

CS61A Lecture 31

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Announcements



- HW9 due tonight

- Ants extra credit due tonight
 - See Piazza for submission instructions

- Hog revisions out, due Monday

- HW10 out tonight

Scheme has built-in pairs that use weird names:

- **cons:** Two-argument procedure that **creates a pair**
- **car:** Procedure that returns the **first element** of a pair
- **cdr:** Procedure that returns the **second element** of a pair

A pair is represented by a dot between the elements, enclosed in parentheses

```
> (cons 1 2)
(1 . 2)
> (car (cons 1 2))
1
> (cdr (cons 1 2))
2
```

Recursive Lists



A recursive list can be represented as a pair in which the second element is a recursive list or the empty list

Scheme lists are recursive lists:

- **nil** is the empty list
- A non-empty Scheme list is a pair in which the second element is **nil** or a Scheme list

Scheme lists are written as space-separated combinations

```
> (define x (cons 1 (cons 2 (cons 3 (cons 4 nil)))))  
> x  
(1 2 3 4)  
> (cdr x)  
(2 3 4)  
> (cons 1 (cons 2 (cons 3 4)))  
(1 2 3 . 4)
```

Not a well-formed list!

Symbols are normally evaluated to produce values; how do we refer to symbols?

```
> (define a 1)
> (define b 2)
> (list a b)
(1 2)
```

No sign of “a” and “b” in the resulting value

Quotation prevents something from being evaluated by Lisp

```
> (list 'a 'b)
(a b)
> (list 'a b)
(a 2)
```

Symbols are now values

Quotation can also be applied to combinations to form lists

```
> (car '(a b c))
a
> (cdr '(a b c))
(b c)
```

Scheme Lists and Quotation



Dots can be used in a quoted list to specify the second element of the final pair

```
> (cdr (cdr '(1 2 . 3)))  
3
```

However, dots appear in the output only of ill-formed lists

```
> '(1 2 . 3)           1 | • → 2 | 3  
(1 2 . 3)  
> '(1 2 . (3 4))      1 | • → 2 | • → 3 | • → 4 | • → nil  
(1 2 3 4)  
> '(1 2 3 . nil)      1 | • → 2 | • → 3 | • → nil  
(1 2 3)
```

What is the printed result of evaluating this expression?

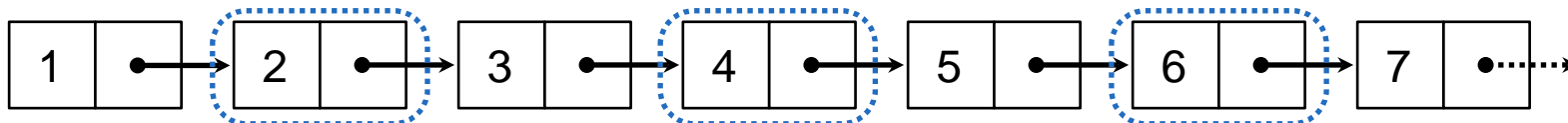
```
> (cdr '((1 2) . (3 4 . (5))))  
(3 4 5)
```

The Let Special Form



Let expressions introduce a new frame, with the given bindings

```
(let ((<name> <exp>) ... ) <body>)
```



```
(define (filter fn s)
  (if (null? s)
      s
      (let ((first (car s))
            (rest (filter fn (cdr s))))
        (if (fn first)
            (cons first rest)
            rest))))
```

```
> (filter even? '(1 2 3 4 5 6 7))
(2 4 6)
```

Quick Sort

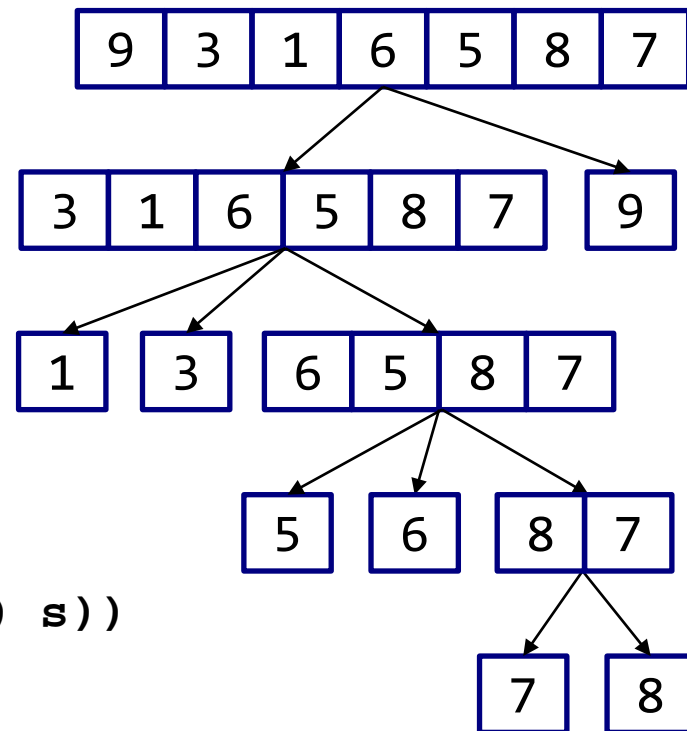


Quick sort algorithm:

1. Choose a pivot (e.g. first element)
2. Partition into three pieces:
< pivot, = pivot, > pivot
3. Recurse on first and last piece

```
(define (filter-comp comp pivot s)
  (filter (lambda (x) (comp x pivot)) s))
```

```
(define (quick-sort s)
  (if (<= (length s) 1)
      s
      (let ((pivot (car s)))
        (append (quick-sort (filter-comp < pivot s))
                  (filter-comp = pivot s)
                  (quick-sort (filter-comp > pivot s))))))
```



The Begin Special Form



Begin expressions allow sequencing

```
(begin <exp1> <exp2> ... <expn>)
```

```
(define (repeat k fn)
```

```
  (if (> k 0)
```

```
      (begin (fn) (repeat (- k 1) fn))
```

```
      'done))
```

```
(define (tri fn)
```

```
  (repeat 3 (lambda () (fn) (lt 120))))
```

```
(define (sier d k)
```

```
  (tri (lambda () (if (= k 1) (fd d) (leg d k)))))
```

```
(define (leg d k)
```

```
  (sier (/ d 2) (- k 1)) (penup) (fd d) (pendown))
```