# Mutability

Announcements

(Demo)

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  - Special syntax that can improve the composition of programs
- In Python, every value is an object
  - All objects have attributes
  - A lot of data manipulation happens through object methods
  - Functions do one thing; objects do many related things

# Example: Strings

(Demo)

### American Standard Code for Information Interchange

	0	1	2	3	4	<sub> </sub> 5	6	7	8	9	Α	В	C	D	E	F
0	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	HT	LF	VT	FF	CR	S0	SI
1	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
2		!	н	#	\$	%	Ś	I	(	)	*	+	,	-	•	/
3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	^	?
4	0	Α	В	С	D	E	F	G	Н	I	J	K	L	Μ	Ν	0
5	Р	Q	R	S	Т	U	V	W	X	Y	Z	]	\	]	^	-
6	`	а	b	с	d	e	f	g	h	i	j	k	ι	m	n	0
7	р	q	r	s	t	u	v	W	х	у	z	{		}	~	DEL

ASCII Code Chart

### **ASCII Code Chart** 1 | 2 | 3 | 4 | 5 6 8 | 9 0 7 AIBICIDIEIF 0 NUL SOH STX ETX EOT ENQ ACK BEL BS ΗT LF VT | FF CR **S**0 SI bits DLE DC1 DC2 DC3 DC4 NAK SYN ETB CAN EM SUB ESC FS GS RS US # \$ % & / 2 1 н . ( ) \* + , -• 2 3 4 5 7 9 ; ? 0 1 6 8 : < = > 3 $\infty$ rows: Ε F Ι @ Α В С D G Н J Κ L М Ν 0 5 Ρ Q R S Т U V W Х Υ Ζ [ ١ ] \_ ^ b d f g i j k 6 а С е h ι m n ο $\infty$ q Х у DEL v z р r s t u W ł ł ~

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			0	1	2	3	4	l 2	6	7	8	9	Α	В	C	D	E	F
000	I	0	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	HT	Ŀ	VT	FF	CR	S0	SI
001	ts	1	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
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101	rows	5	Ρ	Q	R	S	Т	U	V	W	Х	Y	Z	[	\	]	~	-
1 1 0		6	,	а	b	с	d	е	f	g	h	i	j	k	ĩ	m	n	0
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ASCII Code Chart

### **ASCII Code Chart** 1 1 2 3 4 5 6 I 7 8 | 9 AIBICIDIEIF 0 0 NUL SOH STX ETX EOT ENQ ACK BEL 000 BS ΗT LF VT | FF CR **S**0 SI bits 1 DLE DC1 DC2 DC3 DC4 NAK SYN ETB CAN 001 EM SUB ESC FS GS RS US 0 1 0 % 2 # \$ & / 1 н . ( ) \* + , -• 3 0 5 ; ? 0 1 1 1 2 3 4 6 7 8 9 : < ω = > rows: 100 4 @ Α В С D Ε F G Н Ι J Κ М Ν 0 L P 101 5 Q R S Т U V W Х Υ Ζ [ ١ ] ^ \_ 1 1 0 b f i j 6 а С d е g h k ι m n ο $\infty$ 1 1 1 q у DEL 7 р r s t u v W Х z { } ~

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### ASCII Code Chart 1 | 2 | 3 | 4 | 5 6 7 8 | 9 IAIBICIDIEIF 0 0 NUL SOH STX ETX EOT ENQ ACK BEL BS ΗT LF VT | FF CR **S**0 SI 000 bits 001 1 DLE DC1 DC2 DC3 DC4 NAK SYN ETB CAN EM SUB ESC FS GS RS US 0 1 0 % # \$ & / 2 1 н . ( ) \* + , -• 3 0 5 9 ; ? 0 1 1 1 2 3 4 6 7 8 : < > = ω rows: 100 4 @ Α В С D Ε F G Н Ι J Κ М Ν 0 L 101 5 Р Q R S Т U V W Х Υ Ζ [ ١ ] ^ 1 1 0 b f i i а С d е g h k ι m n ο ω 1 1 1 q DEL у р r s t u v W х z ł ł ~

### American Standard Code for Information Interchange

16 columns: 4 bits

• Layout was chosen to support sorting by character code

### ASCII Code Chart 1 | 2 | 3 | 4 | 5 6 8 | 9 ΑΙΒΙCΙDΙΕΙF 7 0 0 NUL SOH STX ETX EOT ENQ ACK BEL BS ΗT LF VT | FF CR **S**0 SI 000 bits 1 DLE DC1 DC2 DC3 DC4 NAK SYN ETB CAN 001 EM SUBESC FS GS RS US 010 % / # \$ & 2 1 н н. ( ) \* + , -• 3 0 5 9 ? 0 1 1 1 2 3 4 6 7 8 ; < = > 1 ω rows: 100 @ Α В С Ε F G Н Ι J Κ М Ν 0 D L 41 101 5 Р Q R Т U V W Х Y Ζ S [ \ 1 ^ 1 1 0 f i а b С d е g h j k ι m n ο ω 1 1 1 q у DEL р r s t u v W Х z ł

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### ASCII Code Chart 1 | 2 | 3 | 4 | 5 6 8 | 9 AIBICIDIEIF 7 0 0 NUL SOH STX ETX EOT ENQ ACK BEL BS ΗT LF VT FF CR **S**0 SI 000 bits 001 1 DLE DC1 DC2 DC3 DC4 NAK SYN ETB CAN EM SUB FS GS RS US 010 % / # \$ & 2 1 н Т. ( ) \* + , -• 3 0 5 9 ? 0 1 1 1 2 3 4 6 7 8 ; < = > 1 ω rows: 100 @ Α В С Ε F G Н Ι J Κ М Ν 0 4 D L 101 5 Р Q R Т U V W Х Y Ζ S [ \ 1 ^ 1 1 0 f i а b С d е g h j k ι m n 0 $\infty$ 1 1 1 q y DEL р r s t u v W Х z ł

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		ASCII Code Chart												Line	e fee	ed''	(\n)			
					0	1	2	3	4	ן 5	6	7	8	9		В	C	D	Е	I F I
0	0	0	T	0	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	HT	LF	VT	FF	CR	S0	SI
0	0	1	ts	1	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
0	1	0	bі	2		!	н	#	\$	%	&	I	(	)	*	+	,	-	•	/
0	1	1	Μ	3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	^	?
1	0	0	 S	4	@	Α	В	С	D	E	F	G	Н	I	J	K	L	М	Ν	0
1	0	1	rows	5	Р	Q	R	S	Т	U	V	W	Х	Y	Z	[	\	]	^	-
1	1	0		6	`	а	b	с	d	е	f	g	h	i	j	k	ι	m	n	0
1	1	1	œ	7	р	q	r	s	t	u	v	w	х	У	z	{		}	ł	DEL

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	"Bell" (\a) ASCII Code Chart												11	Line	fee	ed''	(\n)			
					0	1	2	3	4	5	6	7	8	9		В	С	D	E	I F I
0	0	0	]	0	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	HT	LF	VT	FF	CR	S0	SI
0	0	1	ts	1	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
0	1	0	Ъi	2		!	п	#	\$	%	&	1	(	)	*	+	,	-	-	/
0	1	1	m	3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
1	0	0	 ເ	4	@	Α	В	С	D	E	F	G	Н	I	J	К	L	М	N	0
1	0	1	rows	5	Р	Q	R	S	Т	U	V	W	Х	Y	Z	[	\	]	^	-
1	1	0		6	`	а	b	с	d	е	f	g	h	i	j	k	ι	m	n	0
1	1	1	∞	7	р	q	r	s	t	u	v	w	х	у	z	{		}	1	DEL

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	"Bell" (\a)													11	Line	fee	ed''	(\n)
			0	1	2	3	4	5	6	7	8	9		В	С	D	E	I F I
000	]	0	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	HT	LF	VT	FF	CR	S0	SI
001	ts	1	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
010	bi	2		!	н	#	\$	%	&		(	)	*	+	,	-	•	/
0 1 1	Μ	3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	^	?
100	 S	4	@	Α	В	С	D	E	F	G	Н	I	J	K	L	М	N	0
101	rows	5	Р	Q	R	S	Т	U	V	W	Х	Y	Ζ	[	\	]	^	-
1 1 0		6	`	а	b	с	d	е	f	g	h	i	j	k	ι	m	n	0
1 1 1	ω	7	р	q	r	s	t	u	v	w	х	У	z	{	Ι	}	۲	DEL
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(Demo)

<b></b> 容 二 一	聲	聳	聴	聵	聶	職	聸
8071	8072	8073	8074	8075	8076	8077	8078
健	腲	腳	腴	腵	腵	腷	腸
8171	8172	8173	8174	8175	8176	8177	8178
酿	色	艳	艴	艵	艶	艷	艸
8271	8272	8273	8274	8275	8276	8277	8278
芼	荲	荳	荴	荵	荶	荷	茡
8371	8372	8373	8374	8375	8376	8377	8378
葱	葲	葳	葴	葵	葶	葷	葸

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8071	8072	8073	8074	8075	8076	8077	8078
健	腲	腳	腴	腵	腵	腷	腸
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8271	8272	8273	8274	8275	8276	8277	8278
芎毛	荲	荳	荴	荵	荶	荷	茡
8371	8372	8373	8374	8375	8376	8377	8378
葱	葲	葳	葴	葵	葶	葷	葸

- 137,994 characters in Unicode 12.1
- 150 scripts (organized)

簳	聲	聳	瘛	聵	圤	職	聸
8071	8072	8073	8074	8075	8076	8077	8078
健	腲	腳	腴	腵	腵	腷	腸
8171	8172	8173	8174	8175	8176	8177	8178
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8271	8272	8273	8274	8275	8276	8277	8278
苔毛	荲	荳	荴	荵	荶	荷	茡
8371	8372	8373	8374	8375	8376	8377	8378
葱	葲	葳	葴	葵	葶	葷	葸

- 137,994 characters in Unicode 12.1
- 150 scripts (organized)
- Enumeration of character properties, such as case

鞀	聲	聳	聴	聵	圤	職	聸
8071	8072	8073	8074	8075	8076	8077	8078
<u>健</u> 8171	腲	腳 8173	<b></b> 腴	服	服	届	腸
酿	色	艳	艴	艵	艶	些	丱
8271	8272	8273	8274	8275	8276	8277	8278
芼	荲	荳	荴	荵	荶	荷	荸
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- 150 scripts (organized)
- Enumeration of character properties, such as case
- Supports bidirectional display order

辥	聲	聳	瘛	聵	圤	職	聸
8071	8072	8073	8074	8075	8076	8077	8078
健	腲	腳	腴	腵	腵	腷	腸
8171	8172	8173	8174	8175	8176	8177	8178
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- 150 scripts (organized)
- Enumeration of character properties, such as case
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- A canonical name for every character

辥	聲	聳	瘛	聵	圤	職	聸
8071	8072	8073	8074	8075	8076	8077	8078
健	腲	腳	腴	腵	腵	腷	腸
8171	8172	8173	8174	8175	8176	8177	8178
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芼	荲	荳	荴	荵	荶	荷	茡
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葱	葲	葳	葴	葵	葶	葷	恵

http://ian-albert.com/unicode\_chart/unichart-chinese.jpg

LATIN CAPITAL LETTER A

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辥	聲	聳	聴	聵	圤	職	聸
8071	8072	8073	8074	8075	8076	8077	8078
健	腲	腳	腴	腵	腵	腷	腸
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LATIN CAPITAL LETTER A

DIE FACE-6

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EIGHTH NOTE

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EIGHTH NOTE



(Demo)

**Mutation Operations** 

[<u>Demo</u>]

## [<u>Demo</u>]

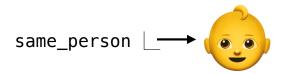
First example in the course of an object changing state

## [<u>Demo</u>]

First example in the course of an object changing state

#### [<u>Demo</u>]

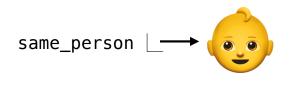
First example in the course of an object changing state



## [<u>Demo</u>]

First example in the course of an object changing state

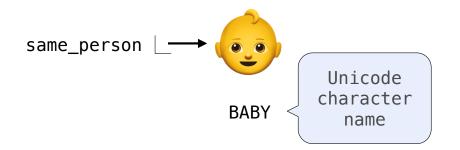
The same object can change in value throughout the course of computation



BABY

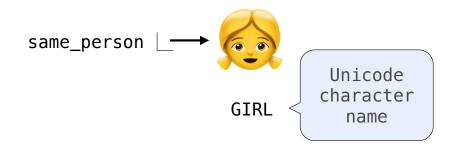
## [<u>Demo</u>]

First example in the course of an object changing state



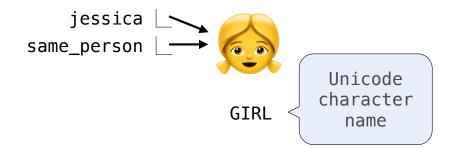
## [<u>Demo</u>]

First example in the course of an object changing state



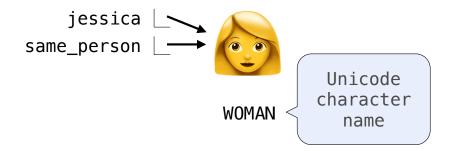
## [<u>Demo</u>]

First example in the course of an object changing state



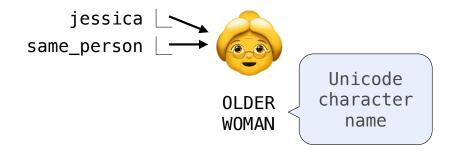
## [<u>Demo</u>]

First example in the course of an object changing state



## [<u>Demo</u>]

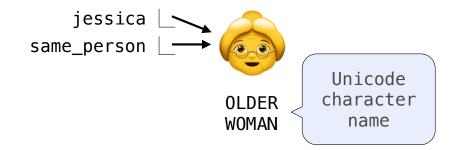
First example in the course of an object changing state



#### [<u>Demo</u>]

First example in the course of an object changing state

The same object can change in value throughout the course of computation

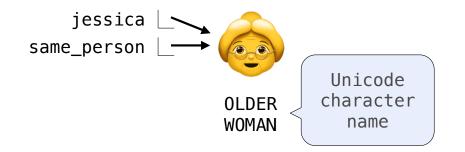


All names that refer to the same object are affected by a mutation

#### [Demo]

First example in the course of an object changing state

The same object can change in value throughout the course of computation



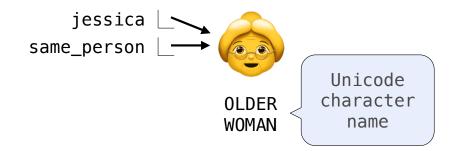
All names that refer to the same object are affected by a mutation

Only objects of *mutable* types can change: lists & dictionaries

#### [Demo]

First example in the course of an object changing state

The same object can change in value throughout the course of computation



All names that refer to the same object are affected by a mutation

Only objects of *mutable* types can change: lists & dictionaries

{Demo}

A function can change the value of any object in its scope

>>> four = [1, 2, 3, 4]

```
>>> four = [1, 2, 3, 4]
>>> len(four)
4
```

```
>>> four = [1, 2, 3, 4]
>>> len(four)
4
>>> mystery(four)
```

```
>>> four = [1, 2, 3, 4]
>>> len(four)
4
>>> mystery(four)
>>> len(four)
2
```

A function can change the value of any object in its scope

```
>>> four = [1, 2, 3, 4]
>>> len(four)
4
>>> mystery(four)
>>> len(four)
2
```

```
def mystery(s):
    s.pop()
    s.pop()
```

A function can change the value of any object in its scope

```
>>> four = [1, 2, 3, 4]
>>> len(four)
4
>>> mystery(four)
>>> len(four)
2
```

A function can change the value of any object in its scope

```
>>> four = [1, 2, 3, 4]
                                             def mystery(s): or def mystery(s):
>>> len(four)
4
>>> mystery(four)
>>> len(four)
2
```

s.pop()

s.pop()

s[2:] = []

```
>>> four = [1, 2, 3, 4]
```

A function can change the value of any object in its scope

```
>>> four = [1, 2, 3, 4]
>>> len(four)
4
>>> mystery(four)
>>> len(four)
2
>>> four = [1, 2, 3, 4]
>>> len(four)
4
```

A function can change the value of any object in its scope

```
>>> four = [1, 2, 3, 4]
>>> len(four)
4
>>> mystery(four)
>>> len(four)
2
>>> four = [1, 2, 3, 4]
>>> four = [1, 2, 3, 4]
>>> len(four)
4
>>> another_mystery() # No arguments!
```

A function can change the value of any object in its scope

```
>>> four = [1, 2, 3, 4]
                                              def mystery(s): or def mystery(s):
                                                  s.pop()
>>> len(four)
                                                                        s[2:] = []
4
                                                  s.pop()
>>> mystery(four)
>>> len(four)
2
>>> four = [1, 2, 3, 4]
>>> len(four)
4
>>> another_mystery() # No arguments!
>>> len(four)
2
```

A function can change the value of any object in its scope

```
>>> four = [1, 2, 3, 4]
                                              def mystery(s): or def mystery(s):
>>> len(four)
                                                  s.pop()
                                                                         s[2:] = []
4
                                                  s.pop()
>>> mystery(four)
>>> len(four)
2
>>> four = [1, 2, 3, 4]
                                              def another_mystery():
>>> len(four)
                                                  four.pop()
                                                  four.pop()
Δ
>>> another_mystery() # No arguments!
>>> len(four)
2
```

# Tuples

(Demo)

Immutable values are protected from mutation

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)

Immutable values are protected from mutation

>>> turtle = (1, 2, 3) >>> ooze()

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)
>>> ooze()
>>> turtle

Immutable values are protected from mutation

```
>>> turtle = (1, 2, 3)
>>> ooze()
>>> turtle
(1, 2, 3)
```

Immutable values are protected from mutation

```
>>> turtle = (1, 2, 3)
>>> ooze()
>>> turtle
(1, 2, 3)
```

>>> turtle = [1, 2, 3]

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)
>>> ooze()
>>> turtle
(1, 2, 3)

>>> turtle = [1, 2, 3]
>>> ooze()

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)
>>> ooze()
>>> turtle
(1, 2, 3)
>>> turtle

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)
>>> ooze()
>>> turtle
(1, 2, 3)

>>> turtle = [1, 2, 3]
>>> ooze()
>>> turtle
['Anything could be inside!']

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:

Name change:

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

>>> X + X

>>> x + x

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:

>>> x + x

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

```
>>> x = 2
>>> x + x
4
Name change:
>>> x + x
```

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

```
Name change:

>>> x = 2

>>> x + x

4

>>> x = 3

>>> x + x
```

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:  

$$>>> x = 2$$
  
 $>>> x + x$   
 $4$   
 $>>> x = 3$   
 $>>> x + x$   
 $6$ 

**Object mutation:** 

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

Name change:  

$$\begin{array}{c} >>> x = 2 \\ >>> x + x \\ 4 \\ >>> x = 3 \\ >>> x + x \\ 6 \end{array}$$
Object mutation:  

$$\begin{array}{c} >>> x + x \\ >>> x + x \\ 6 \end{array}$$

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

x = 2 $  x + x$			>>> x = [1, 2]
		>>> X + X	
Name change:	$^{4}$ >>> x = 3	<b>Object</b> mutation:	
	$\rightarrow \rightarrow \times \times$		>>> x + x
	6		

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

	>>> x = 2		>>> x = [1, 2]
Name change: >>> x + x 4 >>> x = 3 >>> x + x	>>> X + X		>>> X + X
	4	<b>Object</b> mutation:	[1, 2, 1, 2]
	>>> x = 3		
	>>> X + X		>>> X + X
	6		

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

Name change:	>>> $x = 2$ >>> $x + x$ 4 >>> $x = 3$ >>> $x + x$ 6	<b>Object mutation:</b>	<pre>&gt;&gt;&gt; x = [1, 2] &gt;&gt;&gt; x + x [1, 2, 1, 2] &gt;&gt;&gt; x.append(3) &gt;&gt;&gt; x + x</pre>
--------------	--	-------------------------	--

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

Name change:	>>> x = 2 >>> x + x 4 >>> x = 3 >>> x + x 6	<b>Object mutation:</b>	<pre>&gt;&gt;&gt; x = [1, 2] &gt;&gt;&gt; x + x [1, 2, 1, 2] &gt;&gt;&gt; x.append(3) &gt;&gt;&gt; x + x [1, 2, 3, 1, 2, 3]</pre>
--------------	--	-------------------------	---

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:	>>> $x = 2$ >>> $x + x$ 4 >>> $x = 3$ >>> $x + x$ 6	<b>Object mutation:</b>	<pre>&gt;&gt;&gt; x = [1, 2] &gt;&gt;&gt; x + x [1, 2, 1, 2] &gt;&gt;&gt; x.append(3) &gt;&gt;&gt; x + x [1, 2, 3, 1, 2, 3]</pre>
	6		[1, 2, 3, 1, 2, 3]

An immutable sequence may still change if it contains a mutable value as an element

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

An immutable sequence may still change if it contains a mutable value as an element

```
>>> s = ([1, 2], 3)
```

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:  $\begin{array}{c} >>> x = 2 \\ >>> x + x \\ 4 \\ >>> x = 3 \\ >>> x + x \\ 6 \end{array}$ Object mutation:  $\begin{array}{c} >>> x = [1, 2] \\ >>> x + x \\ [1, 2, 1, 2] \\ >>> x + x \\ >>> x + x \\ [1, 2, 3, 1, 2, 3] \end{array}$ 

An immutable sequence may still change if it contains a mutable value as an element

```
>>> s = ([1, 2], 3)
>>> s[0] = 4
```

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:  $\begin{array}{c} >>> x = 2 \\ >>> x + x \\ 4 \\ >>> x = 3 \\ >>> x + x \\ 6 \end{array}$ Object mutation:  $\begin{array}{c} >>> x = [1, 2] \\ >>> x + x \\ [1, 2, 1, 2] \\ >>> x + x \\ >>> x + x \\ [1, 2, 3, 1, 2, 3] \end{array}$ 

An immutable sequence may still change if it contains a mutable value as an element

```
>>> s = ([1, 2], 3)
>>> s[0] = 4
ERROR
```

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

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>>> s = ([1, 2], 3)
>>> s[0] = 4
ERROR
```

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:  $\begin{array}{c} >>> x = 2 \\ >>> x + x \\ 4 \\ >>> x = 3 \\ >>> x + x \\ 6 \end{array}$ Object mutation:  $\begin{array}{c} >>> x = [1, 2] \\ >>> x + x \\ [1, 2, 1, 2] \\ >>> x + x \\ >>> x + x \\ [1, 2, 3, 1, 2, 3] \end{array}$ 

An immutable sequence may still change if it contains a mutable value as an element

```
>>> s = ([1, 2], 3)
>>> s[0] = 4
ERROR
>>> s[0][0] = 4
```

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:  $\begin{array}{c} >>> x = 2 \\ >>> x + x \\ 4 \\ >>> x = 3 \\ >>> x + x \\ 6 \end{array}$ Object mutation:  $\begin{array}{c} >>> x = [1, 2] \\ >>> x + x \\ [1, 2, 1, 2] \\ >>> x + x \\ >>> x + x \\ [1, 2, 3, 1, 2, 3] \end{array}$ 

An immutable sequence may still change if it contains a mutable value as an element

```
>>> s = ([1, 2], 3)
>>> s[0] = 4
ERROR
>>> s
```

Immutable values are protected from mutation

>>> turtle = (1, 2, 3)	>>> turtle = [1, 2, 3]
>>> ooze()	>>> ooze()
>>> turtle	>>> turtle
(1, 2, 3)	['Anything could be inside!']

The value of an expression can change because of changes in names or objects

Name change:  $\begin{array}{c} >>> x = 2 \\ >>> x + x \\ 4 \\ >>> x = 3 \\ >>> x + x \\ 6 \end{array}$ Object mutation:  $\begin{array}{c} >>> x = [1, 2] \\ >>> x + x \\ [1, 2, 1, 2] \\ >>> x + x \\ (1, 2, 3, 1, 2, 3] \end{array}$ 

An immutable sequence may still change if it contains a mutable value as an element

```
>>> s = ([1, 2], 3)

>>> s[0] = 4

ERROR

>>> s [0] [0] = 4

>>> s

([4, 2], 3)
```

**Mutation** 

• As long as we never modify objects, a compound object is just the totality of its pieces

• As long as we never modify objects, a compound object is just the totality of its pieces

• A rational number is just its numerator and denominator

- As long as we never modify objects, a compound object is just the totality of its pieces
- A rational number is just its numerator and denominator
- This view is no longer valid in the presence of change

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• As long as we never modify objects, a compound object is just the totality of its pieces

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>>> a = [10]

• As long as we never modify objects, a compound object is just the totality of its pieces

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>>> a = [10] >>> b = a

• As long as we never modify objects, a compound object is just the totality of its pieces

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```
>>> a = [10]
>>> b = a
>>> a == b
True
```

• As long as we never modify objects, a compound object is just the totality of its pieces

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```
>>> a = [10]
>>> b = a
>>> a == b
True
>>> a.append(20)
```

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```
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>>> b = a
>>> a == b
True
>>> a.append(20)
>>> a
[10, 20]
```

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>>> a = [10]
>>> b = a
>>> a == b
True
>>> a.append(20)
>>> a
[10, 20]
>>> b
[10, 20]
```

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>>> a = [10]
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>>> a
[10, 20]
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[10, 20]
>>> a == b
True
```

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[10, 20]
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```

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>>> b = a
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True
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>>> a
[10, 20]
>>> b
[10, 20]
>>> a == b
True
```

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```

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```
>>> a = [10]
>>> b = a
>>> b = [10]
>>> b = [10]
>>> b = [10]
>>> a == b
True
>>> a == b
True
>>> a == b
True
>>> a
[10, 20]
>>> b
[10, 20]
>>> a == b
True
```

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```
>>> a = [10]
                                    >>> a = [10]
                                    >>> b = [10]
>>> b = a
>>> a == b
                                    >>> a == b
True
                                    True
>>> a.append(20)
                                    >>> b.append(20)
>>> a
[10, 20]
>>> b
[10, 20]
>>> a == b
True
```

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```
>>> a = [10]
                                    >>> a = [10]
                                    >>> b = [10]
>>> b = a
>>> a == b
                                    >>> a == b
True
                                    True
>>> a.append(20)
                                    >>> b_append(20)
>>> a
                                     >>> a
[10, 20]
                                     [10]
>>> b
[10, 20]
>>> a == b
True
```

• As long as we never modify objects, a compound object is just the totality of its pieces

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>>> a = [10]
                                    >>> a = [10]
                                    >>> b = [10]
>>> b = a
>>> a == b
                                    >>> a == b
True
                                    True
>>> a.append(20)
                                    >>> b_append(20)
>>> a
                                     >>> a
[10, 20]
                                     [10]
>>> b
                                     >>> b
[10, 20]
                                     [10, 20]
>>> a == b
True
```

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- A rational number is just its numerator and denominator
- This view is no longer valid in the presence of change
- A compound data object has an "identity" in addition to the pieces of which it is composed
- A list is still "the same" list even if we change its contents

>>> a = [10]	>>> a = [10]
>>> b = a	>>> b = [10]
>>> a == b	>>> a == b
True	True
>>> a.append(20)	>>> b.append(20)
>>> a	>>> a
[10, 20]	[10]
>>> b	>>> b
[10, 20]	[10, 20]
>>> a == b	>>> a == b
True	False

### Identity

#### <exp0> is <exp1>

evaluates to True if both <exp0> and <exp1> evaluate to the same object

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#### Equality

<exp0> == <exp1>

evaluates to True if both <exp0> and <exp1> evaluate to equal values

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evaluates to True if both <exp0> and <exp1> evaluate to equal values

Identical objects are always equal values

#### Identity

<exp0> is <exp1>

evaluates to True if both <exp0> and <exp1> evaluate to the same object

#### Equality

<exp0> == <exp1>

evaluates to True if both <exp0> and <exp1> evaluate to equal values

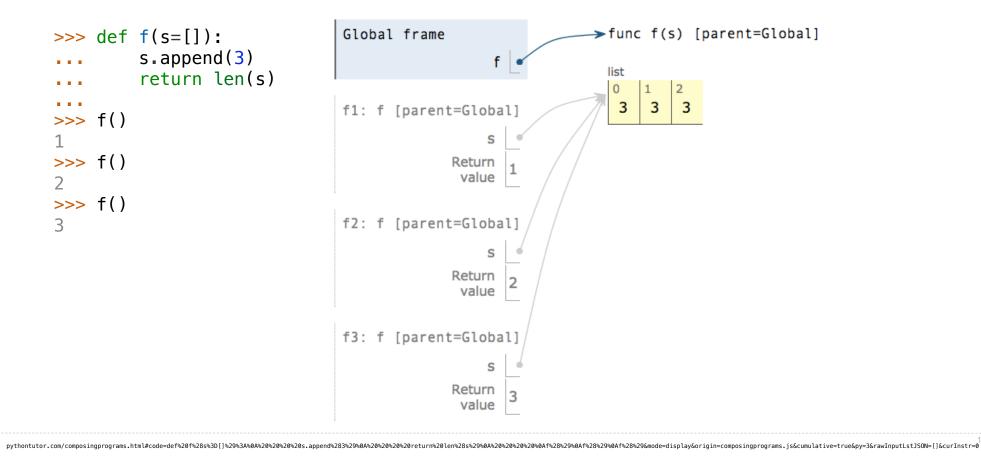
Identical objects are always equal values

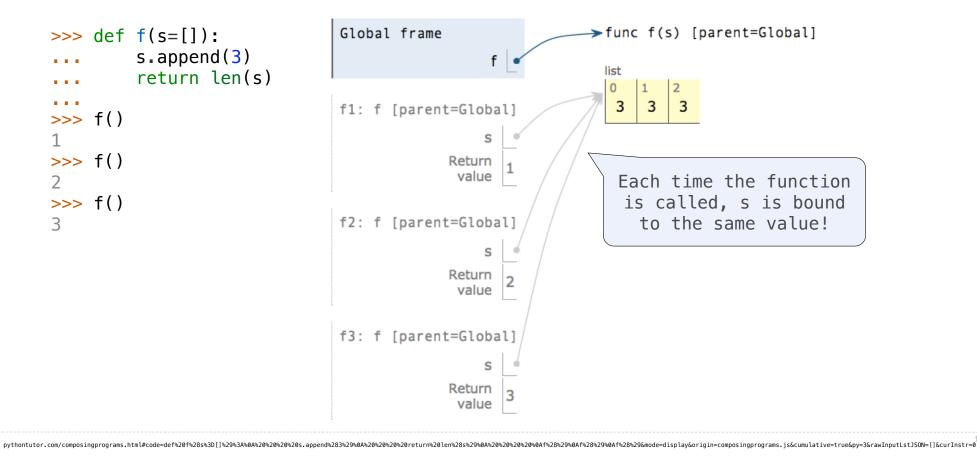
(Demo)

```
>>> def f(s=[]):
... s.append(3)
... return len(s)
...
```

```
>>> def f(s=[]):
... s.append(3)
... return len(s)
...
>>> f()
1
```

```
>>> def f(s=[]):
... s.append(3)
... return len(s)
...
>>> f()
1
>>> f()
2
```





**Mutable Functions** 

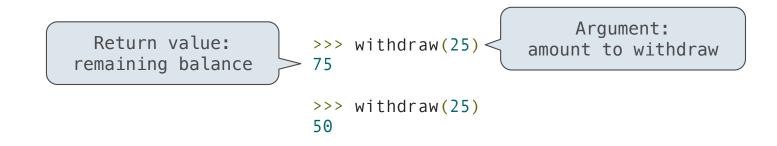
Let's model a bank account that has a balance of \$100

>>> withdraw(25)

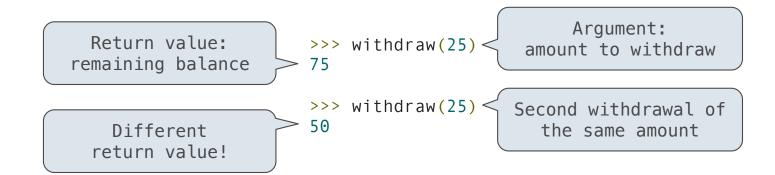
Let's model a bank account that has a balance of \$100

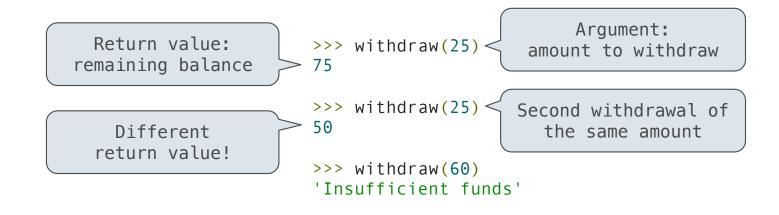
>>> withdraw(25)
75

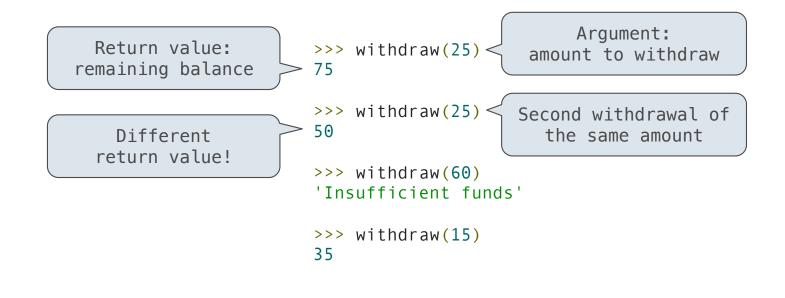


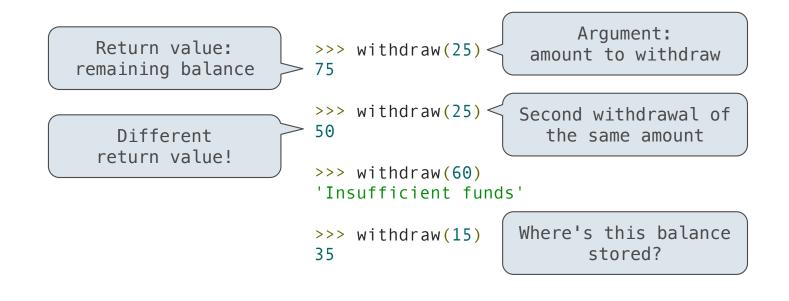


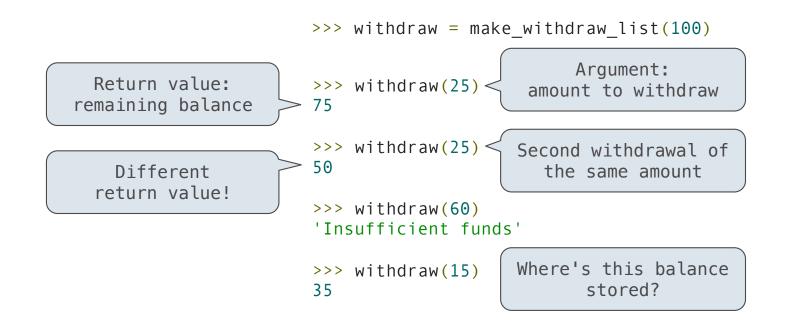


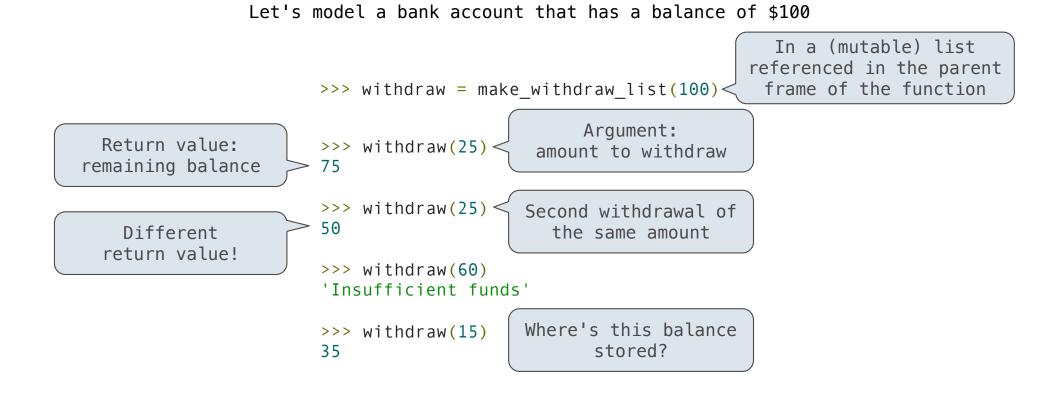












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```
def make_withdraw_list(balance):
    b = [balance]
    def withdraw(amount):
        if amount > b[0]:
            return 'Insufficient funds'
        b[0] = b[0] - amount
        return b[0]
    return withdraw
withdraw = make_withdraw_list(100)
withdraw(25)
```

