

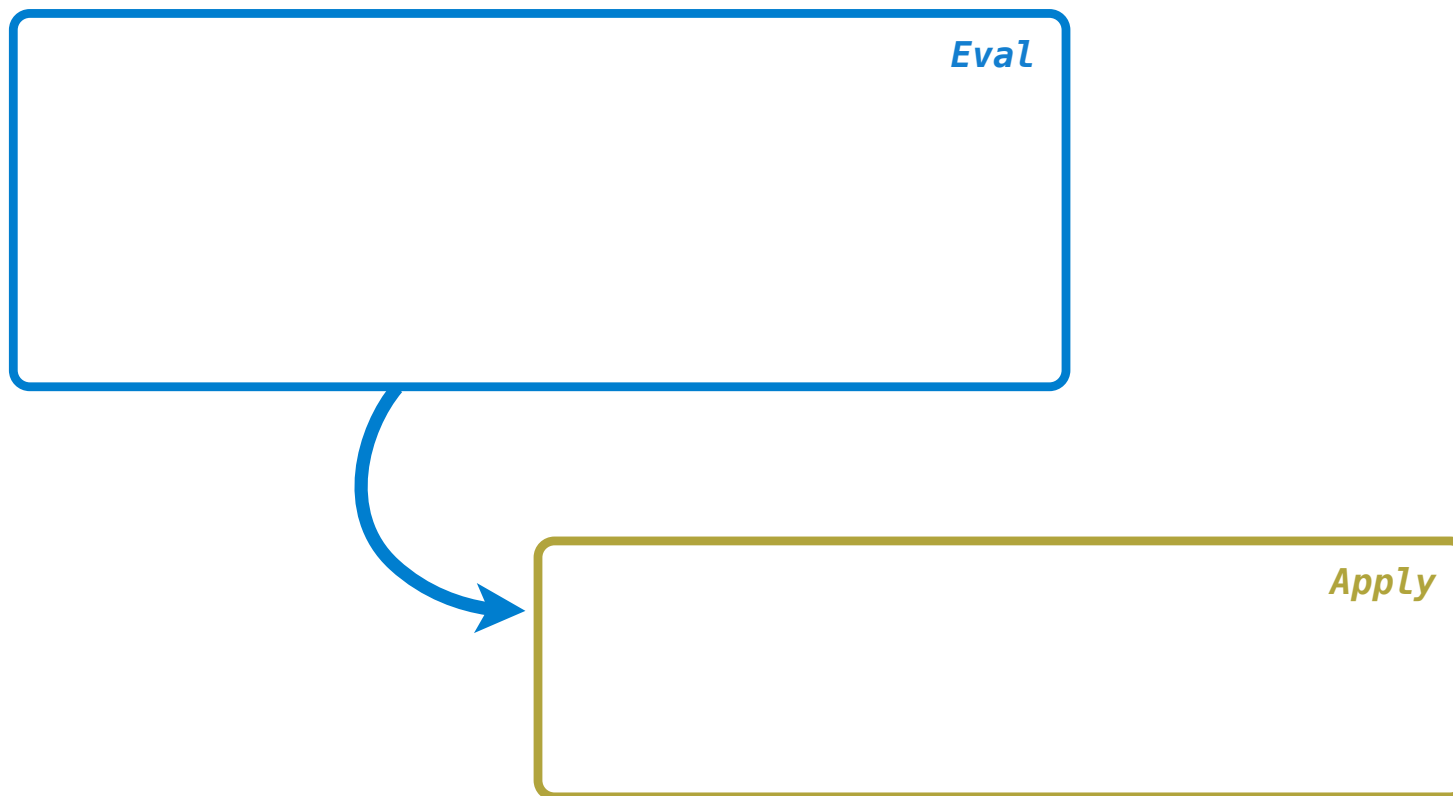
Interpreters

Announcements

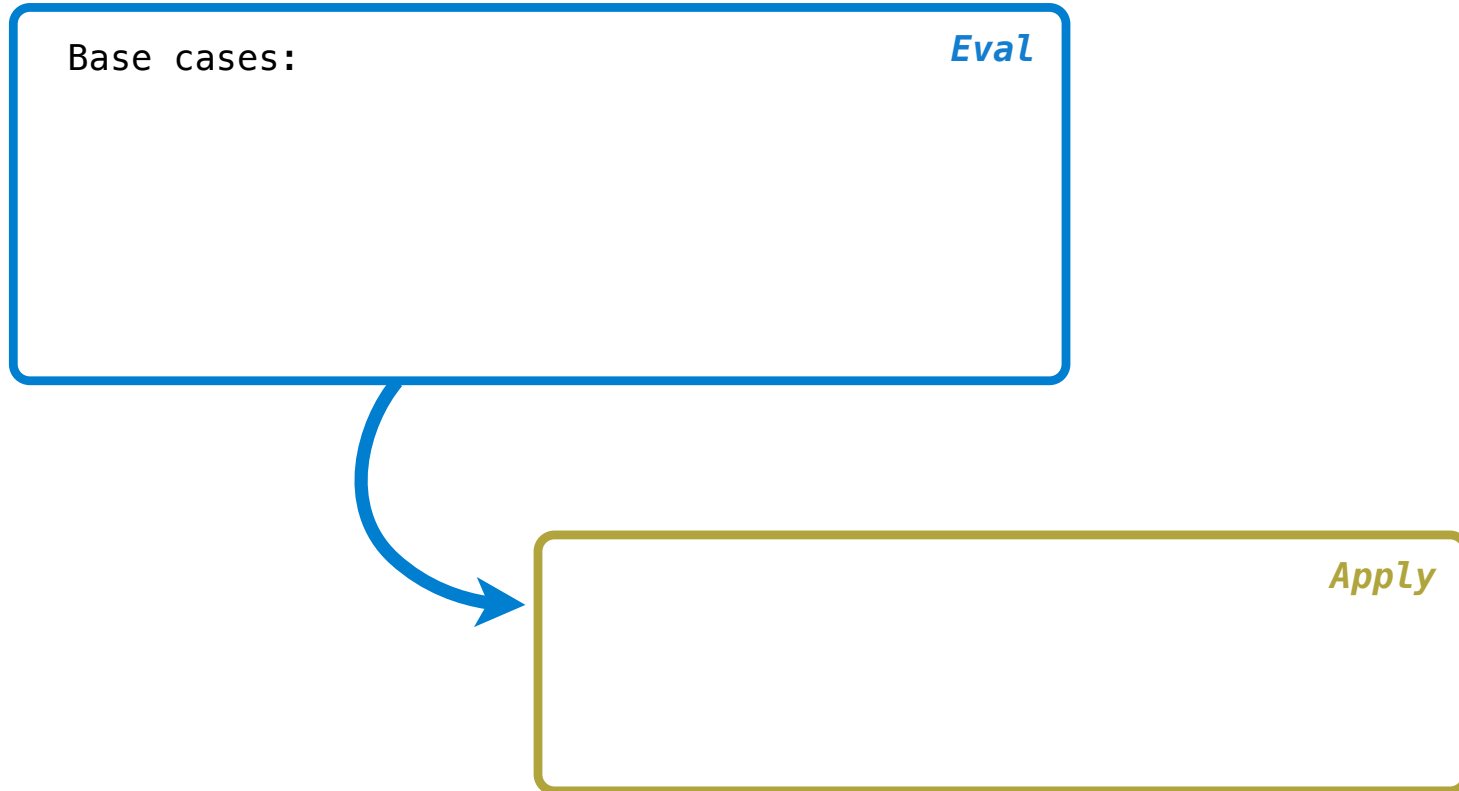
Interpreting Scheme

The Structure of an Interpreter

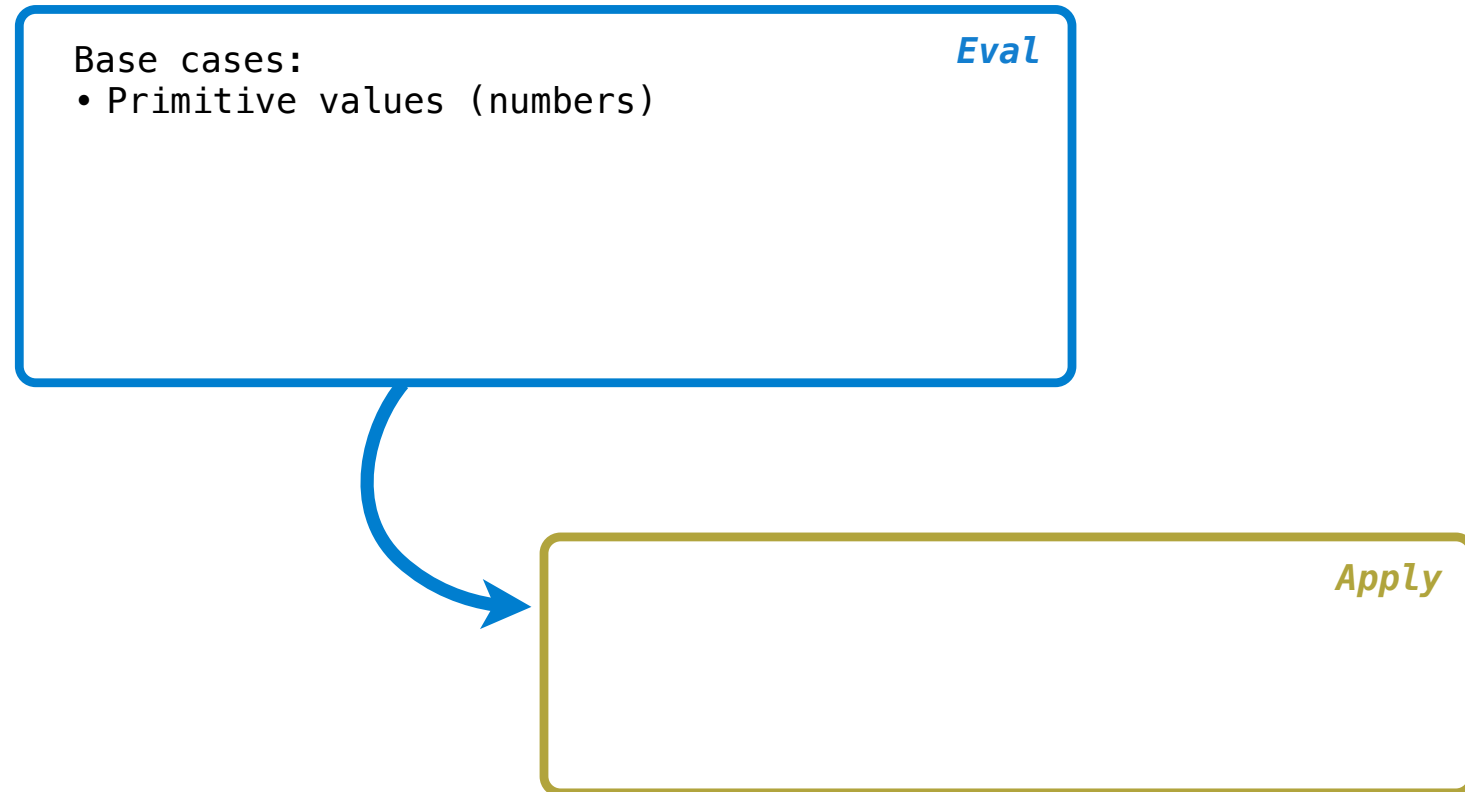
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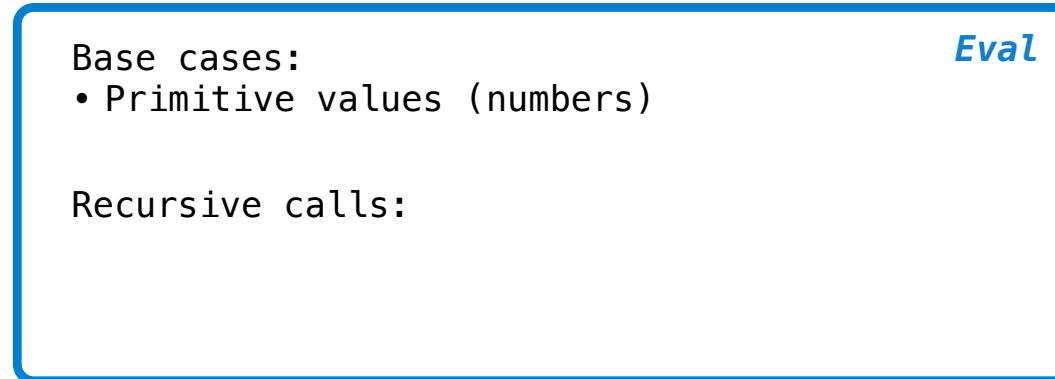
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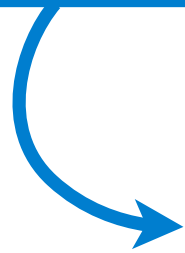
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- Primitive values (numbers)

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Recursive calls:

- `Eval(operator, operands)` of call expressions



Apply

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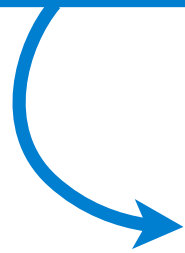
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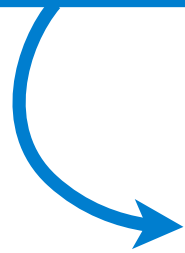
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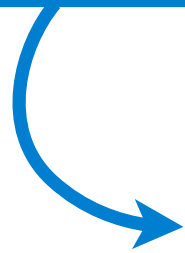
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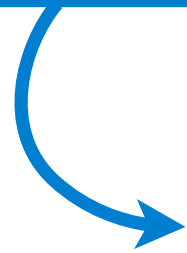
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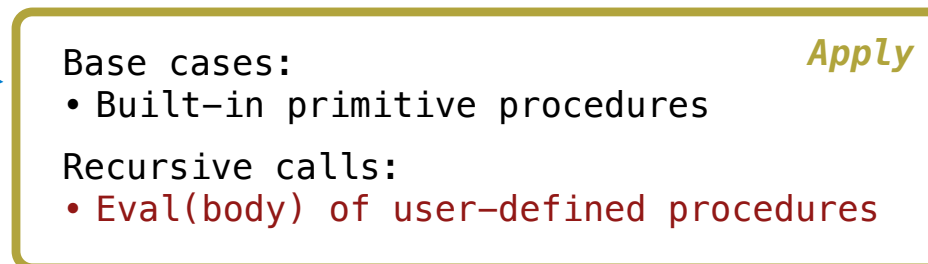
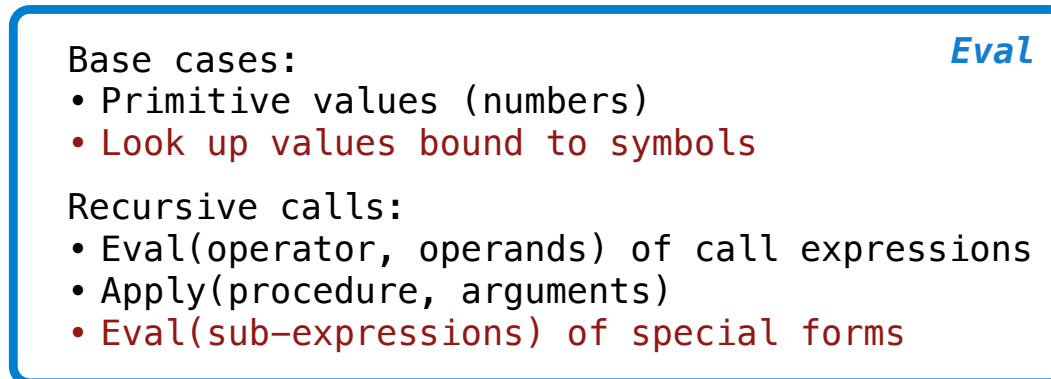


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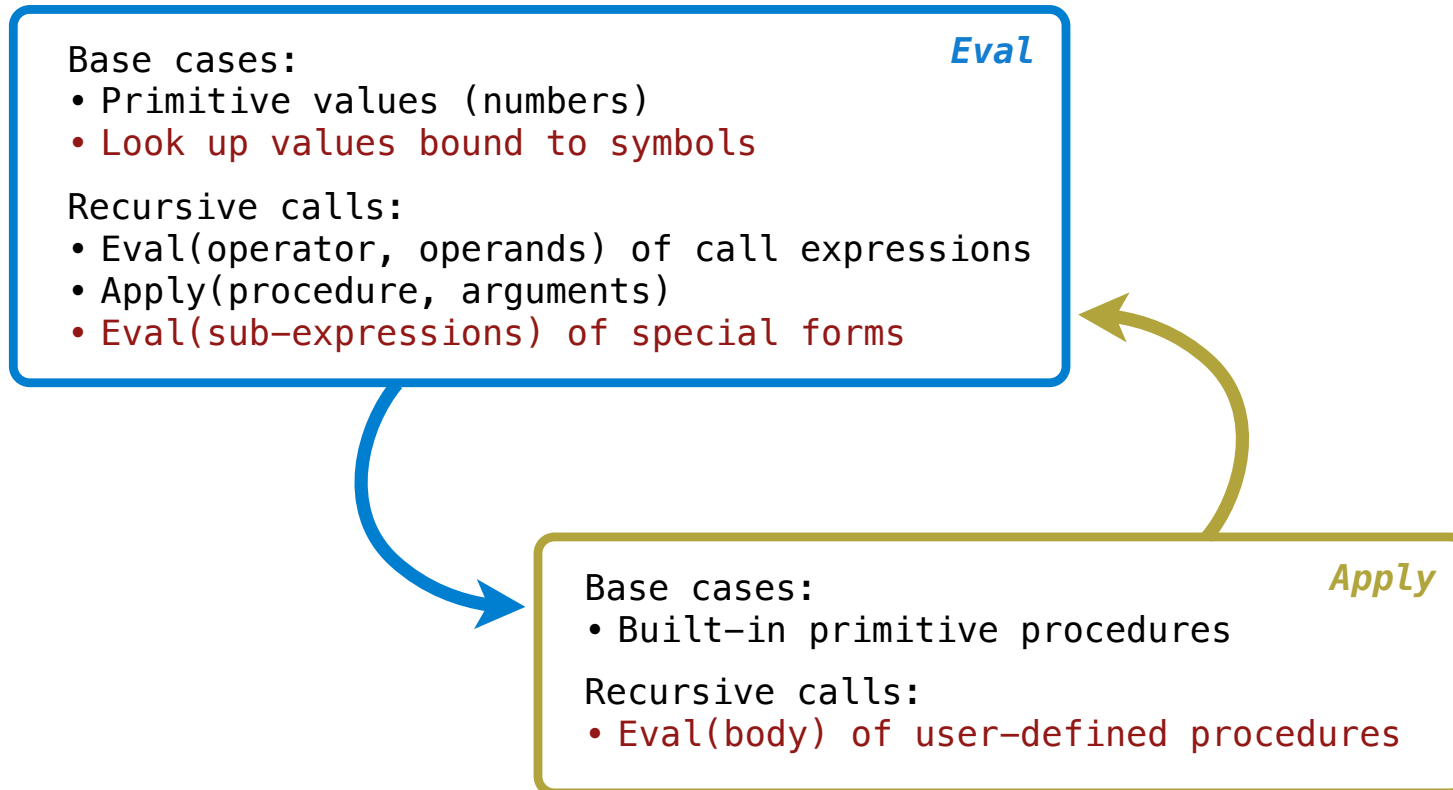
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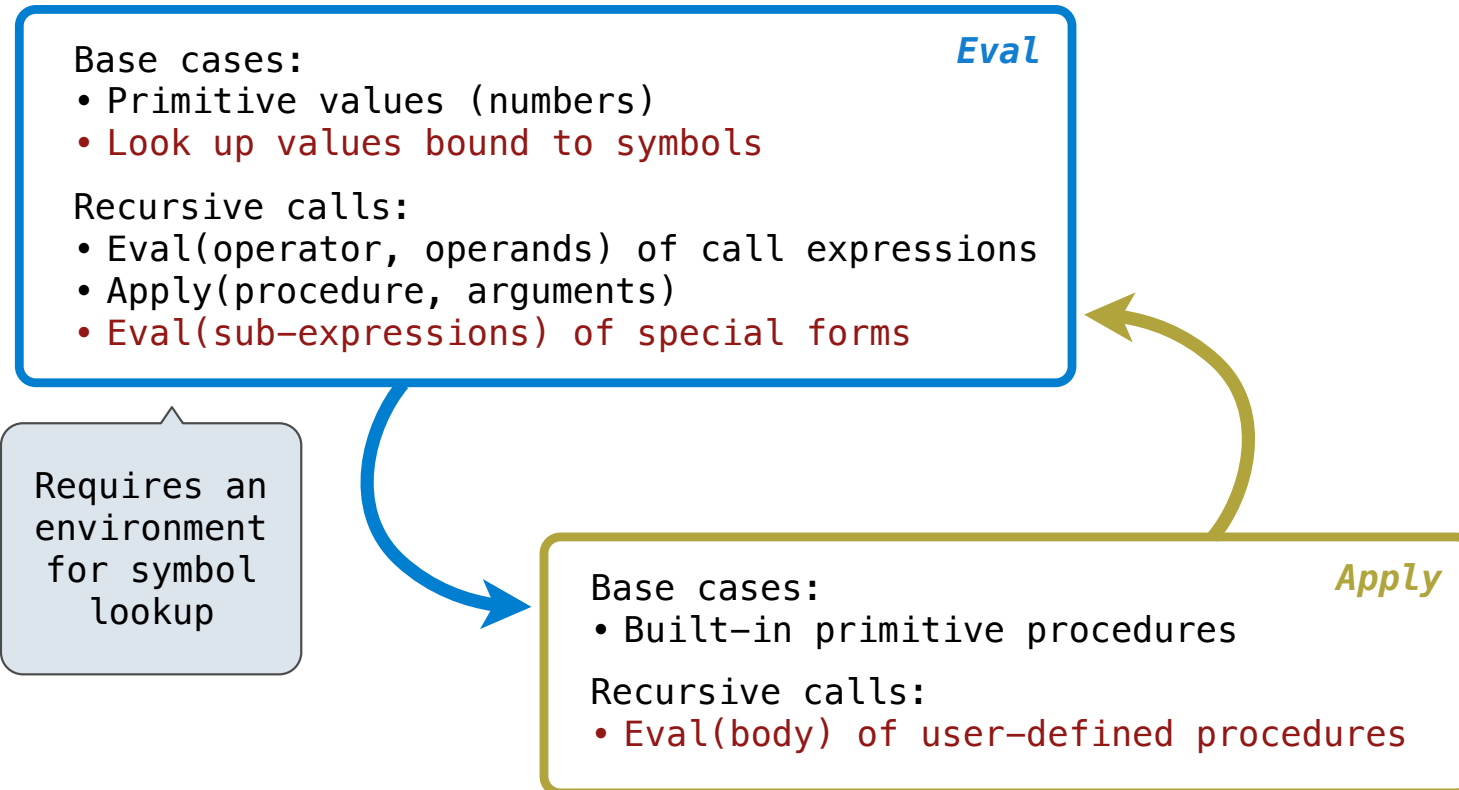
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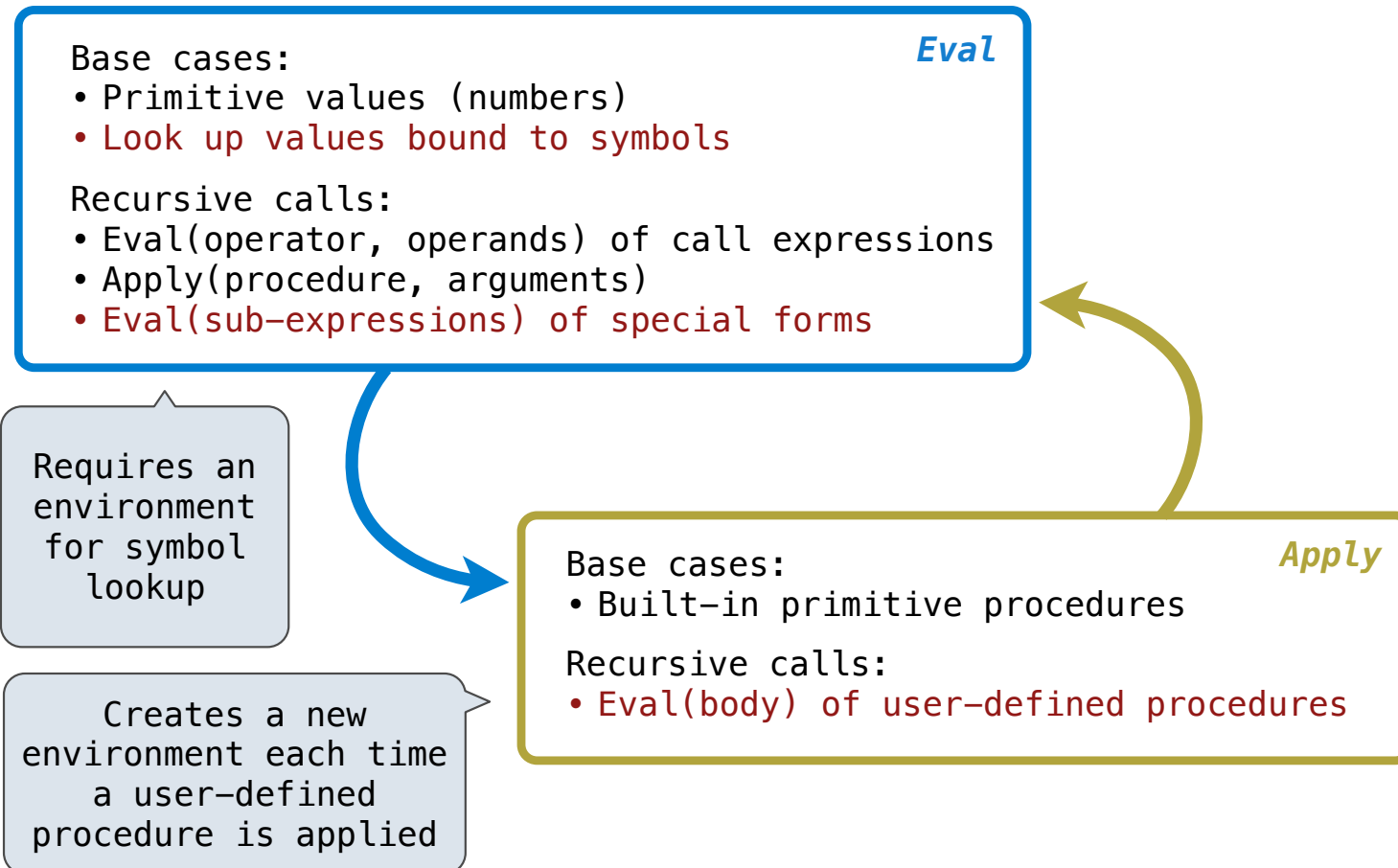
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Special Forms

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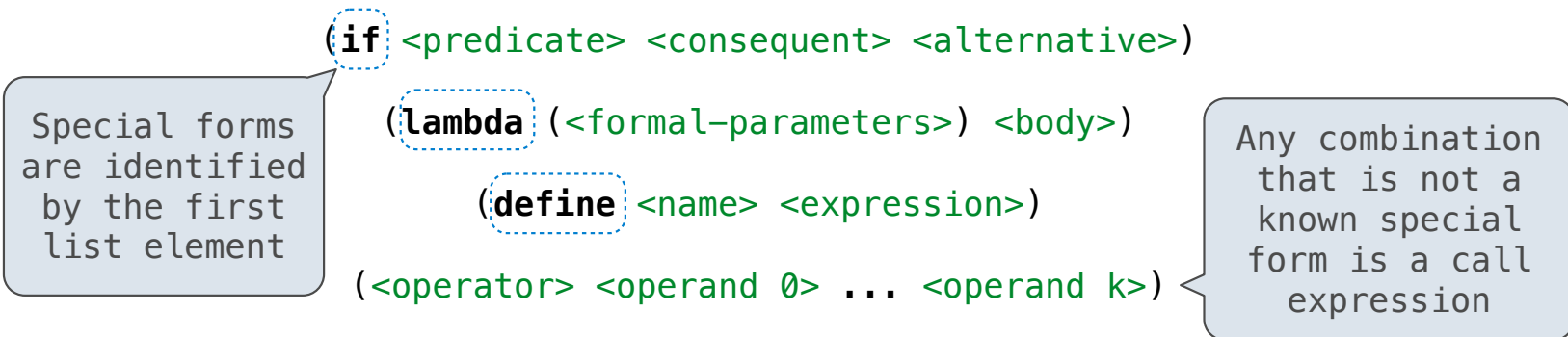
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Any combination that is not a known special form is a call expression

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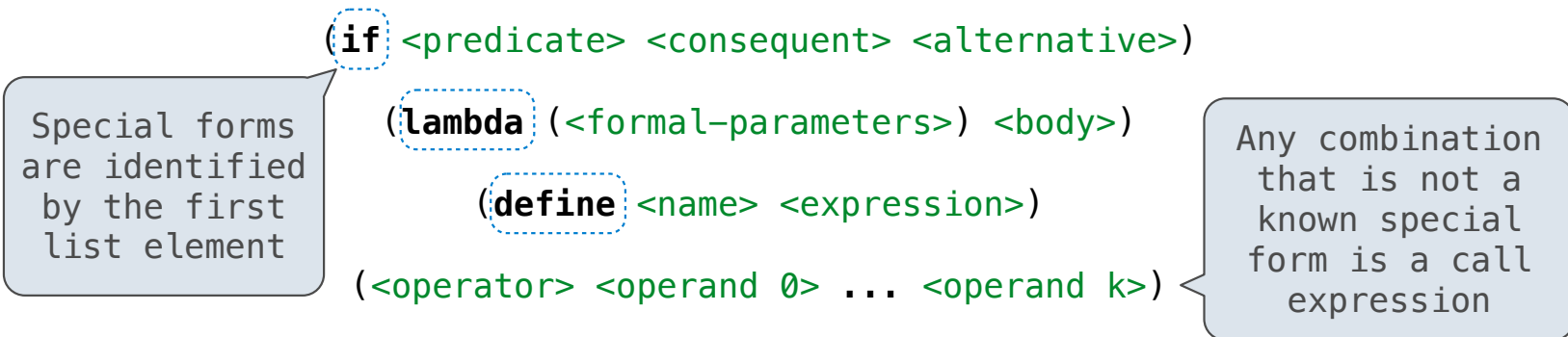


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(Demo)

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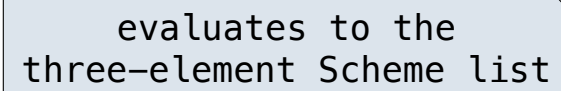
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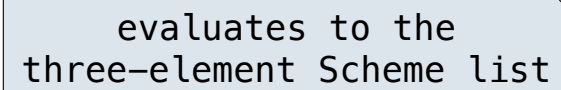
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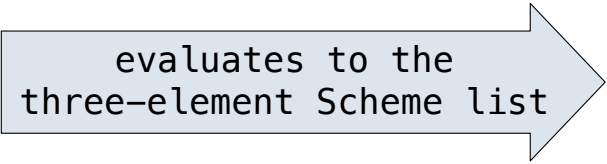
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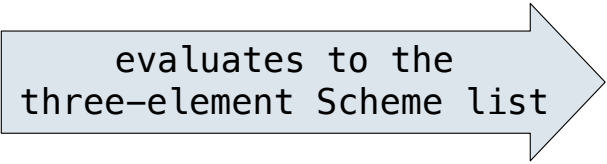
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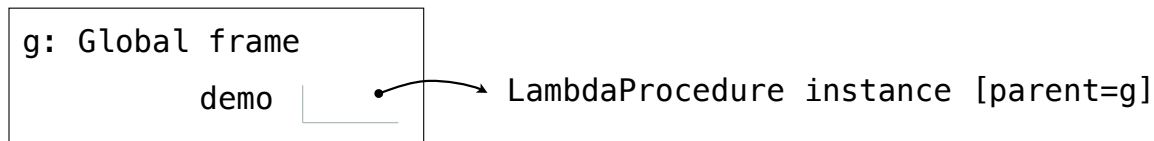
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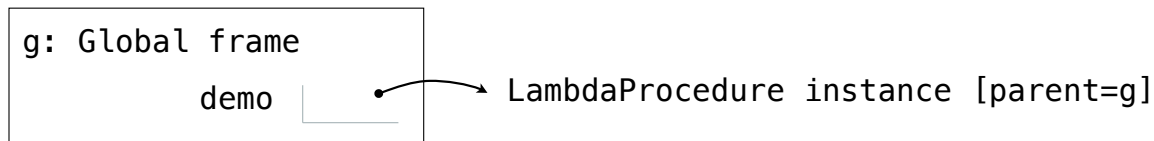


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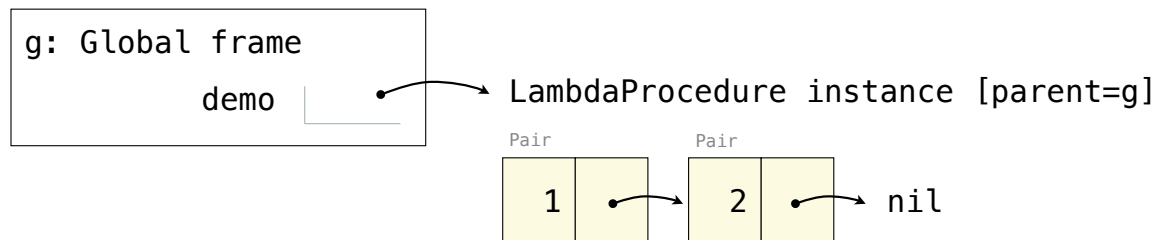


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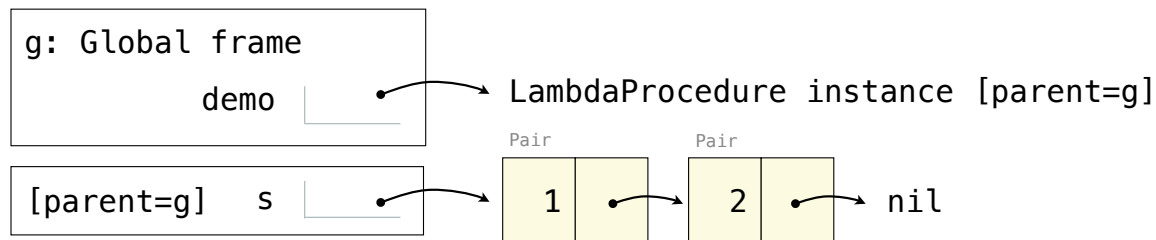


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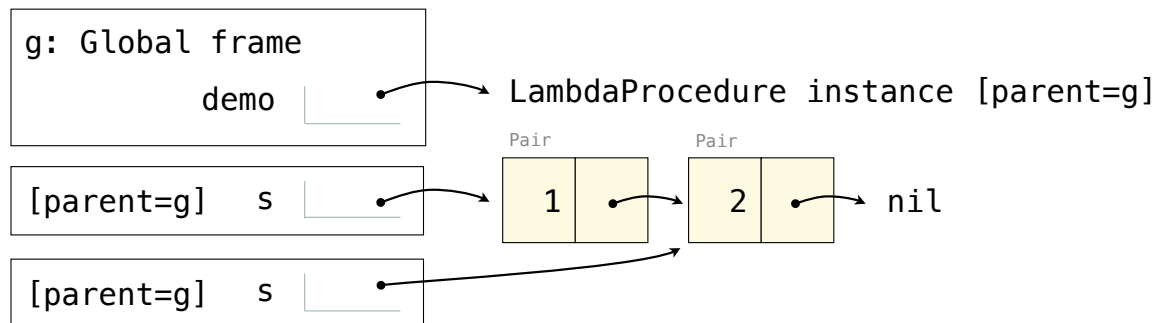


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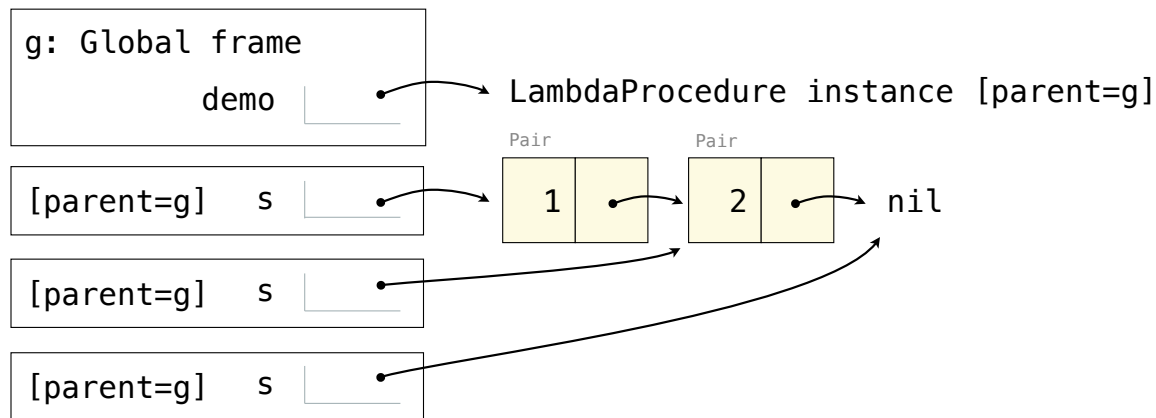


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```



Eval/Apply in Lisp 1.5

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```
apply[fn;x;a] =
  [atom[fn] → [eq[fn;CAR] → caar[x];
               eq[fn;CDR] → cdar[x];
               eq[fn;CONS] → cons[car[x];cadr[x]];
               eq[fn;ATOM] → atom[car[x]];
               eq[fn;EQ] → eq[car[x];cadr[x]];
               T → apply[eval[fn;a];x;a]];
  eq[car[fn];LAMBDA] → eval[caddr[fn];pairlis[cadr[fn];x;a]];
  eq[car[fn];LABEL] → apply[caddr[fn];x;cons[cons[cadr[fn];
                                                    caddr[fn]];a]]]

eval[e;a] = [atom[e] → cdr[assoc[e;a]];
            atom[car[e]] →
              [eq[car[e],QUOTE] → cadr[e];
               eq[car[e];COND] → evcon[cdr[e];a];
               T → apply[car[e];evlis[cdr[e];a];a]];
            T → apply[car[e];evlis[cdr[e];a];a]]
```