

CS61A Lecture 17

Amir Kamil
UC Berkeley
March 1, 2013

Announcements



- HW6 due next Thursday

- Trends project due on Tuesday
 - Partners are required; find one in lab or on Piazza
 - Will not work in IDLE
 - New bug submission policy; see Piazza

Practical Guidance: Choosing Names



Names typically don't matter for correctness,
but they matter tremendously for legibility

boolean → turn_is_over d → dice play_helper → take_turn

Use names for repeated compound expressions

```
if sqrt(square(a) + square(b)) > 1:
    x = x + sqrt(square(a) + square(b))
    ↓
    h = sqrt(square(a) + square(b))
    if h > 1:
        x = x + h
```

Use names for meaningful parts of compound expressions

```
x = (-b + sqrt(square(b) - 4 * a * c)) / (2 * a)
    ↓
disc_term = sqrt(square(b) - 4 * a * c)
x = (-b + disc_term) / (2 * a)
```

Practical Guidance: DRY



Sometimes, removing repetition requires restructuring the code

```
def find_quadratic_root(a, b, c, plus=True):
    """Applies the quadratic formula to the polynomial
    ax^2 + bx + c."""
    if plus:
        return (-b + sqrt(square(b) - 4 * a * c)) / (2 * a)
    else:
        return (-b - sqrt(square(b) - 4 * a * c)) / (2 * a)
```



```
def find_quadratic_root(a, b, c, plus=True):
    """Applies the quadratic formula to the polynomial
    ax^2 + bx + c."""
    disc_term = sqrt(square(b) - 4 * a * c)
    if not plus:
        disc_term *= -1
    return (-b + disc_term) / (2 * a)
```

Test-Driven Development



Write the test of a function before you write a
function

A test will clarify the (one) job of the function
Your tests can help identify tricky edge cases

Develop incrementally and test each piece before
moving on

You can't depend upon code that hasn't been tested
Run your old tests again after you make new changes

Hog Contest



Contest rules:

- All entries run against every other entry
- An entry wins a match if its true win rate is > 0.5
- All strategies must be deterministic, pure functions and
must not use pre-computed data
- Extra credit for entries with the most wins or the highest
cumulative win rate
- Total of 54 valid submissions

We used `itertools.combinations` to determine
the set of matches

Top Finishers



Congratulations to the team of Colin Lockard and Sherry Xu, who achieved a perfect 53-0 record and the highest win rate (28.77)!

Second-most wins (51-2): Eric Holt and Anna Carey

Second-highest win rate (28.70): Don Mai and Jeechee Chen

Third-highest in both (50-3, 28.67): Sean Scofield and Frank Lu

Complete rankings will be posted on the website

Computing Win Rates Exactly



A state in the game:
(who rolls next?, player score, opponent score)

A strategy is a table

```
(me,0,0): 5
(me,0,70): 9
...
(me,96,99): 0
...
(me,99,99): 10
```

Each state has a chance to win

When rolling 2 dice:
 $1/36 * 1 + 35/36 * 0$
 ...
 (me,87,99)
 ...
 (you,88,99) 0
 (you,90,99) 0
 ...
 (you,98,99) 0
 (you,100+,99) 1
 (me,99,100+) 0

Requires access to both strategies, which must be deterministic

Achieving the Perfect Strategy



Optimal strategy given an opponent:

- At each state, compute probability of winning for each allowed number of dice
- Choose the number of dice that maximizes the probability

The perfect strategy: use iterative improvement!

- Initial guess: always roll 5
- Update to: optimal opponent of current strategy
- Done when: 0.5 win rate against optimal opponent

Takes only 16 steps to converge!

Can also compute perfect strategy directly using table

A Function with Evolving Behavior



Let's model a bank account that has a balance of \$100

Return value:
remaining balance

```
>>> withdraw(25)
75
```

Argument:
amount to withdraw

Different
return value!

```
>>> withdraw(25)
50
```

Second withdrawal
of the same amount

```
>>> withdraw(60)
'Insufficient funds'
```

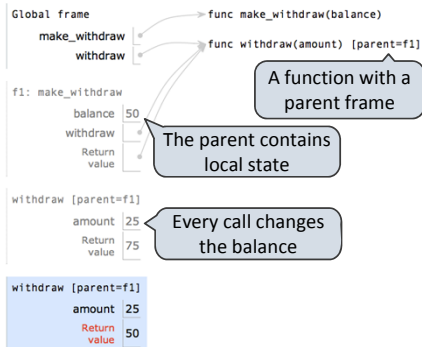
Where's this
balance stored?

```
>>> withdraw(15)
35
```

```
>>> withdraw = make_withdraw(100)
```

Within the
function!

Persistent Local State



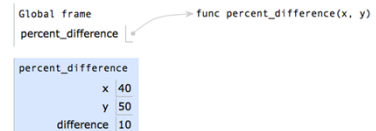
Example: <http://goo.gl/5LZ6F>

Reminder: Local Assignment



```
def percent_difference(x, y):
    difference = abs(x-y)
    return 100 * difference / x
diff = percent_difference(40, 50)
```

Assignment binds name(s) to value(s) in the first frame of the current environment



Execution rule for assignment statements:

- Evaluate all expressions right of =, from left to right.
- Bind the names on the left the resulting values in the first frame of the current environment.

Example: <http://goo.gl/xkYnN>

Non-Local Assignment

```
def make_withdraw(balance):
    """Return a withdraw function with a starting balance."""
    def withdraw(amount):
        nonlocal balance
        if amount > balance:
            return 'Insufficient funds'
        balance = balance - amount
        return balance
    return withdraw
```

Declare the name "balance" nonlocal

Re-bind balance where it was bound previously

The Effect of Nonlocal Statements

```
nonlocal <name>, <name 2>, ...
```

Effect: Future assignments to that name change its pre-existing binding in the **first non-local frame** of the current environment in which that name is bound.

Python Docs: an "enclosing scope"

From the Python 3 language reference:

Names listed in a [nonlocal](#) statement must refer to pre-existing bindings in an enclosing scope. Names listed in a nonlocal [statement](#) must not collide with pre-existing bindings in the local scope.

http://docs.python.org/release/3.3.3/reference/simple_stmts.html#the-nonlocal-statement
<http://www.python.org/dev/peps/pep-3104/>

Effects of Assignment Statements

Status	Effect
<ul style="list-style-type: none"> No nonlocal statement "x" is not bound locally 	Create a new binding from name "x" to object 2 in the first frame of the current environment.
<ul style="list-style-type: none"> No nonlocal statement "x" is bound locally 	Re-bind name "x" to object 2 in the first frame of the current env.
<ul style="list-style-type: none"> nonlocal x "x" is bound in a non-local frame 	Re-bind "x" to 2 in the first non-local frame of the current environment in which it is bound.
<ul style="list-style-type: none"> nonlocal x "x" is not bound in a non-local frame 	SyntaxError: no binding for nonlocal 'x' found
<ul style="list-style-type: none"> nonlocal x "x" is not bound in a non-local frame "x" also bound locally 	SyntaxError: name 'x' is parameter and nonlocal

`x = 2`

Python Particulars

Python pre-computes which frame contains each name before executing the body of a function.

Therefore, within the body of a function, all instances of a name must refer to the same frame.

```
def make_withdraw(balance):
    def withdraw(amount):
        if amount > balance:
            return 'Insufficient funds'
        balance = balance - amount
        return balance
    return withdraw

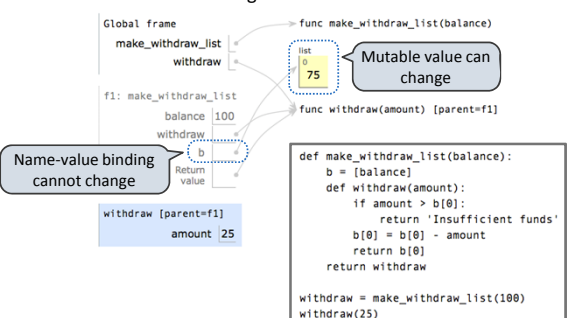
wd = make_withdraw(20)
wd(5)
```

Local assignment

UnboundLocalError: local variable 'balance' referenced before assignment

Mutable Values and Persistent State

Mutable values can be changed without a nonlocal statement.

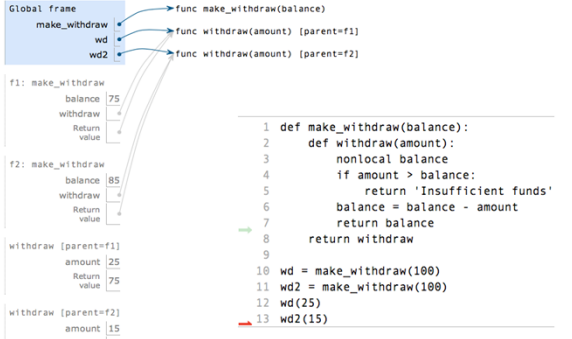


```
def make_withdraw_list(balance):
    b = [balance]
    def withdraw(amount):
        if amount > b[0]:
            return 'Insufficient funds'
        return b[0] - amount
    return b[0]
    return withdraw

withdraw = make_withdraw_list(100)
withdraw(25)
```

Example: <http://goo.gl/CEpmz>

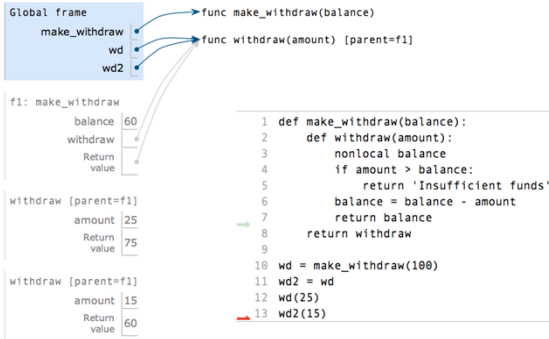
Creating Two Withdraw Functions



```
1 def make_withdraw(balance):
2   def withdraw(amount):
3     nonlocal balance
4     if amount > balance:
5       return 'Insufficient funds'
6     balance = balance - amount
7     return balance
8   return withdraw
9
10 wd = make_withdraw(100)
11 wd2 = make_withdraw(100)
12 wd(25)
13 wd2(15)
```

Example: <http://goo.gl/gITvB>

Multiple References to a Withdraw Function



Example: <http://goo.gl/X2aG9>

The Benefits of Non-Local Assignment



- Ability to maintain some state that is local to a function, but evolves over successive calls to that function.
- The binding for balance in the first non-local frame of the environment associated with an instance of withdraw is inaccessible to the rest of the program.
- An abstraction of a bank account that manages its own internal state.

Weasley Account
\$10

Potter Account
\$1,000,000

Referential Transparency



Expressions are referentially transparent if substituting an expression with its value does not change the meaning of a program.



```

mul(add(2, mul(4, 6)), 3)
mul(add(2, 24), 3)
mul(26, 3)
    
```



Mutation is a *side effect* (like printing)

Side effects violate the condition of referential transparency because they do more than just return a value; they change the state of the computer.