

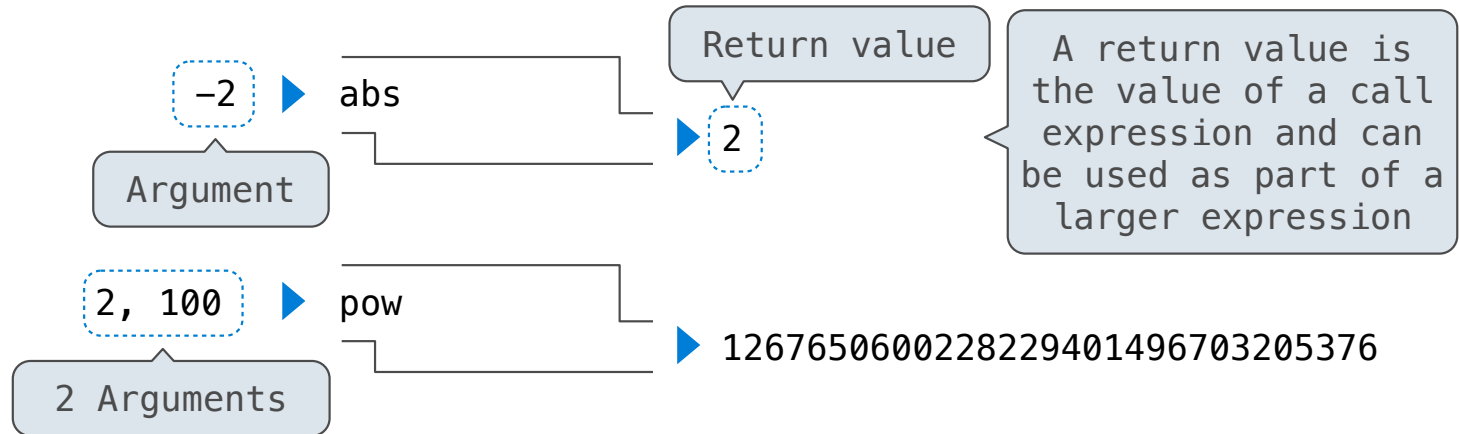
Control

Announcements

Print and None

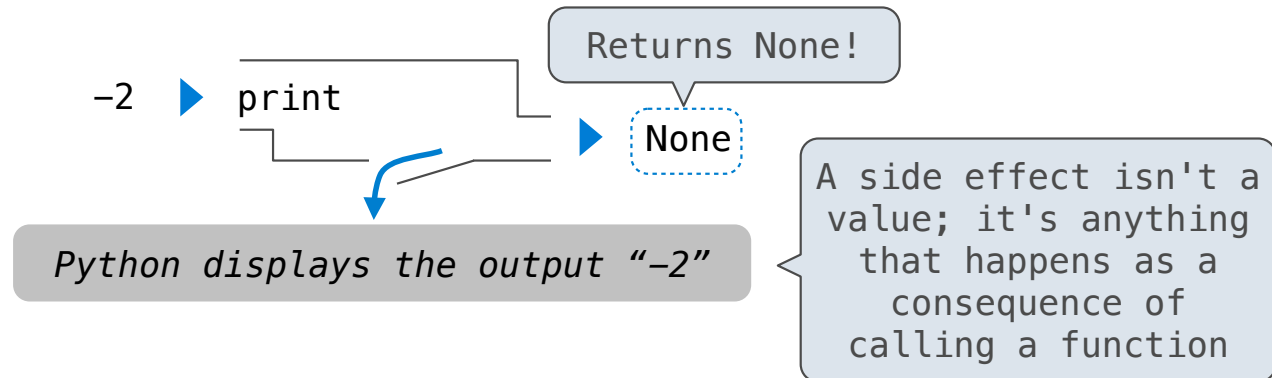
Pure Functions & Non-Pure Functions

Pure Functions
just return values



A return value is the value of a call expression and can be used as part of a larger expression

Non-Pure Functions
have side effects



A side effect isn't a value; it's anything that happens as a consequence of calling a function

Example: Print Then Return

Implement a function `h(x)` that first prints, then returns, the value of `f(x)`.

```
def h(x):  
    return print(f(x))
```

(A)

```
def h(x):  
    print(f(x))  
    return f(x)
```

(B)

```
def h(x):  
    y = f(x)  
    print(y)  
    return y
```

(C)

What's a function `f` for which implementations (B) and (C) would have different behavior?

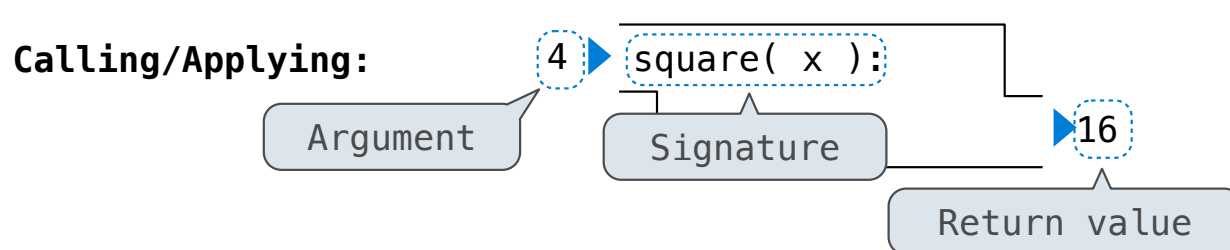
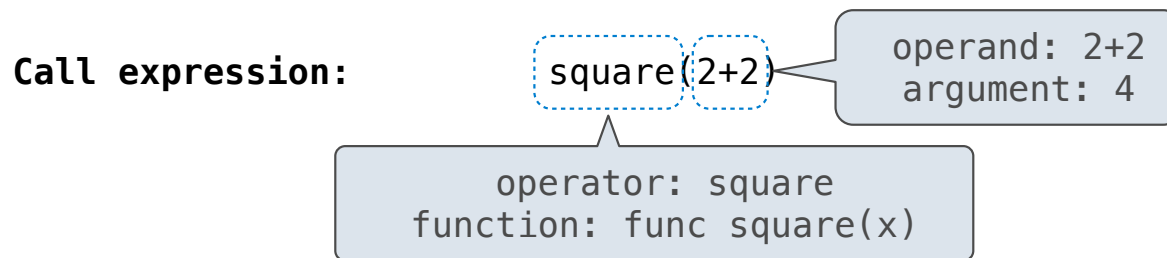
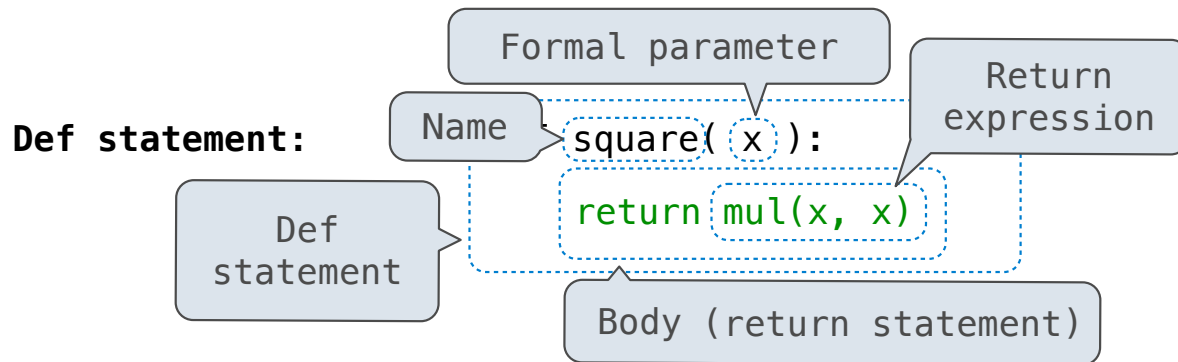
```
>>> h(2)  
...
```

```
>>> h(2)  
...
```

(Demo)

Multiple Environments

Life Cycle of a User-Defined Function



What happens?

A new function is created!

Name bound to that function
in the current frame

Operator & operands evaluated
Function (value of operator)
called on arguments
(values of operands)

A new frame is created!

Parameters bound to arguments

Body is executed in that new
environment

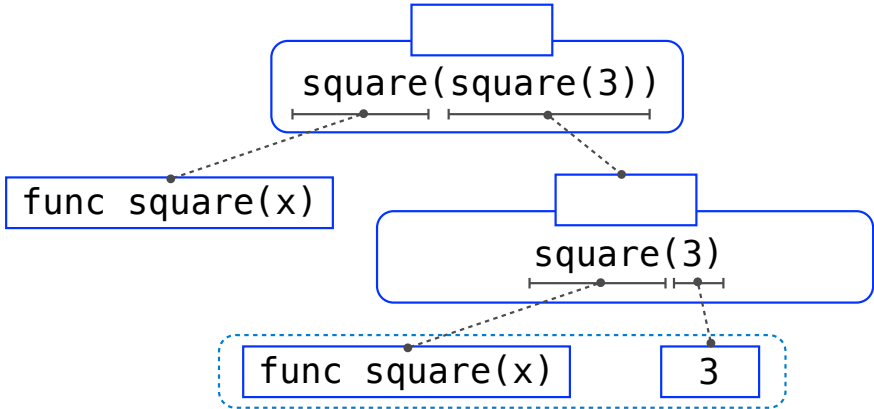
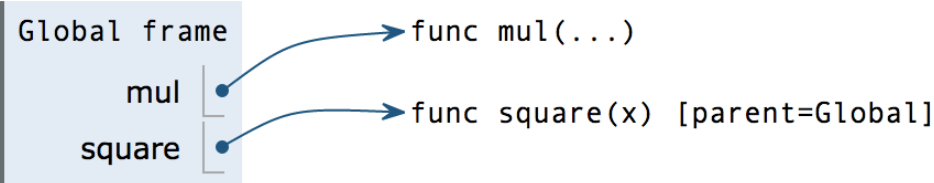
(Demo)

Multiple Environments in One Diagram!

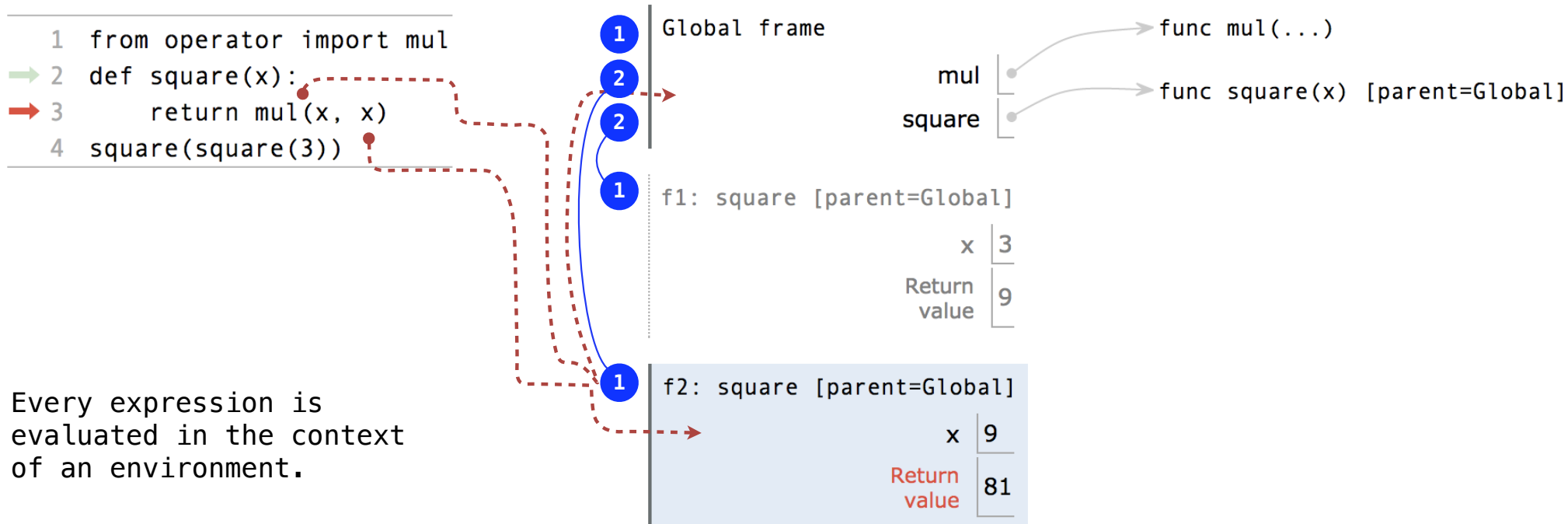
```

1 from operator import mul
→ 2 def square(x):
3     return mul(x, x)
→ 4 square(square(3))

```



Names Have No Meaning Without Environments



Every expression is evaluated in the context of an environment.

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

An environment is a sequence of frames.

- The global frame alone
- A local, then the global frame

Control

Conditional Statements

Conditional statements (often called "If" Statements) contain statements that may or may not be evaluated.

		x=10	x=1	x=-1
<pre>if x > 2: print('big') if x > 0: print('positive')</pre>	Two separate (unrelated) conditional statements	big positive	positive	
<pre>if x > 2: print('big') elif x > 0: print('positive')</pre>	One statement with two clauses: if and elif Only one body can ever be executed	big	positive	
<pre>if x > 2: print('big') elif x > 0: print('positive') else: print('not pos')</pre>	One statement with three clauses: if, elif, else Only one body can ever be executed	big	positive	not pos

While Statements

While statements contain statements that are repeated as long as some condition is true.

Important considerations:

- How many separate names are needed and what do they mean?
- The while condition must eventually become a false value for the statement to end (unless there is a return statement inside the while body).
- Once the while condition is evaluated, the entire body is executed.

Names and their initial values

```
1 i, total = 0, 0
```

```
2 while i < 3:
```

The while condition is evaluated before each iteration

A name that appears in the while condition is changing

```
    i = i + 1
```

```
    total = total + i
```

Executed even when i is set to 3

Example: Prime Factorization

Prime Factorization

Each positive integer n has a set of prime factors: primes whose product is n

...

$$8 = 2 * 2 * 2$$

$$9 = 3 * 3$$

$$10 = 2 * 5$$

$$11 = 11$$

$$12 = 2 * 2 * 3$$

...

One approach: Find the smallest prime factor of n , then divide by it

$$858 = 2 * 429 = 2 * 3 * 143 = 2 * 3 * 11 * 13$$

(Demo)