

Import statement

```
1 from math import pi
2 tau = 2 * pi
```

Assignment statement

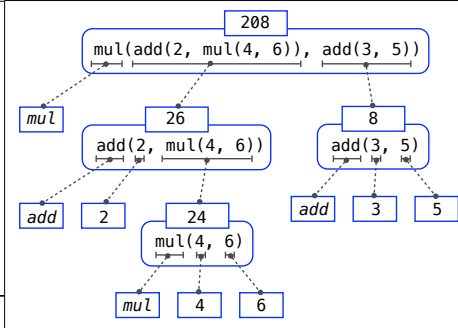
Global frame

Name	Value
pi	3.1416

Binding

Code (left): Statements and expressions
Red arrow points to next line. Gray arrow points to the line just executed

Frames (right): A name is bound to a value
In a frame, there is at most one binding per name



Pure Functions

```
-2 > abs(number): 2
2, 10 > pow(x, y): 1024
```

Non-Pure Functions

```
-2 > print(...): None
```

display "-2"

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(-2)
```

Global frame

Intrinsic name of function called

mul

square

Local frame

f1: square [parent=Global]

Formal parameter bound to argument

x -2

Return value

4

User-defined function

Return value is not a binding!

Built-in function

func mul(...) [parent=Global]

func square(x) [parent=Global]

Defining:

```
>>> def square(x):
    return mul(x, x)
```

Def statement

Formal parameter

Return expression

Body (return statement)

Call expression: square(2+2)

operator: square

function: func square(x)

operand: 2+2

argument: 4

Compound statement

Clause

```
<header>:
<statement>
<statement>
```

Suite

```
<separating header>:
<statement>
<statement>
...
```

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(square(3))
```

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

Global frame

mul

square

Local frame

f1: square [parent=Global]

x 3

Return value 9

Local frame

f2: square [parent=Global]

x 9

Return value 81

Calling/Applying:

```
4 > square(x):
    return mul(x, x)
```

Argument

Intrinsic name

Return value

```
def abs_value(x):
    1 statement,
    3 clauses,
    3 headers,
    3 suites,
    2 boolean contexts
    if x > 0:
        return x
    elif x == 0:
        return 0
    else:
        return -x
```

Evaluation rule for call expressions:

- Evaluate the operator and operand subexpressions.
- Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions.

Applying user-defined functions:

- Create a new local frame with the same parent as the function that was applied.
- Bind the arguments to the function's formal parameter names in that frame.
- Execute the body of the function in the environment beginning at that frame.

```
1 def f(x, y):
2     return g(x)
3
4 def g(a):
5     return a + y
6
7 result = f(1, 2)
```

Global frame

func f(x, y) [parent=Global]

func g(a) [parent=Global]

f1: f [parent=Global]

x 1

y 2

f2: g [parent=Global]

a 1

Error

"y" is not found

- An environment is a sequence of frames
- An environment for a non-nested function (no def within def) consists of one local frame, followed by the global frame

Execution rule for def statements:

- Create a new function value with the specified name, formal parameters, and function body.
- Its parent is the first frame of the current environment.
- Bind the name of the function to the function value in the first frame of the current environment.

Execution rule for assignment statements:

- Evaluate the expression(s) on the right of the equal sign.
- Simultaneously bind the names on the left to those values, in the first frame of the current environment.

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(4)
```

Global frame

mul

square

Local frame

f1: square [parent=Global]

square 4

Return value 16

A call expression and the body of the function being called are evaluated in different environments

Higher-order function: A function that takes a function as an argument value or returns a function as a return value

Nested def statements: Functions defined within other function bodies are bound to names in the local frame

Execution rule for conditional statements:

Each clause is considered in order.

- Evaluate the header's expression.
- If it is a true value, execute the suite, then skip the remaining clauses in the statement.

Evaluation rule for or expressions:

- Evaluate the subexpression <left>.
- If the result is a true value v, then the expression evaluates to v.
- Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for and expressions:

- Evaluate the subexpression <left>.
- If the result is a false value v, then the expression evaluates to v.
- Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for not expressions:

- Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

Execution rule for while statements:

- Evaluate the header's expression.
- If it is a true value, execute the (whole) suite, then return to step 1.

```
def fib(n):
    """Compute the nth Fibonacci number, for N >= 1."""
    pred, curr = 0, 1 # Zeroth and first Fibonacci numbers
    k = 1 # curr is the kth Fibonacci number
    while k < n:
        pred, curr = curr, pred + curr
        k = k + 1
    return curr
```

def cube(k):
return pow(k, 3)

def summation(n, term):
"""Sum the first n terms of a sequence.

```
>>> summation(5, cube)
225
```

total, k = 0, 1
while k <= n:
total, k = total + term(k), k + 1
return total

0 + 1³ + 2³ + 3³ + 4³ + 5³

Function of a single argument (not called term)

A formal parameter that will be bound to a function

The cube function is passed as an argument value

The function bound to term gets called here

Rational implementation using functions:

```
def rational(n, d):
    def select(name):
        if name == 'n':
            return n
        elif name == 'd':
            return d
    return select
```

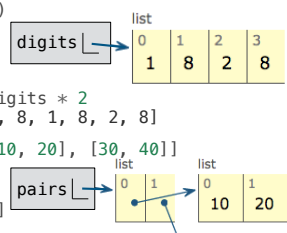
This function represents a rational number

```
def numer(x):
    return x('n')
def denom(x):
    return x('d')
```

Constructor is a higher-order function
Selector calls x

Lists:

```
>>> digits = [1, 8, 2, 8]
>>> len(digits)
4
>>> digits[3]
8
>>> [2, 7] + digits * 2
[2, 7, 1, 8, 2, 8, 1, 8, 2, 8]
>>> pairs = [[10, 20], [30, 40]]
>>> pairs[1]
[30, 40]
>>> pairs[1][0]
30
```



Executing a for statement:

```
for <name> in <expression>:
    <suite>
```

- Evaluate the header <expression>, which must yield an iterable value (a list, tuple, iterator, etc.)
- For each element in that sequence, in order:
 - Bind <name> to that element in the current frame
 - Execute the <suite>

Unpacking in a for statement:

```
>>> pairs = [[1, 2], [2, 2], [3, 2], [4, 4]]
>>> same_count = 0
for x, y in pairs:
    if x == y:
        same_count = same_count + 1
>>> same_count
2
```

A sequence of fixed-length sequences
A name for each element in a fixed-length sequence

```
..., -3, -2, -1, 0, 1, 2, 3, 4, ...
range(-2, 2)
```

Length: ending value - starting value
Element selection: starting value + index

```
>>> list(range(-2, 2))
[-2, -1, 0, 1]
>>> list(range(4))
[0, 1, 2, 3]
```

List constructor
Range with a 0 starting value

Membership:

```
>>> digits = [1, 8, 2, 8]
>>> 2 in digits
True
>>> 1828 not in digits
True
```

Slicing:

```
>>> digits[0:2]
[1, 8]
>>> digits[1:]
[8, 2, 8]
```

Slicing creates a new object

Functions that aggregate iterable arguments

- sum(iterable[, start]) -> value
- max(iterable[, key=func]) -> value
- max(a, b, c, ..., [key=func]) -> value
- min(iterable[, key=func]) -> value
- min(a, b, c, ..., [key=func]) -> value
- all(iterable) -> bool
- any(iterable) -> bool

```
iter(iterable):
    Return an iterator over the elements of an iterable value
next(iterator):
    Return the next element
```

A generator function is a function that yields values instead of returning them.

```
>>> def plus_minus(x):
...     yield x
...     yield -x
>>> t = plus_minus(3)
>>> next(t)
3
>>> next(t)
-3
```

List comprehensions:

```
[<map exp> for <name> in <iter exp> if <filter exp>]
Short version: [<map exp> for <name> in <iter exp>]
```

A combined expression that evaluates to a list using this evaluation procedure:

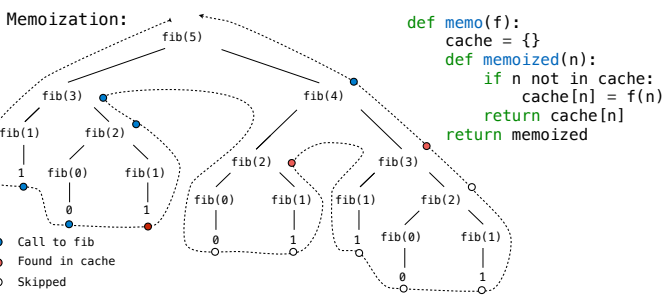
- Add a new frame with the current frame as its parent
- Create an empty result list that is the value of the expression
- For each element in the iterable value of <iter exp>:
 - Bind <name> to that element in the new frame from step 1
 - If <filter exp> evaluates to a true value, then add the value of <map exp> to the result list

```
>>> repr(12e12)
12000000000000.0
>>> print(repr(12e12))
12000000000000.0
```

```
>>> today = datetime.date(2019, 10, 13)
>>> print(today)
2019-10-13
>>> today.__repr__()
'datetime.date(2019, 10, 13)'
>>> today.__str__()
'2019-10-13'
```

str and repr are both polymorphic; they apply to any object
repr invokes a zero-argument method __repr__ on its argument

```
def cascade(n):
    if n < 10:
        print(n)
    else:
        print(n)
        cascade(n//10)
        print(n)
>>> cascade(123)
123
12
1
```



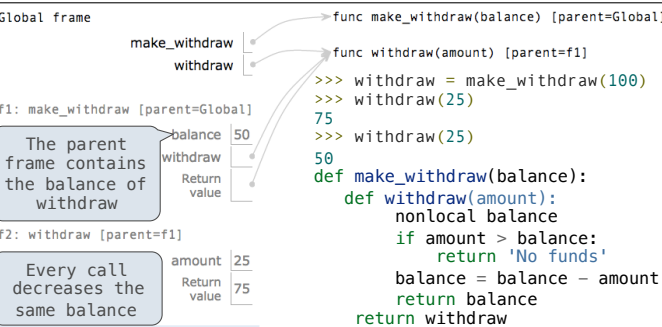
Exponential growth. E.g., recursive fib
Incrementing n multiplies time by a constant

Quadratic growth. E.g., overlap
Incrementing n increases time by n times a constant

Linear growth. E.g., slow exp
Incrementing n increases time by a constant

Logarithmic growth. E.g., exp_fast
Doubling n only increments time by a constant

Constant growth. Increasing n doesn't affect time



The parent frame contains the balance of withdraw
Every call decreases the same balance

List & dictionary mutation:

```
>>> a = [10]
>>> b = a
>>> a == b
True
>>> a.append(20)
>>> a == b
True
[10, 20]
>>> b
[10, 20]
>>> a == b
False
```

```
>>> nums = {'I': 1.0, 'V': 5, 'X': 10}
>>> nums['X']
10
>>> nums['I'] = 1
>>> nums['L'] = 50
>>> nums
{'X': 10, 'L': 50, 'V': 5, 'I': 1}
>>> sum(nums.values())
66
>>> dict([(3, 9), (4, 16), (5, 25)])
{3: 9, 4: 16, 5: 25}
>>> nums.get('A', 0)
0
>>> nums.get('V', 0)
5
>>> {x: x*x for x in range(3,6)}
{3: 9, 4: 16, 5: 25}
```

```
>>> suits = ['coin', 'string', 'myriad']
>>> suits.pop()
'myriad'
>>> suits.remove('string')
>>> suits.append('cup')
>>> suits.extend(['sword', 'club'])
>>> suits[2] = 'spade'
>>> suits
['coin', 'cup', 'spade', 'club']
>>> suits[0:2] = ['diamond']
>>> suits
['diamond', 'spade', 'club']
>>> suits.insert(0, 'heart')
>>> suits
['heart', 'diamond', 'spade', 'club']
```

Remove and return the last element
Remove a value
Add all values
Replace a slice with values
Add an element at an index

Identity:
<exp0> is <exp1> evaluates to True if both <exp0> and <exp1> evaluate to the same object
Equality:
<exp0> == <exp1> evaluates to True if both <exp0> and <exp1> evaluate to equal values
Identical objects are always equal values

You can copy a list by calling the list constructor or slicing the list from the beginning to the end.

False values:

```
>>> bool(0)
False
>>> bool(1)
True
>>> bool('')
False
>>> bool('0')
True
>>> bool([])
False
>>> bool([[]])
True
>>> bool({})
False
>>> bool(())
False
>>> bool(lambda x: 0)
True
```

All other values are true values.

Status	Effect
•No nonlocal statement •"x" is not bound locally	Create a new binding from name "x" to number 2 in the first frame of the current environment
•No nonlocal statement •"x" is bound locally	Re-bind name "x" to object 2 in the first frame of the current environment
•nonlocal x •"x" is bound in a non-local frame	Re-bind "x" to 2 in the first non-local frame of the current environment in which "x" is bound
•nonlocal x •"x" is not bound in a non-local frame	SyntaxError: no binding for nonlocal 'x' found
•nonlocal x •"x" is bound in a non-local frame	SyntaxError: name 'x' is parameter and nonlocal
•"x" also bound locally	

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