Trees

Announcements

Dictionaries

{'Dem': 0}

Dictionary Comprehensions

{<key exp>: <value exp> for <name> in <iter exp> if <filter exp>}

Short version: {<key exp>: <value exp> for <name> in <iter exp>}

Data Abstraction

Data Abstraction

A small set of functions enforce an abstraction barrier between *representation* and *use*

```
• How data are represented (as some underlying list, dictionary, etc.)
```

• How data are manipulated (as whole values with named parts)

E.g., refer to the parts of a line (affine function) called f:

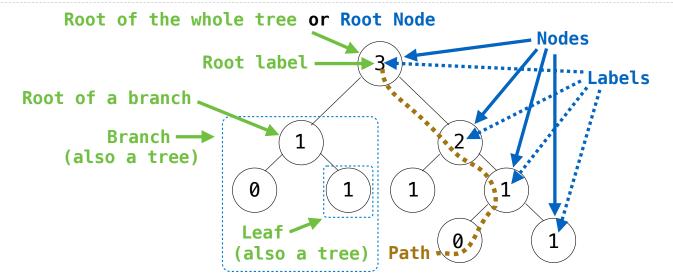
```
•slope(f) instead of f[0] or f['slope']
```

```
•y_intercept(f) instead of f[1] or f['y_intercept']
```

Why? Code becomes easier to read & revise

Trees

Tree Abstraction



Recursive description (wooden trees): A tree has a root label and a list of branches Each branch is a tree A tree with zero branches is called a leaf A tree starts at the root Relative description (family trees): Each location in a tree is called a node Each node has a label that can be any value One node can be the parent/child of another The top node is the root node

People often refer to labels by their locations: "each parent is the sum of its children"

Using the Tree Abstraction

For a tree t, you can only:

•Get the label for the root of the tree: label(t)

•Get the list of branches for the tree: branches(t)

•Determine whether the tree is a leaf: is_leaf(t)

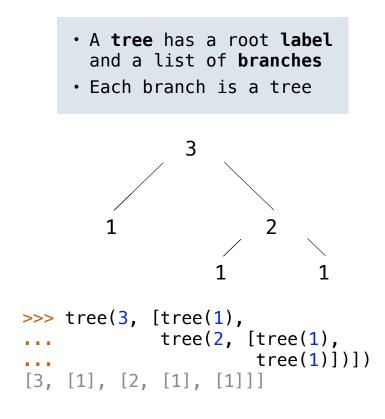
•Treat t as a value: return t, f(t), [t], s = t, etc.

Implementing the Tree Abstraction

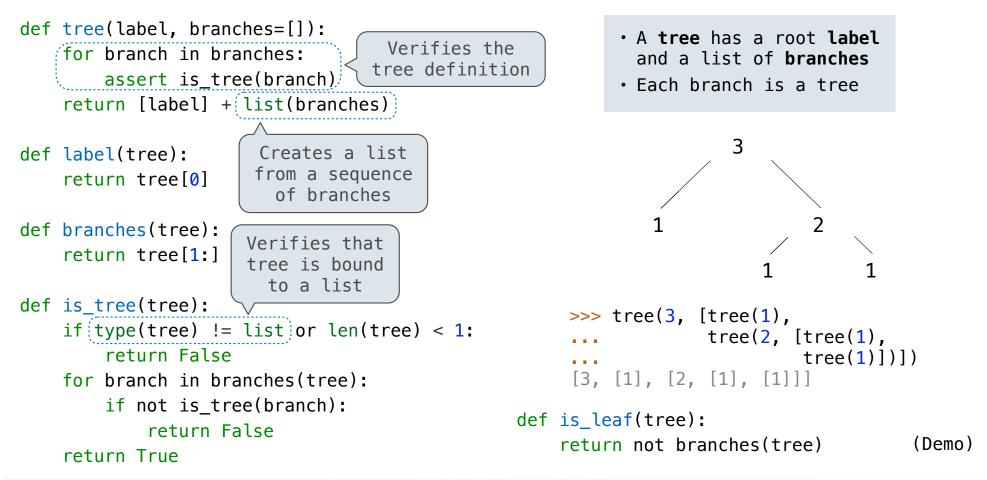
```
def tree(label, branches=[]):
    return [label] + branches

def label(tree):
    return tree[0]

def branches(tree):
    return tree[1:]
```



Implementing the Tree Abstraction



Tree Processing

Tree Processing Uses Recursion

```
Processing a leaf is often the base case of a tree processing function
```

The recursive case typically makes a recursive call on each branch, then aggregates

```
def count_leaves(t):
    """Count the leaves of a tree."""
    if is_leaf(t):
        return 1
    else:
        branch_counts = [count_leaves(b) for b in branches(t)]
        return sum(branch_counts)
```

Example: Summing Paths

Example: Counting Paths

Count Paths that have a Total Label Sum

