

The Closure Property of Data Types	
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Lists can contain lists as elements (in addition to anything else)



Box-and-Pointer	Notation	in	Environment	Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element

5

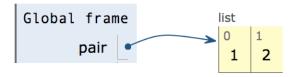
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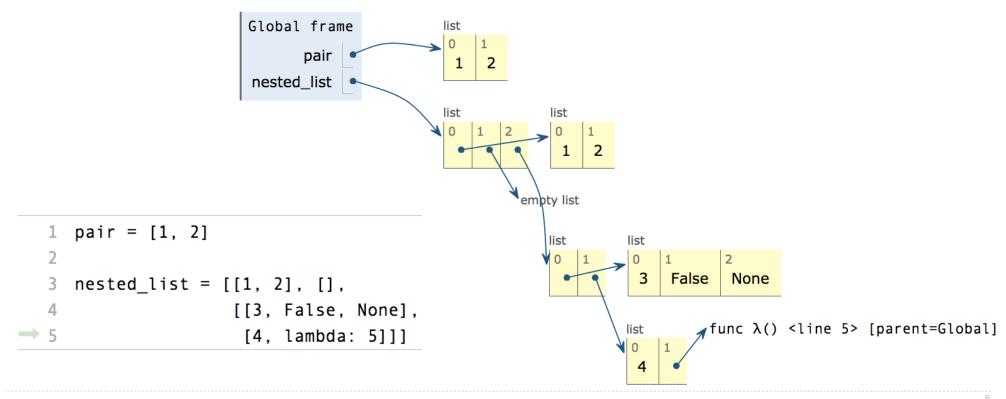
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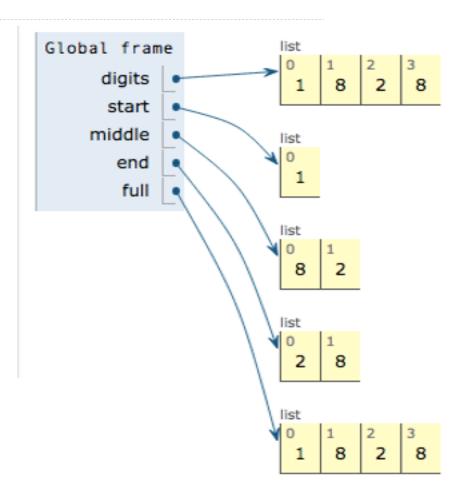
Slicing

(Demo)

Slicing Creates New Values

```
1 digits = [1, 8, 2, 8]
2 start = digits[:1]
3 middle = digits[1:3]
4 end = digits[2:]

> 5 full = digits[:]
```



pythontutor.com/composingprograms.html#code=digits%20%3D%20figits[%3A]]%0Astart%20%3D%20digits[%3A]]%0A

Processing Container Values

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Return the sum of an iterable (not of strings) plus the value of parameter 'start' (which defaults to 0). When the iterable is empty, return start.

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 max(a, b, c, ...[, key=func]) -> value

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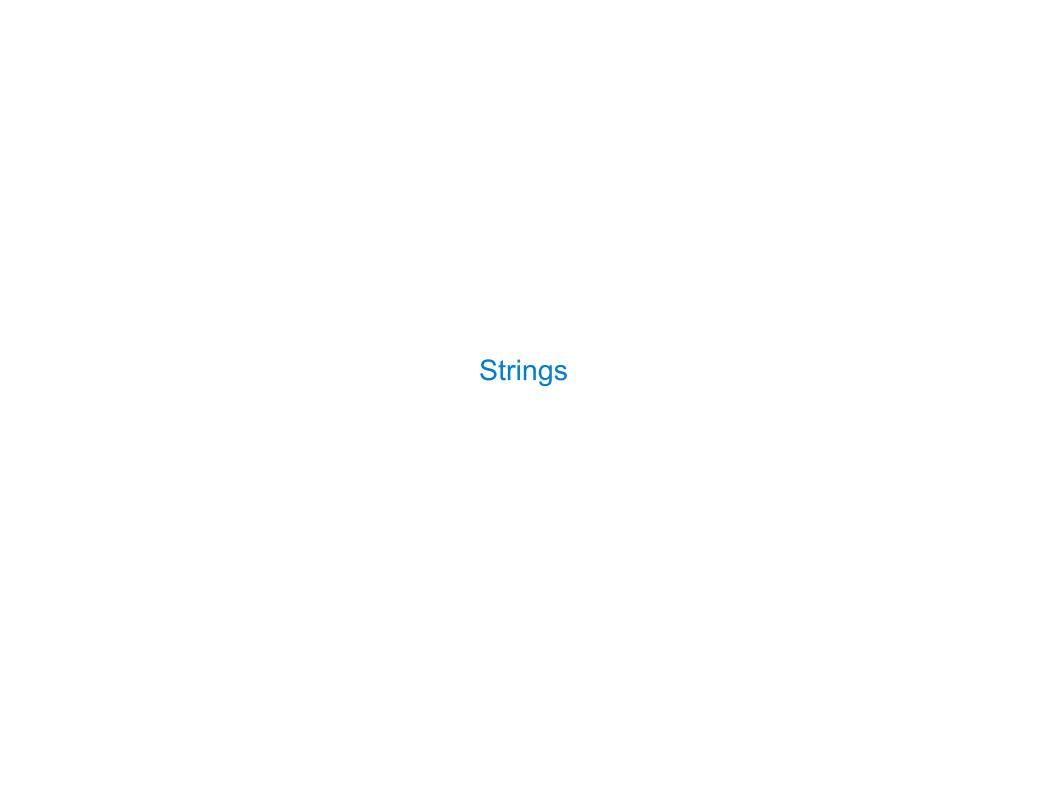
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all(iterable) -> bool

Return True if bool(x) is True for all values x in the iterable. If the iterable is empty, return True.



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Representing data:

'200' '1.2e-5' 'False' '[1, 2]'

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"""And, as imagination bodies forth
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Representing programs:

```
'curry = lambda f: lambda x: lambda y: f(x, y)'
```

Representing data:

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Representing language:

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>>> 'I am string!'
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>>> "I've got an apostrophe"
"I've got an apostrophe"
>>> '您好'
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claims, Readability counts.
Read more: import this."""
'The Zen of Python\nclaims, Readability counts.\nRead more: import this.'

A backslash "escapes" the following character
```

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>>> 'I am string!'
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                                Single-quoted and double-quoted
"I've got an apostrophe"
                                     strings are equivalent
>>> '您好'
'您好'
>>> """The Zen of Python
claims, Readability counts.
Read more: import this."""
'The Zen of Python\nclaims, Readability counts.\nRead more: import this.'
      A backslash "escapes" the
                                          "Line feed" character
         following character
                                          represents a new line
```

Dictionaries

{'Dem': 0}

Limitations on Dictionaries

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The second restriction is part of the dictionary abstraction

If you want to associate multiple values with a key, store them all in a sequence value

Dictionary Comprehensions

```
{<key exp>: <value exp> for <name> in <iter exp> if <filter exp>}
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An expression that evaluates to a dictionary using this evaluation procedure:

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 - A. Bind <name> to that element in the new frame from step 1

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{<key exp>: <value exp> for <name> in <iter exp> if <filter exp>}
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 - B. If <filter exp> evaluates to a true value, then add to the result dictionary an entry that pairs the value of <key exp> to the value of <value exp>

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  A. Bind <name> to that element in the new frame from step 1
  B. If <filter exp> evaluates to a true value, then add to the result dictionary
     an entry that pairs the value of <key exp> to the value of <value exp>
 \{x * x: x \text{ for } x \text{ in } [1, 2, 3, 4, 5] \text{ if } x > 2\} evaluates to \{9: 3, 16: 4, 25: 5\}
```

Example: Indexing

Implement index, which takes a sequence of keys, a sequence of values, and a two-argument match function. It returns a dictionary from keys to lists in which the list for a key k contains all values v for which match(k, v) is a true value.

```
def index(keys, values, match):
    """Return a dictionary from keys k to a list of values v for which
    match(k, v) is a true value.

>>> index([7, 9, 11], range(30, 50), lambda k, v: v % k == 0)
    {7: [35, 42, 49], 9: [36, 45], 11: [33, 44]}
    """
    return
```

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