

1 Learning Goals

- Get exam-level practice with various topics covered thus far

2 Recursion! Take the leap!

”Plaudite, amici, comedia finita est” (Applaud, my friends, the comedy is over).—
Beethoven [Said on his deathbed]

This quote is not really relevant to the question, but I (Murtz) found it amusing, even though I did not write the question. Let us write a symphony!

Assume you are given a function, `judge`, that takes in a list and returns a real number. The list is a representation of a symphony and the number is how good the symphony is. Given this function, use tree recursion to write a function that generates the best symphony of a predetermined length.

```
def best_symphony(symphony_so_far, possible_notes, length):
    2.1     if length == len(symphony_so_far):
            return symphony_so_far

    symphonies = []

    for next_note in possible_notes:
        symphony = best_symphony(symphony_so_far + [next_note], possible_notes, length)
        symphonies += [(symphony, judge(symphony))]

    return max(symphonies, key=lambda v: v[1])[0]
```

3 Iterators/Generators! Linked Lists! Trees! Next! Yield! Woohoo!

3.1 To make the Link class iterable, implement the LinkIterator class.

```
class Link:
    empty = ()
    def __init__(self, first, rest=empty):
        self.first = first
        self.rest = rest
    def __iter__(self):
        return LinkIterator(self)
```

```
class LinkIterator:
    def __init__(self, link):

        self.link = link

    def __iter__(self):

        return self

    def __next__(self):

        if self.link is Link.empty:
            raise StopIteration
        val = self.link.first
        self.link = self.link.rest
        return val
```

4 Review!

- 3.2 Implement `sum_paths_gen`, which takes in a tree `t` and returns a generator which yields the sum of all the nodes from a path from the root of a tree to a leaf.

You may yield the sums in any order.

```
def sum_paths_gen(t):  
    """  
    >>> t1 = tree(5)  
    >>> next(sum_paths_gen(t1))  
    5  
    >>> t2 = tree(1, [tree(2, [tree(3), tree(4)]), tree(9)])  
    >>> sorted(sum_paths_gen(t2))  
    [6, 7, 10]  
    """
```

```
if _____:  
  
    yield _____  
  
for _____:  
  
    for _____:  
  
        yield _____
```

```
def sum_paths_gen(t):  
    if is_leaf(t):  
        yield label(t)  
    for b in branches(t):  
        for s in sum_paths_gen(b):  
            yield s + label(t)
```

- 3.3 Implement `long_paths`, which returns a list of all *paths* in a tree with length at least `n`. A path in a tree is a linked list of node values that starts with the root and ends at a leaf. Each subsequent element must be from a child of the previous value's node. The *length* of a path is the number of edges in the path (i.e. one less than the number of nodes in the path). Paths are listed in order from left to right. See the doctests for some examples.

```
def long_paths(tree, n):
    """Return a list of all paths in tree with length at least n.
```

```
>>> t = Tree(3, [Tree(4), Tree(4), Tree(5)])
>>> left = Tree(1, [Tree(2), t])
>>> mid = Tree(6, [Tree(7, [Tree(8)]), Tree(9)])
>>> right = Tree(11, [Tree(12, [Tree(13, [Tree(14)])])])
>>> whole = Tree(0, [left, Tree(13), mid, right])
>>> for path in long_paths(whole, 2):
...     print(path)
...
<0 1 2>
<0 1 3 4>
<0 1 3 4>
<0 1 3 5>
<0 6 7 8>
<0 6 9>
<0 11 12 13 14>
>>> for path in long_paths(whole, 3):
...     print(path)
...
<0 1 3 4>
<0 1 3 4>
<0 1 3 5>
<0 6 7 8>
<0 11 12 13 14>
>>> long_paths(whole, 4)
[Link(0, Link(11, Link(12, Link(13, Link(14)))))]
"""
```

```
paths = []
if n <= 0 and tree.is_leaf():
    paths.append(Link(tree.label))
for b in tree.branches:
    for path in long_paths(b, n - 1):
        paths.append(Link(tree.label, path))
return paths
```

4 Scheme! Languages! Parentheses!

4.1 [Fall 2020 Final, Question 5](#)

[Fall 2020 Final, Question 5 Solution](#)