

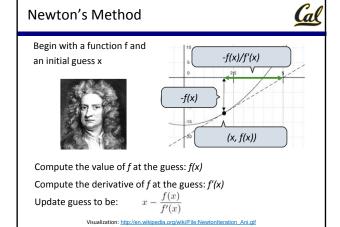
CS61A Lecture 8

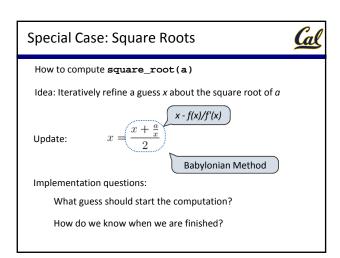
Amir Kamil UC Berkeley February 8, 2013

Announcements

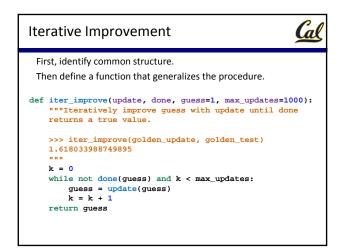


- ☐ HW3 out, due Tuesday at 7pm
- ☐ Midterm next Wednesday at 7pm
 - ☐ Keep an eye out for your assigned location
 - □ Old exams posted
 - □ Review sessions
 - Saturday 2-4pm in 2050 VLSB
 - Extended office hours Sunday 11-3pm in 310 Soda
 - HKN review session Sunday 3-6pm in 145 Dwinelle
- ☐ Environment diagram handout on website
- □ Code review system online
 - ☐ See Piazza post for details





Special Case: Cube Roots How to compute cube_root(a) Idea: Iteratively refine a guess x about the cube root of aUpdate: $x = \frac{2x + \frac{a}{x^2}}{3}$ Implementation questions: What guess should start the computation? How do we know when we are finished?



Newton's Method for nth Roots



Factorial



The factorial of a non-negative integer *n* is

$$n! = \begin{cases} 1, & n = 0 \text{ or } n = 1\\ n * ((n-1) * \cdots * 1) & n > 1 \end{cases}$$

$$(n-1)!$$

Factorial



The factorial of a non-negative integer *n* is

$$n! = \begin{cases} 1, & n = 0 \text{ or } n = 1\\ n * ((n-1)!) & n > 1 \end{cases}$$

This is called a recurrence relation;

Factorial is defined in terms of itself

Can we write code to compute factorial using the same pattern?

Computing Factorial



We can compute factorial using the direct definition

$$n! = \begin{cases} 1, & n = 0 \text{ or } n = 1\\ n*(n-1)*\cdots*1, & n > 1 \end{cases}$$

$$\text{def factorial(n):} \\ \text{if n = 0 or n == 1:} \\ \text{return 1} \\ \text{total = 1} \\ \text{while n >= 1:} \\ \text{total, n = total * n, n - 1} \\ \text{return total} \end{cases}$$

Computing Factorial



Can we compute it using the recurrence relation?

$$n! = \begin{cases} 1, & n = 0 \text{ or } n = 1\\ n * (n-1)! & n > 1 \end{cases}$$

$$\text{def factorial(n):}$$

$$\text{if n == 0 or n == 1:}$$

$$\text{return 1}$$

$$\text{return n * (factorial(n-1))}$$

This is much shorter! But can a function call itself?

Cal Factorial Environment Diagram Let's see what happens! factorial factorial Compute 4! def factorial(n): if n == 0 or n == 1: return 1 return n * factorial(n - 1) factorial Compute 3! ___6 factorial(4) factorial Compute 2! factorial Compute 1! Example: http://goo.gl/NiCKG

Recursive Functions A function is recursive if the body calls the function itself, either directly or indirectly Recursive functions have two important components: 1. Base case(s), where the function directly computes an answer without calling itself 2. Recursive case(s), where the function calls itself as part of the computation def factorial(n): if n == 0 or n == 1: return 1 Recursive

return n * factorial(n - 1)

```
Cal
Practical Guidance: Choosing Names
 Names typically don't matter for correctness,
 but they matter tremendously for legibility
 boolean 📥 turn_is_over
                         d 📦 dice
                                      play_helper 📥 take_turn
 Use names for repeated compound expressions
 if sqrt(square(a) + square(b)) > 1:
     x = x + sqrt(square(a) + square(b))
                        h = sqrt(square(a) + square(b))
                            if h > 1:
                               x = x + h
 Use names for meaningful parts of compound expressions
   x = (-b + sqrt(square(b) - 4 * a * c)) / (2 * a)
   disc_term = sqrt(square(b) - 4 * a * c)
   x = (-b + disc_term) / (2 * a)
```

```
Sometimes, removing repetition requires restructuring the code

def find_quadratic_root(a, b, c, plus=True):

"""Applies the quadratic formula to the polynomial

ax^2 + bx + c."""

if plus:

return (-b + sqrt(square(b) - 4 * a * c)) / (2 * a)

else:

return (-b - sqrt(square(b) - 4 * a * c)) / (2 * a)

def find_quadratic_root(a, b, c, plus=True):

"""Applies the quadratic formula to the polynomial

ax^2 + bx + c."""

disc_term = sqrt(square(b) - 4 * a * c)

if not plus:

disc_term *= -1

return (-b + disc_term) / (2 * a)
```

Test-Driven Development



Write the test of a function before you write a function

A test will clarify the (one) job of the function Your tests can help identify tricky edge cases

Develop incrementally and test each piece before moving on

You can't depend upon code that hasn't been tested Run your old tests again after you make new changes