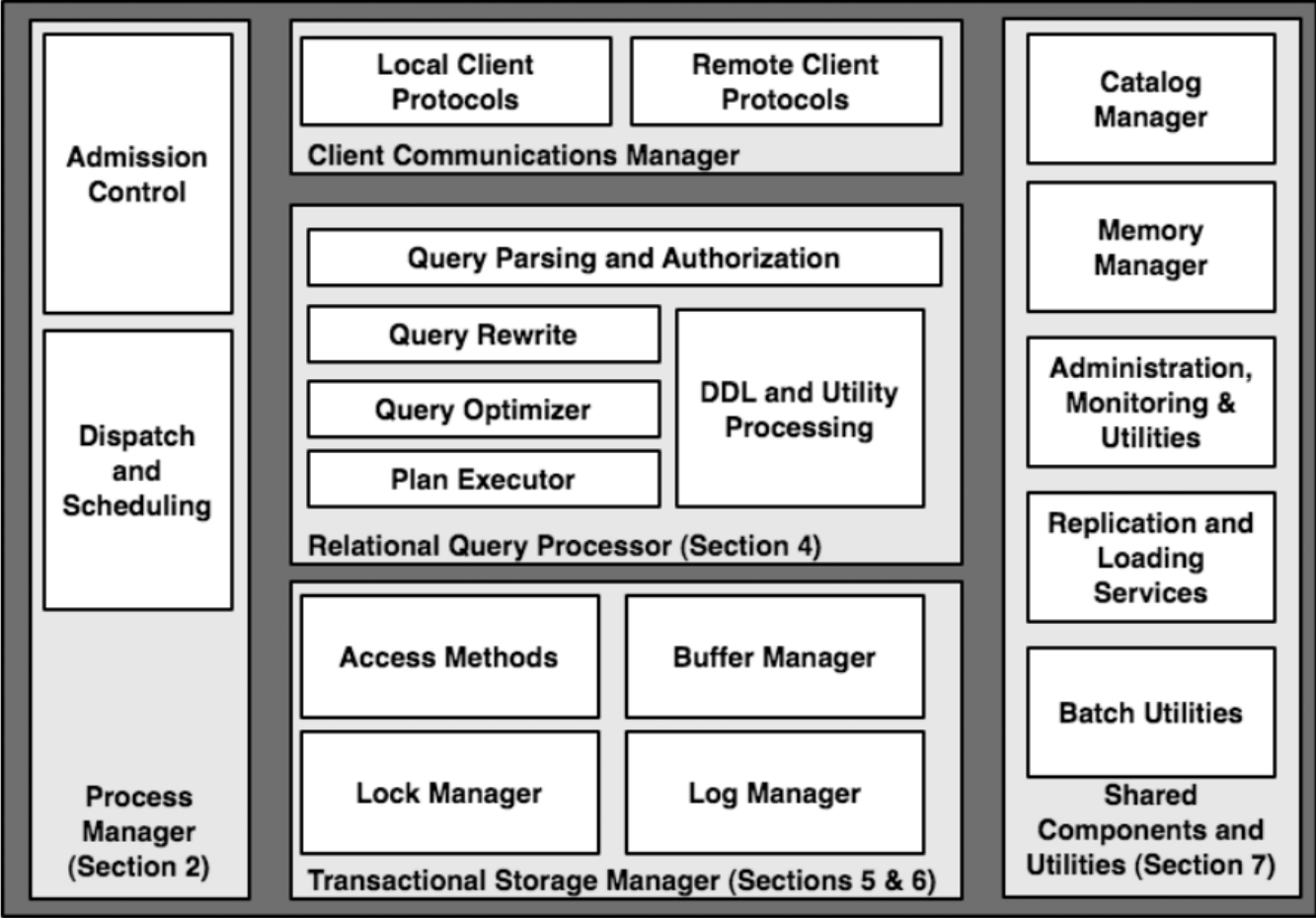


61A Lecture 33

Announcements

Database Management Systems

Database Management System Architecture



Architecture of a Database System by Hellerstein, Stonebreaker, and Hamilton

Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Select the parents of curly-furred dogs:

```
select parent from parents, dogs
      where child = name and fur = "curly";
```

Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Select the parents of curly-furred dogs:

```
select parent from {parents, dogs}
                    where child = name and fur = "curly";
```

Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Select the parents of curly-furred dogs:

```
select parent from {parents, dogs}
                  {child = name} and fur = "curly";
```


Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Select the parents of curly-furred dogs:

```
select parent from parents, dogs
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Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Select the parents of curly-furred dogs:

```
select parent from parents, dogs
where child = name and fur = "curly";
```

Join all rows of parents to all rows of dogs, filter by `child = name` and `fur = "curly"`

Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Select the parents of curly-furred dogs:

```
select parent from parents, dogs
where child = name and fur = "curly";
```

Join all rows of parents to all rows of dogs, filter by `child = name` and `fur = "curly"`

Join only rows of parents and dogs where `child = name`, filter by `fur = "curly"`

Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Select the parents of curly-furred dogs:

```
select parent from parents, dogs
where child = name and fur = "curly";
```

Join all rows of parents to all rows of dogs, filter by `child = name` and `fur = "curly"`

Join only rows of parents and dogs where `child = name`, filter by `fur = "curly"`

Filter dogs by `fur = "curly"`, join result with all rows of parents, filter by `child = name`

Query Planning

The manner in which tables are filtered, sorted, and joined affects execution time

Select the parents of curly-furred dogs:

```
select parent from parents, dogs
where child = name and fur = "curly";
```

Join all rows of parents to all rows of dogs, filter by `child = name` and `fur = "curly"`

Join only rows of parents and dogs where `child = name`, filter by `fur = "curly"`

Filter dogs by `fur = "curly"`, join result with all rows of parents, filter by `child = name`

Filter dogs by `fur = "curly"`, join only rows of result and parents where `child = name`

Local Tables

Local Tables

A `create table` statement names a table globally

Local Tables

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```
create table parents as
  select "abraham" as parent, "barack" as child union
  select "abraham"      , "clinton"      union
  select "delano"       , "herbert"     union
  select "fillmore"    , "abraham"   union
  select "fillmore"    , "delano"    union
  select "fillmore"    , "grover"    union
  select "eisenhower"  , "fillmore";
```


Local Tables

A `create table` statement names a table globally

```
create table parents as
  select "abraham" as parent, "barack" as child union
  select "abraham"      , "clinton"      union
  select "delano"       , "herbert"     union
  select "fillmore"    , "abraham"   union
  select "fillmore"    , "delano"   union
  select "fillmore"    , "grover"   union
  select "eisenhower" , "fillmore";
```

parents:

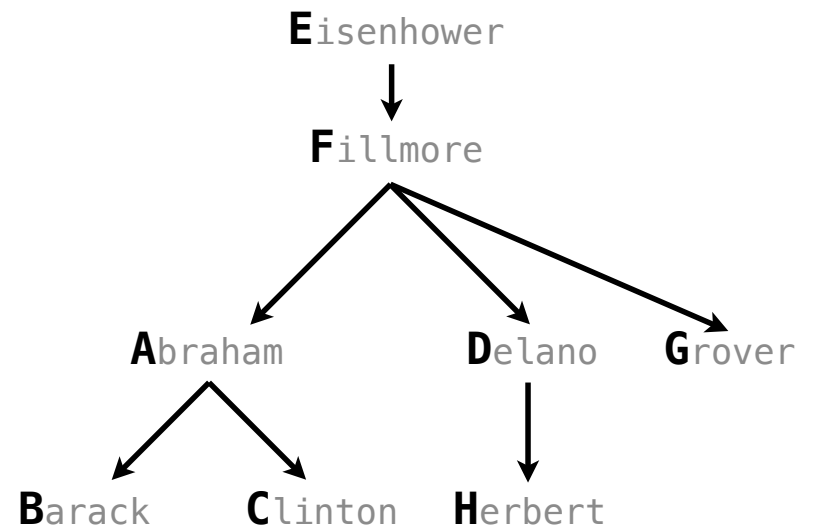
| Parent | Child |
|------------|----------|
| abraham | barack |
| abraham | clinton |
| delano | herbert |
| fillmore | abraham |
| fillmore | delano |
| fillmore | grover |
| eisenhower | fillmore |

Local Tables

A `create table` statement names a table globally

```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

parents:



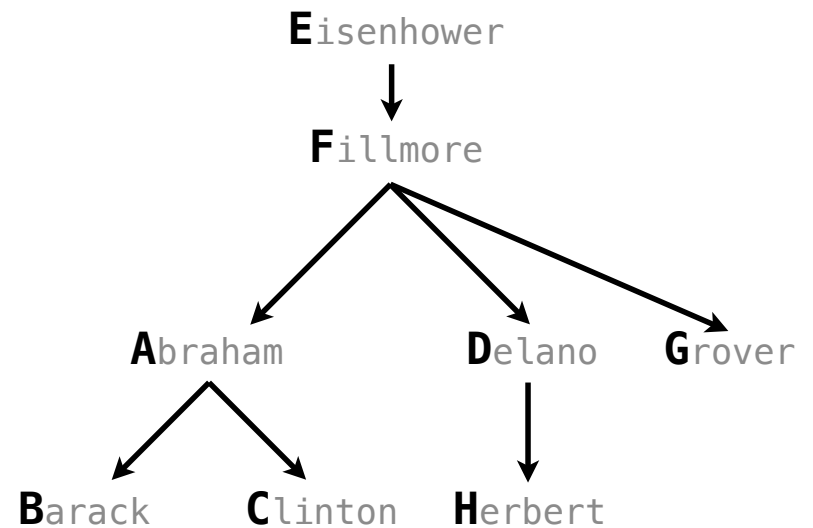
Local Tables

A `create table` statement names a table globally

A `with` clause of a `select` statement names a table that is local to the statement

```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

parents:

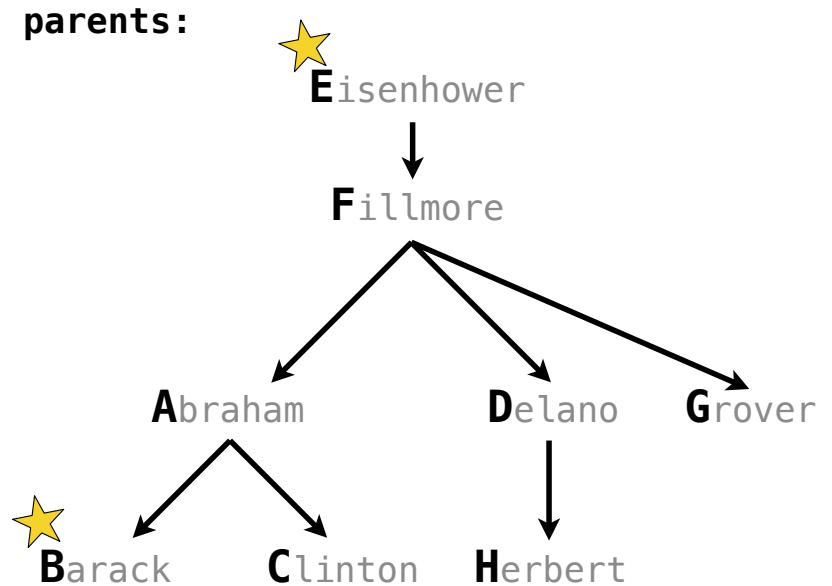


Local Tables

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```
create table parents as
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  ...
```



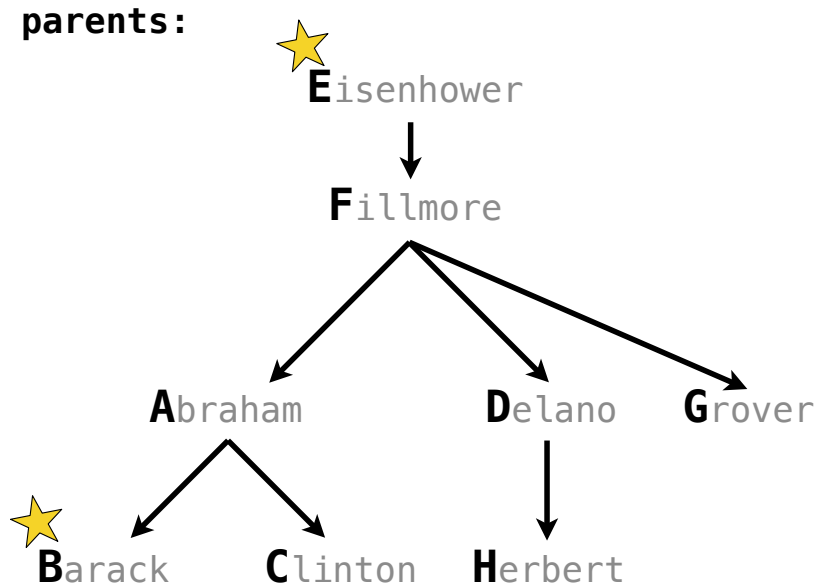
Local Tables

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A `with` clause of a `select` statement names a table that is local to the statement

```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

```
select parent from ...
```



Local Tables

A `create table` statement names a table globally

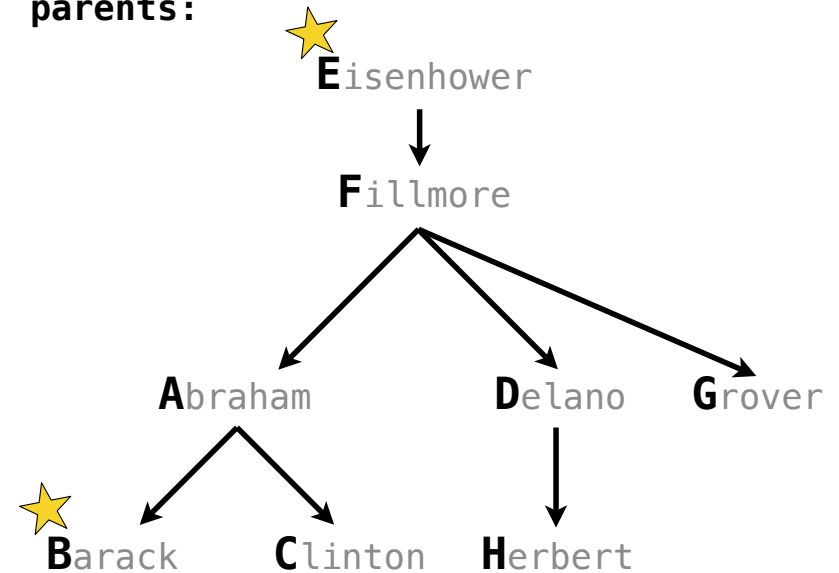
A `with` clause of a `select` statement names a table that is local to the statement

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create table parents as
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  ...
```

with

```
select parent from ...
```

parents:



Local Tables

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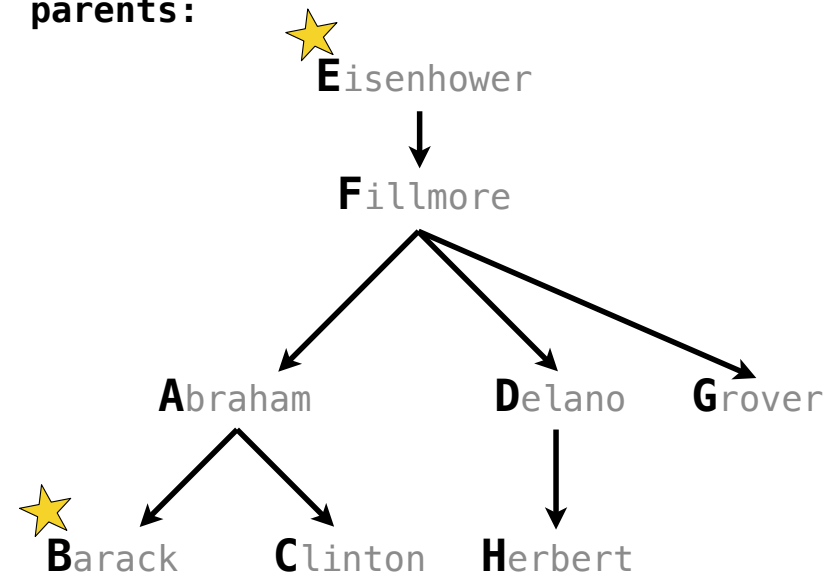
```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

with

```
best(dog) as (
```

```
select parent from ...
```

parents:



Local Tables

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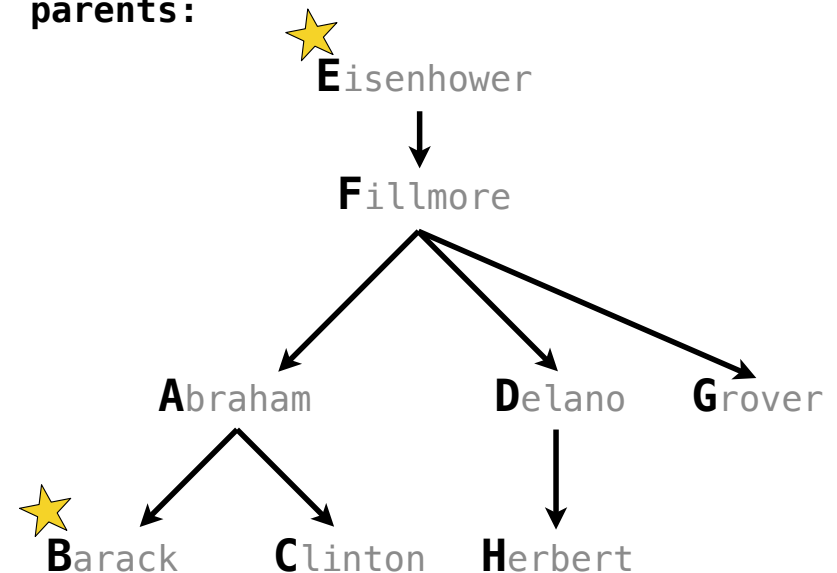
```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

with

```
best(dog) as (
  select "eisenhower" union
```

```
select parent from ...
```

parents:



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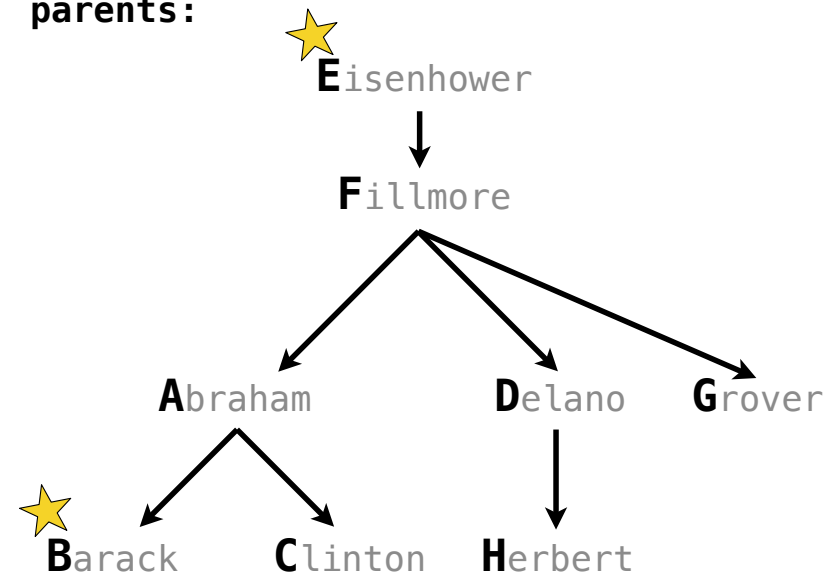
```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

with

```
best(dog) as (
  select "eisenhower" union
  select "barack"
```

```
select parent from ...
```

parents:



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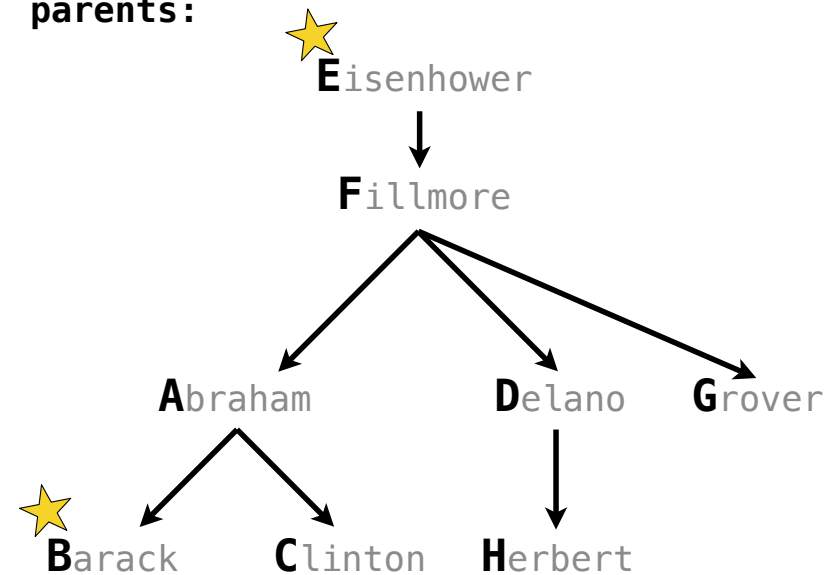
```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

with

```
best(dog) as (
  select "eisenhower" union
  select "barack"
)
```

```
select parent from ...
```

parents:



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create table parents as
  select "abraham" as parent, "barack" as child union
  ...
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with

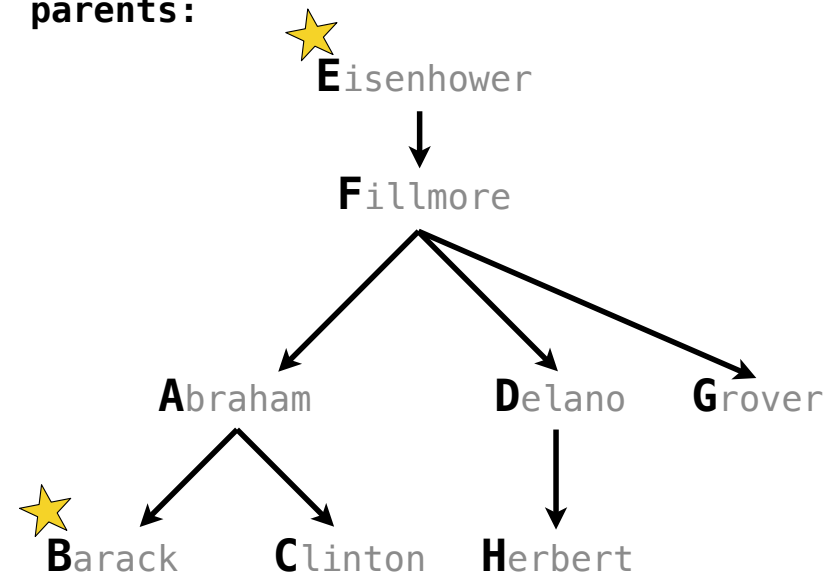
```
best(dog) as (
  select "eisenhower" union
  select "barack"
)
```

```
select parent from ...
```

best:

| dog |
|------------|
| eisenhower |
| barack |

parents:



Local Tables

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```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

with

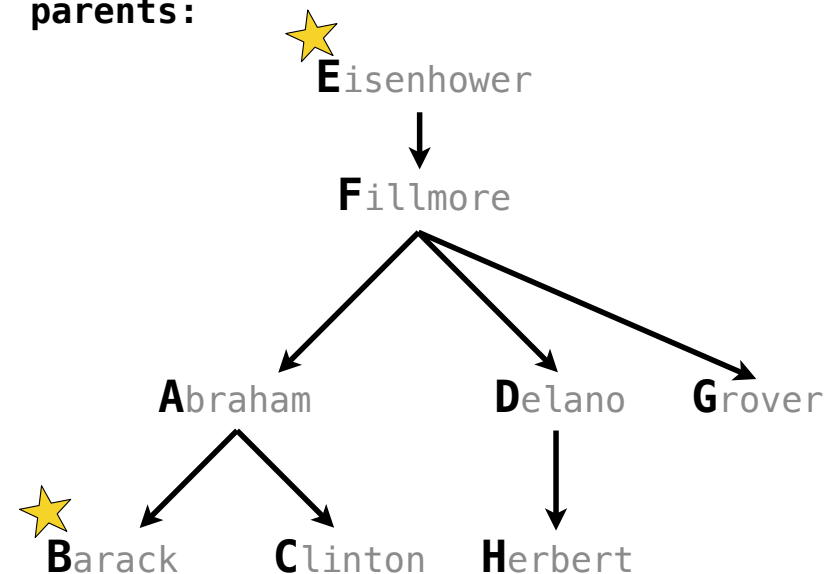
```
best(dog) as (
  select "eisenhower" union
  select "barack"
)
```

best:

| dog |
|------------|
| eisenhower |
| barack |

```
select parent from parents, best where child=dog;
```

parents:



Local Tables

A `create table` statement names a table globally

A `with` clause of a `select` statement names a table that is local to the statement

```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

with

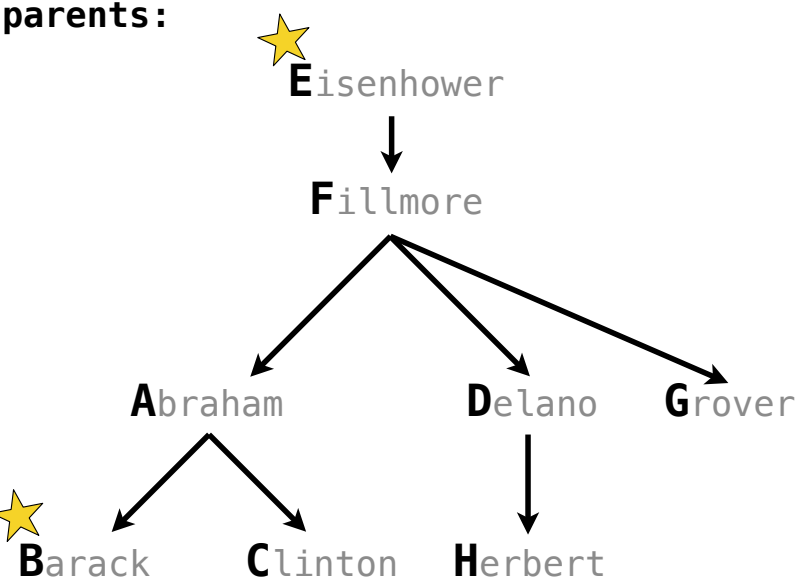
```
best(dog) as (
  select "eisenhower" union
  select "barack"
)
```

best:

| dog |
|------------|
| eisenhower |
| barack |

```
select parent from parents, best where child=dog;
```

| parent |
|---------|
| abraham |



Local Tables

A `create table` statement names a table globally

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```
create table parents as  
  select "abraham" as parent, "barack" as child union  
  ...
```

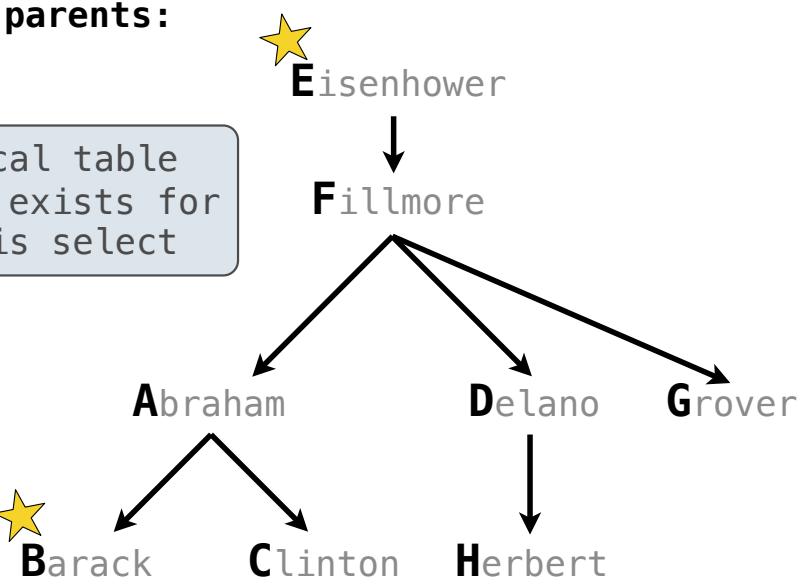
```
with  
  best(dog) as (  
    select "eisenhower" union  
    select "barack"  
  )
```

```
select parent from parents, best where child=dog;
```

| parent |
|---------|
| abraham |

| best: |
|------------|
| dog |
| eisenhower |
| barack |

Local table only exists for this select



Local Tables

A `create table` statement names a table globally

A `with` clause of a `select` statement names a table that is local to the statement

```
create table parents as  
  select "abraham" as parent, "barack" as child union
```

...
with Part of the select statement

```
  best(dog) as (  
    select "eisenhower" union  
    select "barack"  
  )
```

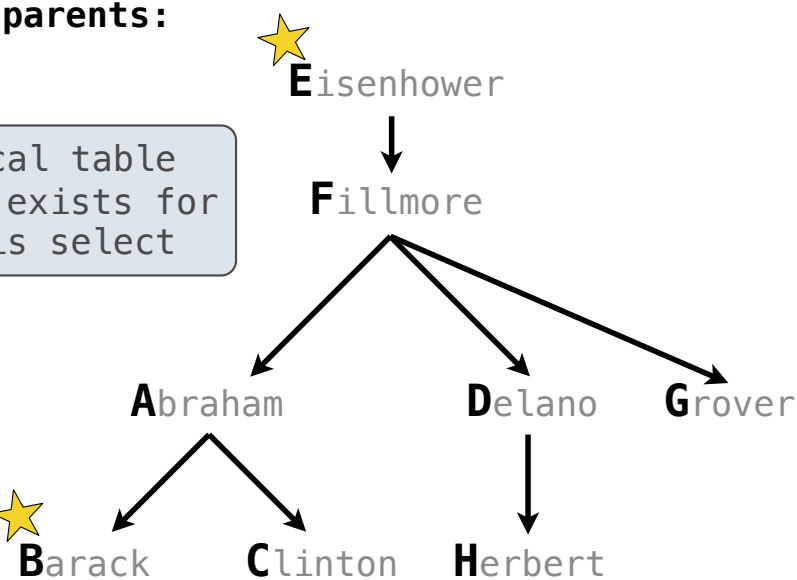
best:

| dog |
|------------|
| eisenhower |
| barack |

Local table only exists for this select

```
select parent from parents, best where child=dog;
```

| parent |
|---------|
| abraham |



Local Tables

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A `with` clause of a `select` statement names a table that is local to the statement

```
create table parents as
  select "abraham" as parent, "barack" as child union
```

...

Part of the
select statement

with

```
best(dog) as (
  select "eisenhower" union
  select "barack"
)
```

best:

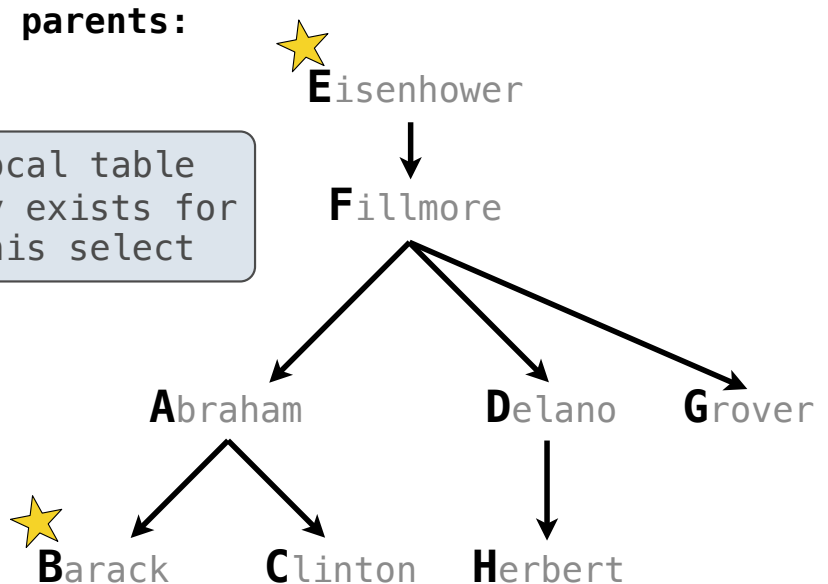
| dog |
|------------|
| eisenhower |
| barack |

Local table
only exists for
this select

```
select parent from parents, best where child=dog;
```

| parent |
|---------|
| abraham |

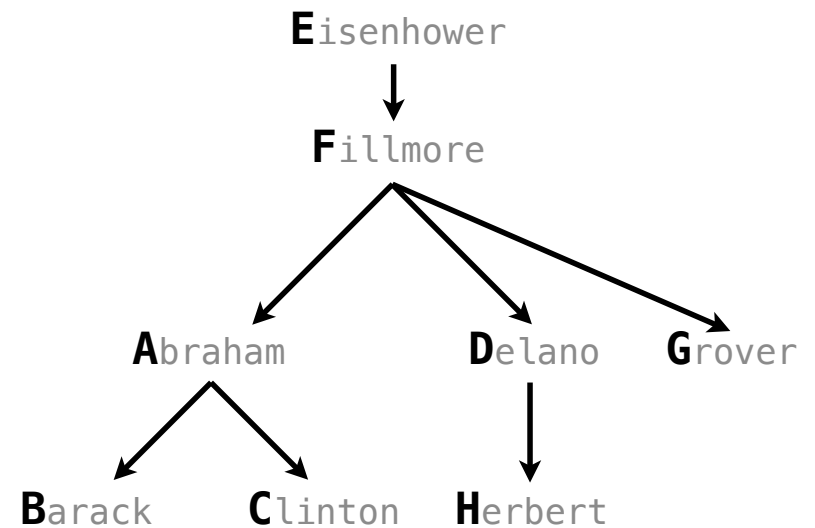
(Demo)



Example: Relationships

```
with
  what(first, second) as (
    select a.child, b.child
           from parents as a, parents as b
           where a.parent = b.parent and
                 a.child != b.child
  )
select child as _____, second as _____
       from parents, what where parent=first;
```

parents:



Example: Relationships

(A) What are appropriate names for the columns in this result?

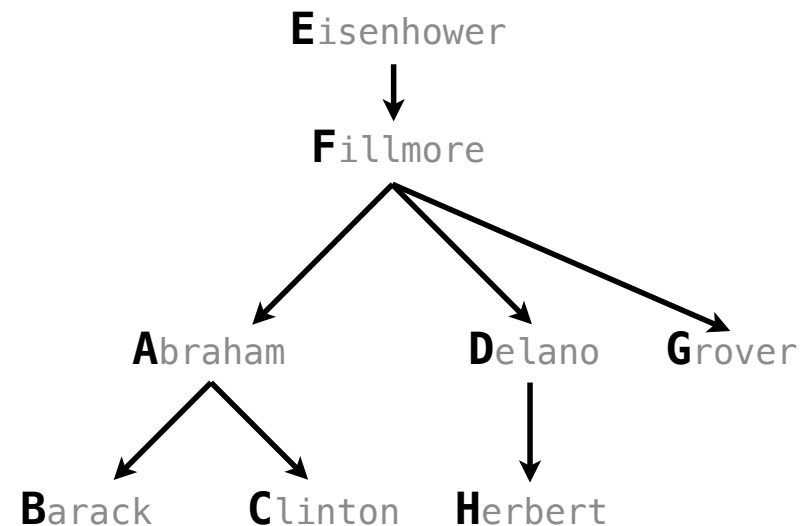
with

```
what(first, second) as (  
  select a.child, b.child  
    from parents as a, parents as b  
   where a.parent = b.parent and  
         a.child != b.child
```

)

```
select child as _____, second as _____  
  from parents, what where parent=first;
```

parents:



Example: Relationships

(A) What are appropriate names for the columns in this result?

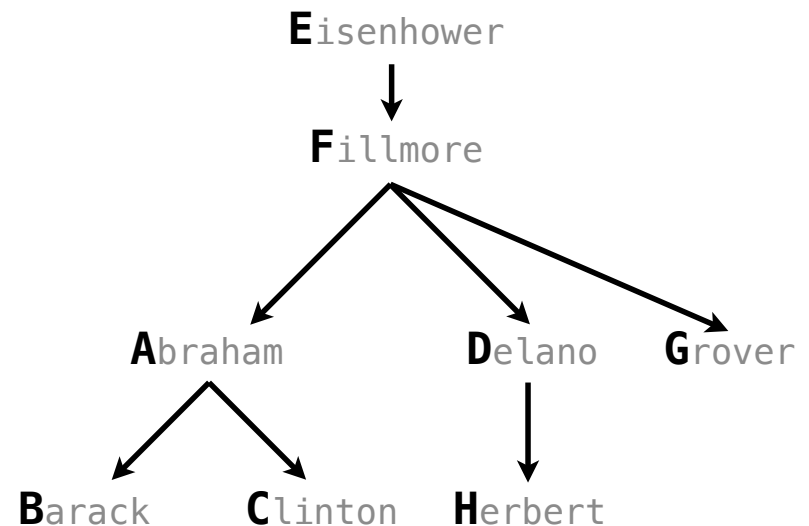
(B) How many rows and columns will result?

with

```
what(first, second) as (  
  select a.child, b.child  
    from parents as a, parents as b  
   where a.parent = b.parent and  
         a.child != b.child  
)
```

```
select child as _____, second as _____  
  from parents, what where parent=first;
```

parents:



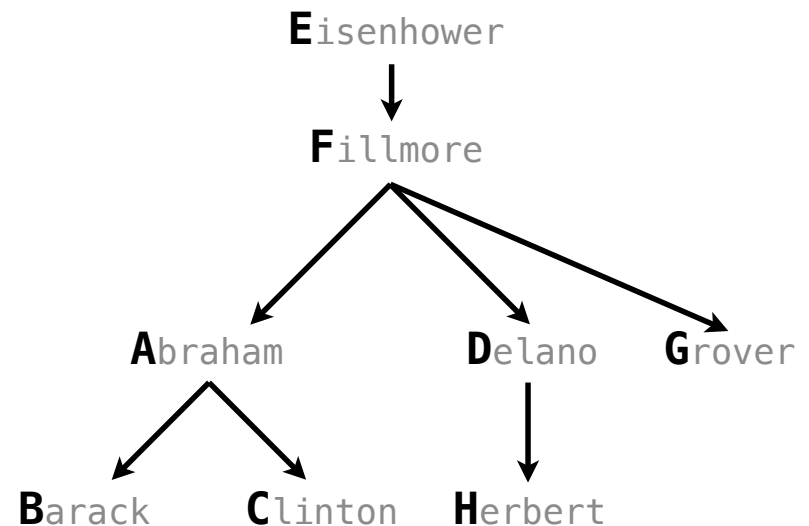
Example: Relationships

(A) What are appropriate names for the columns in this result?

(B) How many rows and columns will result?

```
with
siblings
what(first, second) as (
  select a.child, b.child
        from parents as a, parents as b
        where a.parent = b.parent and
              a.child != b.child
)
select child as _____, second as _____
       from parents, what siblings where parent=first;
```

parents:



Example: Relationships

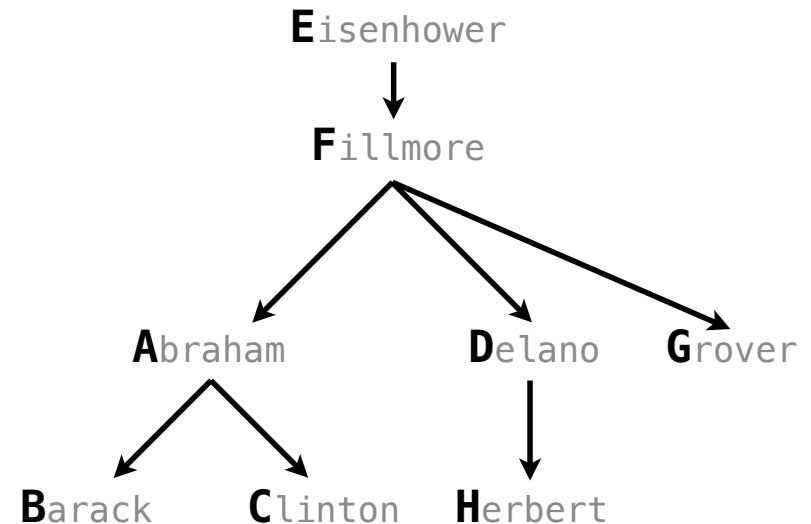
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with
siblings
what(first, second) as (
  select a.child, b.child
        from parents as a, parents as b
        where a.parent = b.parent and
              a.child != b.child
)
select child as _____, second as _____
      from parents, what siblings
      where parent=first;
```

| parent | child | first | second |
|---------|--------|---------|--------|
| abraham | barack | abraham | delano |

parents:



Example: Relationships

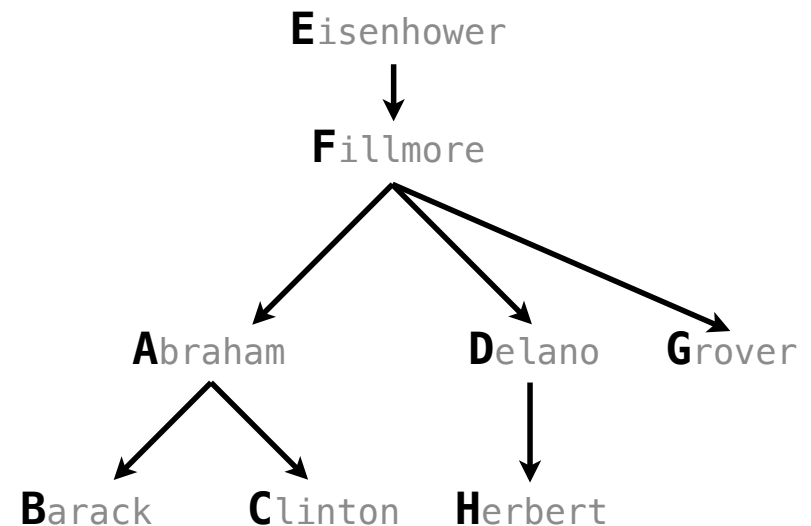
(A) What are appropriate names for the columns in this result?

(B) How many rows and columns will result?

```
with
siblings
what(first, second) as (
  select a.child, b.child
        from parents as a, parents as b
        where a.parent = b.parent and
              a.child != b.child
)
select child as _____, second as _____
      from parents, what siblings
      where parent=first;
```

| parent | child | first | second |
|---------|--------|---------|--------|
| abraham | barack | abraham | delano |

parents:



Example: Relationships

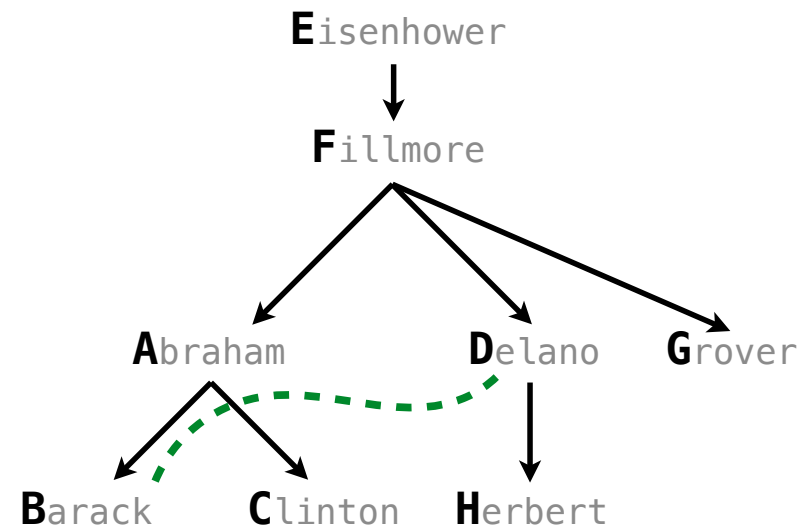
(A) What are appropriate names for the columns in this result?

(B) How many rows and columns will result?

```
with
siblings
what(first, second) as (
  select a.child, b.child
        from parents as a, parents as b
        where a.parent = b.parent and
              a.child != b.child
)
select child as _____, second as _____
      from parents, what siblings where parent=first;
```

| parent | child | first | second |
|---------|--------|---------|--------|
| abraham | barack | abraham | delano |

parents:



Example: Relationships

(A) What are appropriate names for the columns in this result?

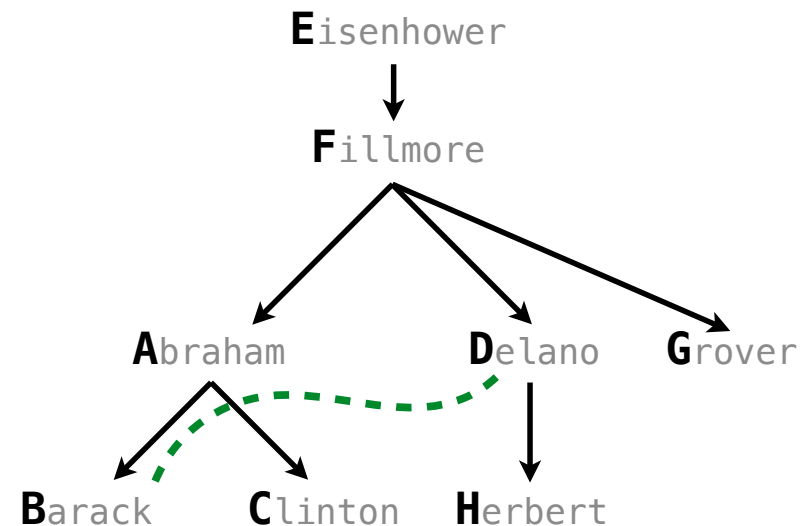
(B) How many rows and columns will result?

```

with
siblings
what(first, second) as (
  select a.child, b.child
        from parents as a, parents as b
        where a.parent = b.parent and
              a.child != b.child
)
select child as nephew, second as uncle
        from parents, what siblings where parent=first;
  
```

| parent | child | first | second |
|---------|------------------|---------|-------------------|
| abraham | barack | abraham | delano |

parents:



Recursive Local Tables

Local Tables can be Declared Recursively

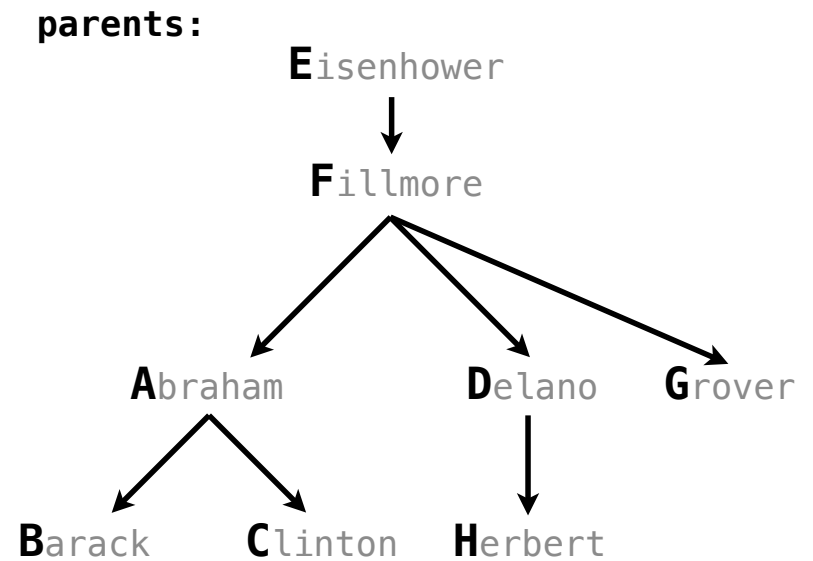
Local Tables can be Declared Recursively

An ancestor is your parent or an ancestor of your parent

Local Tables can be Declared Recursively

An ancestor is your parent or an ancestor of your parent

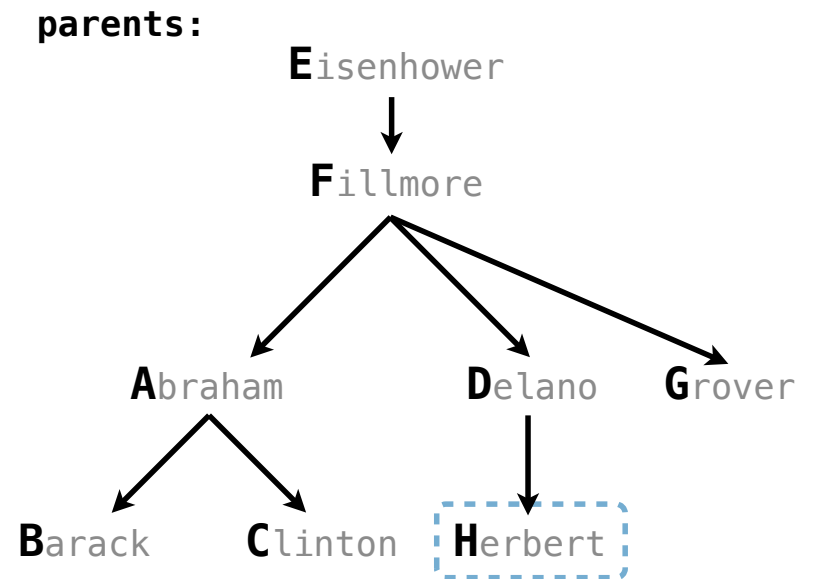
```
create table parents as
select "abraham" as parent, "barack" as child union
...
```



Local Tables can be Declared Recursively

An ancestor is your parent or an ancestor of your parent

```
create table parents as
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...
```

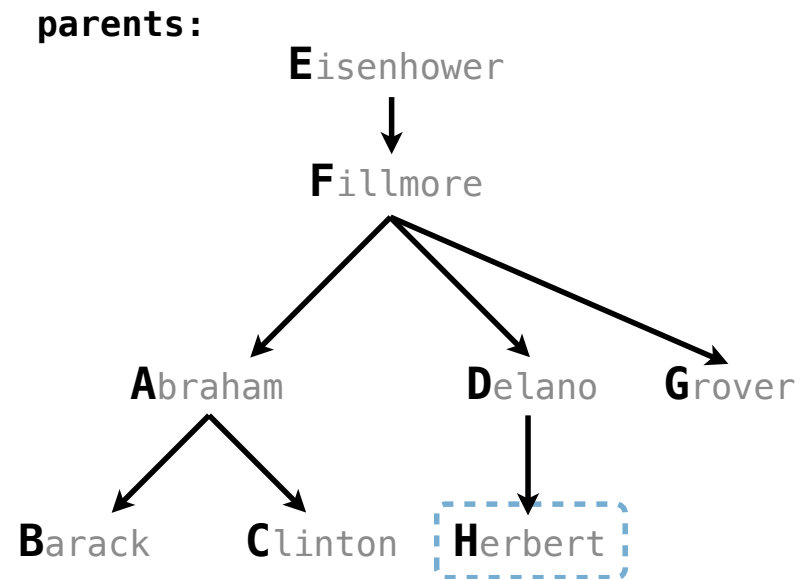


Local Tables can be Declared Recursively

An ancestor is your parent or an ancestor of your parent

```
create table parents as
select "abraham" as parent, "barack" as child union
...
```

ancestors(ancestor, descendent)

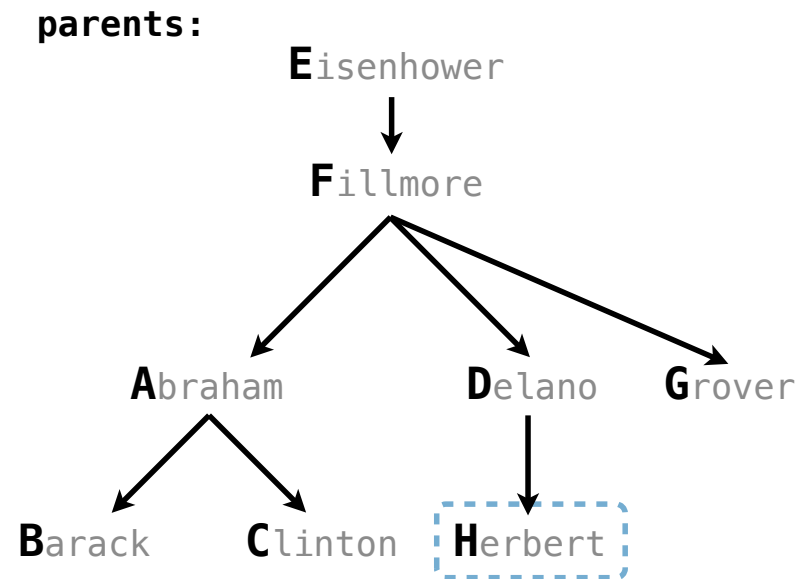


Local Tables can be Declared Recursively

An ancestor is your parent or an ancestor of your parent

```
create table parents as
select "abraham" as parent, "barack" as child union
...
```

```
ancestors(ancestor, descendent) as (
  select parent, child from parents union
  select ancestor, child
  from ancestors, parents
  where parent = descendent
)
```



Local Tables can be Declared Recursively

An ancestor is your parent or an ancestor of your parent

```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

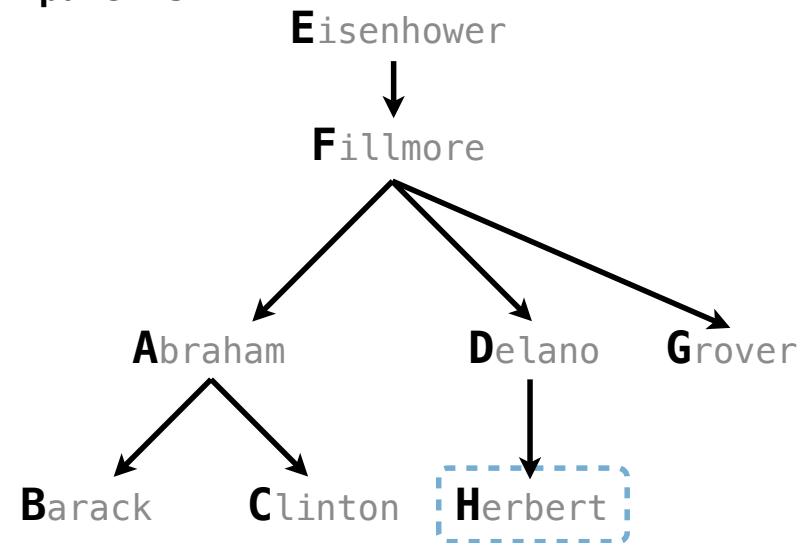
with

```
ancestors(ancestor, descendent) as (
  select parent, child from parents union
  select ancestor, child
  from ancestors, parents
  where parent = descendent
```

)

```
select ancestor from ancestors where descendent="herbert";
```

parents:



Local Tables can be Declared Recursively

An ancestor is your parent or an ancestor of your parent

```
create table parents as
  select "abraham" as parent, "barack" as child union
  ...
```

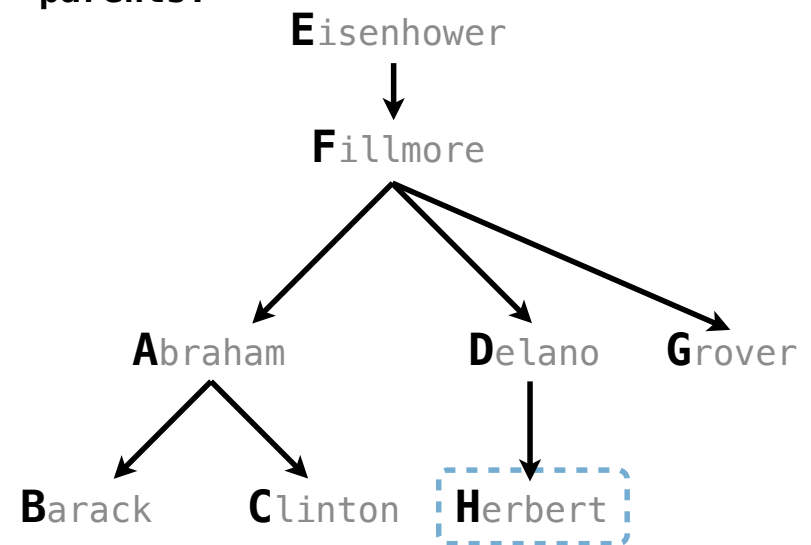
with

```
ancestors(ancestor, descendent) as (
  select parent, child from parents union
  select ancestor, child
  from ancestors, parents
  where parent = descendent
```

)

```
select ancestor from ancestors where descendent="herbert";
```

parents:



| ancestor |
|------------|
| delano |
| fillmore |
| eisenhower |

Global Names for Recursive Tables

To create a table with a global name, you need to select the contents of the local table

Global Names for Recursive Tables

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```
create table odds as
with
  odds(n) as (
    select 1 union
    select n+2 from odds where n < 15
  )
select n from odds;
```

Global Names for Recursive Tables

To create a table with a global name, you need to select the contents of the local table

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    select 1 union
    select n+2 from odds where n < 15
  )
select n from odds;
```

odds:

| n |
|----|
| 1 |
| 3 |
| 5 |
| 7 |
| 9 |
| 11 |
| 13 |
| 15 |

Global Names for Recursive Tables

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| 1 |
| 3 |
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| 7 |
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odds:

| n |
|----|
| 1 |
| 3 |
| 5 |
| 7 |
| 9 |
| 11 |
| 13 |
| 15 |

Which names above can change without affecting the result?

Global Names for Recursive Tables

To create a table with a global name, you need to select the contents of the local table

```
create table odds as
with
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  )
select n from odds;
```

odds:

| n |
|----|
| 1 |
| 3 |
| 5 |
| 7 |
| 9 |
| 11 |
| 13 |
| 15 |

Which names above can change without affecting the result?

Limits on Recursive Select Statements

Limits on Recursive Select Statements

Recursive table definitions are only possible within a with clause

Limits on Recursive Select Statements

Recursive table definitions are only possible within a with clause

No mutual recursion: two or more tables cannot be defined in terms of each other

Limits on Recursive Select Statements

Recursive table definitions are only possible within a with clause

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with
  odds(x) as (
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```
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      from ints as a, ints as b
  )
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String Examples

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Noun phrases can contain relative pronouns that introduce relative clauses


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(Demo)

Integer Examples

Input-Output Tables

A table containing the inputs to a function can be used to map from output to input

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```
create table pairs as
with
  i(n) as (
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  )
select a.n as x, b.n as y from i as a, i as b where a.n <= b.n;
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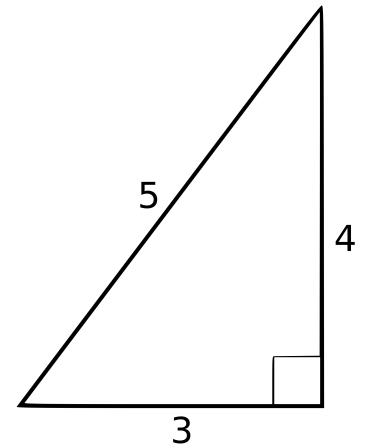
(Demo)

Example: Pythagorean Triples

All triples a, b, c such that $a^2 + b^2 = c^2$

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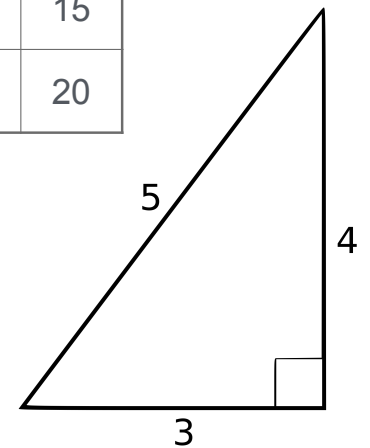
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Example: Pythagorean Triples

All triples a , b , c such that $a^2 + b^2 = c^2$

| a | b | c |
|----------|----------|----------|
| 3 | 4 | 5 |
| 5 | 12 | 13 |
| 6 | 8 | 10 |
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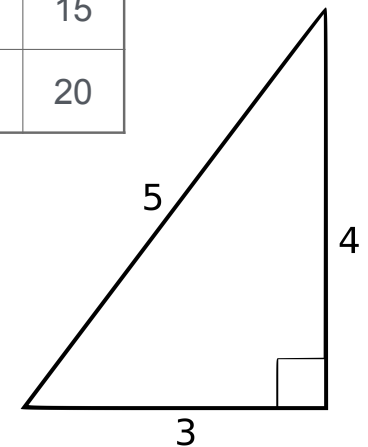
`)`

`select a.n as a, b.n as b, c.n as c`

`from _____`

`where _____ and a.n*a.n + b.n*b.n = c.n*c.n;`

| a | b | c |
|----|----|----|
| 3 | 4 | 5 |
| 5 | 12 | 13 |
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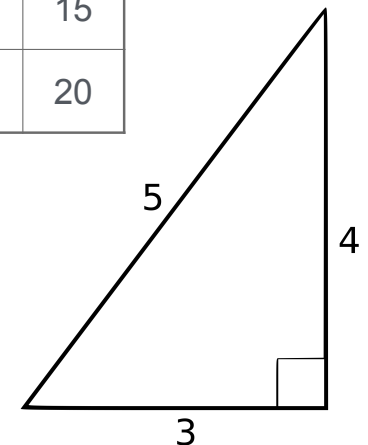
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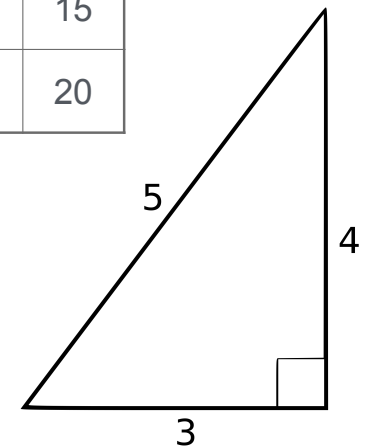
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Example: Fibonacci Sequence

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Computing the next Fibonacci number requires both the previous and current numbers

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fib:

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|----|
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Computing the next Fibonacci number requires both the previous and current numbers

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create table fibs as
with
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