



Tree-Structured Data

```
def tree(label, branches=[]):
    return [label] + list(branches)

def label(t):
    return t[0]

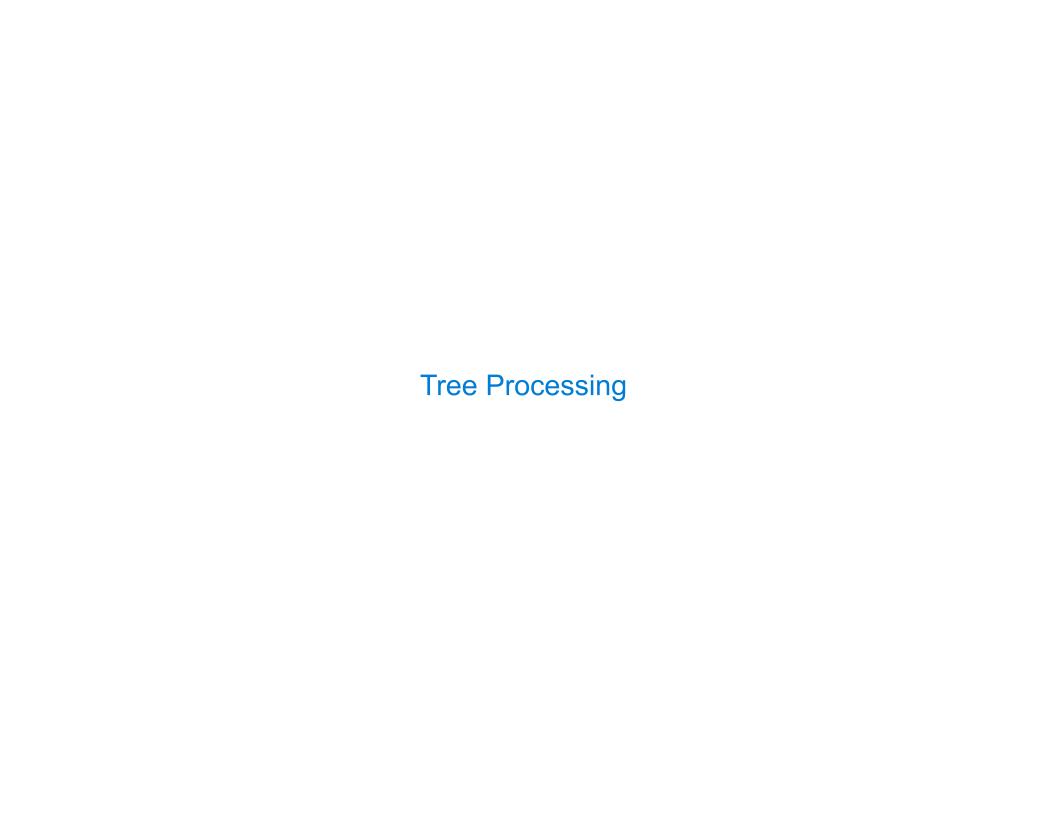
def branches(t):
    return t[1:]

def is_leaf(t):
    return not branches(t)

class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        self.branches = list(branches)

def is_leaf(self):
    return not self.branches
```

```
A tree can contains other trees:
[5, [6, 7], 8, [[9], 10]]
(+5(-67)8(*(-9)10))
(S
 (NP (JJ Short) (NNS cuts))
 (VP (VBP make)
     (NP (JJ long) (NNS delays)))
 (. .))
<l
 Midterm <b>1</b>
 Midterm <b>2</b>
Tree processing often involves
recursive calls on subtrees
```

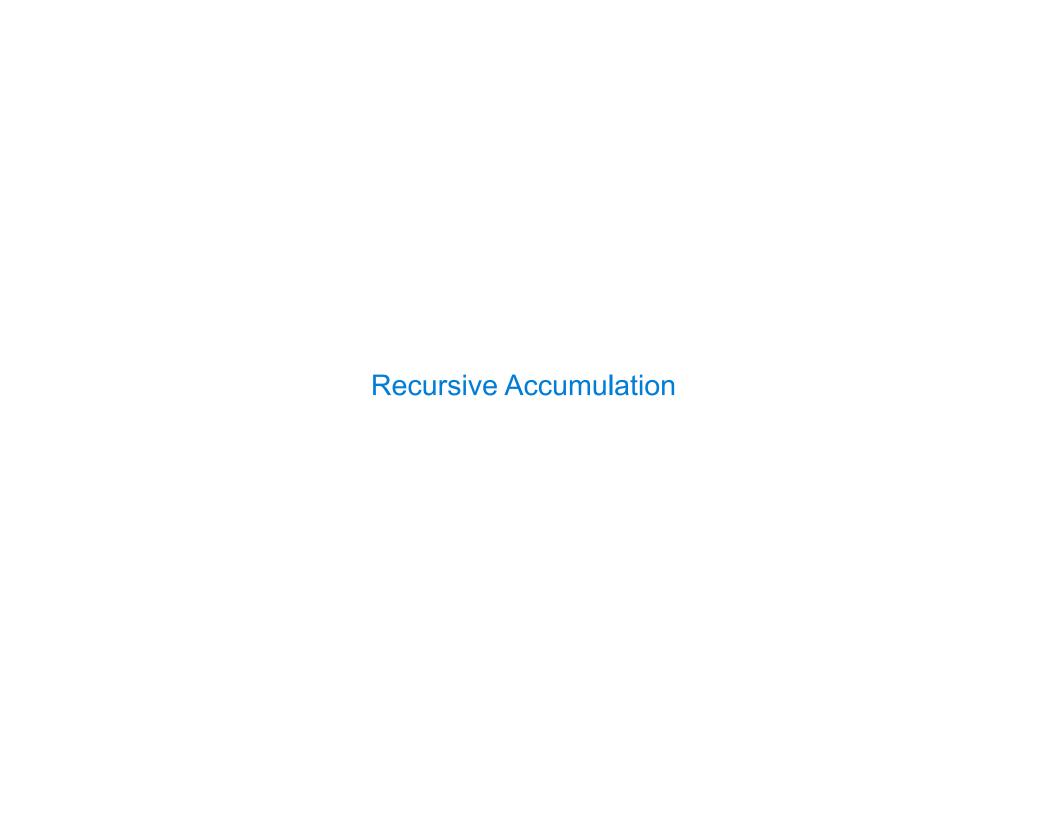


Solving Tree Problems

```
Implement bigs, which takes a Tree instance t containing integer labels. It returns the
number of nodes in t whose labels are larger than all labels of their ancestor nodes.
(Assume the root label is always larger than all of its ancestors, since it has none.)
def bigs(t):
    """Return the number of nodes in t that are larger than all their ancestors.
   >>> a = Tree(1, [Tree(4, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(2)])])])
   >>> bigs(a)
                                                                                   5
                                                             Somehow track a
  if t.is leaf():
                                                            list of ancestors
      return
  else:
                                               if node.label > max(ancestors):
      return ([ for b in t-branches])
                                                            Somehow track the
                                                             largest ancestor
            Somehow increment
             the total count
                                               if node.label > max ancestors:
```

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   >>> a = Tree(1, [Tree(4, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(2)])])])
    >>> bigs(a)
                   Somehow track the
                    largest ancestor
   def f(a, x):
    A node max_ancestor
                                        node.label > max_ancestors
        if
            return 1 + sum([f(b, a.label) for b in a.branches])
                           Somehow increment the total count
        else:
                       sum([f(b, x) for b in a.branches])
            return
            f(t,t.label - 1 ) < Root label is always larger than its ancestors
                  Some initial value for the largest ancestor so far...
```



Solving Tree Problems

Implement **bigs**, which takes a Tree instance t containing integer labels. It returns the number of nodes in t whose labels are larger than any labels of their ancestor nodes.

Designing Functions

How to Design Programs

From Problem Analysis to Data Definitions

Identify the information that must be represented and how it is represented in the chosen programming language. Formulate data definitions and illustrate them with examples.

Signature, Purpose Statement, Header

State what kind of data the desired function consumes and produces. Formulate a concise answer to the question what the function computes. Define a stub that lives up to the signature.

Functional Examples

Work through examples that illustrate the function's purpose.

Function Template

Translate the data definitions into an outline of the function.

Function Definition

Fill in the gaps in the function template. Exploit the purpose statement and the examples.

Testing

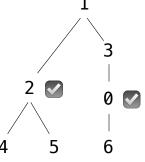
Articulate the <u>examples</u> as tests and ensure that the function passes all. Doing so discovers mistakes. Tests also supplement examples in that they help others read and understand the definition when the need arises—and it will arise for any serious program.

Applying the Design Process

Designing a Function

Implement smalls, which takes a Tree instance t containing integer labels. It returns the non-leaf nodes in t whose labels are smaller than any labels of their descendant nodes.

```
Signature: Tree -> List of Trees
def smalls(t):
   """Return the non-leaf nodes in t that are smaller than all their descendants.
   >>> a = Tree(1, [Tree(2, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(6)])])])
   >>> sorted([t.label for t in smalls(a)])
    [0, 2]
    0.00
                         Signature: Tree -> number
    result = []
   def process(t):
                         "Find smallest label in t & maybe add t to result"
       if t.is_leaf():
           return t.label
       else:
           return min(...)
    process(t)
    return result
```

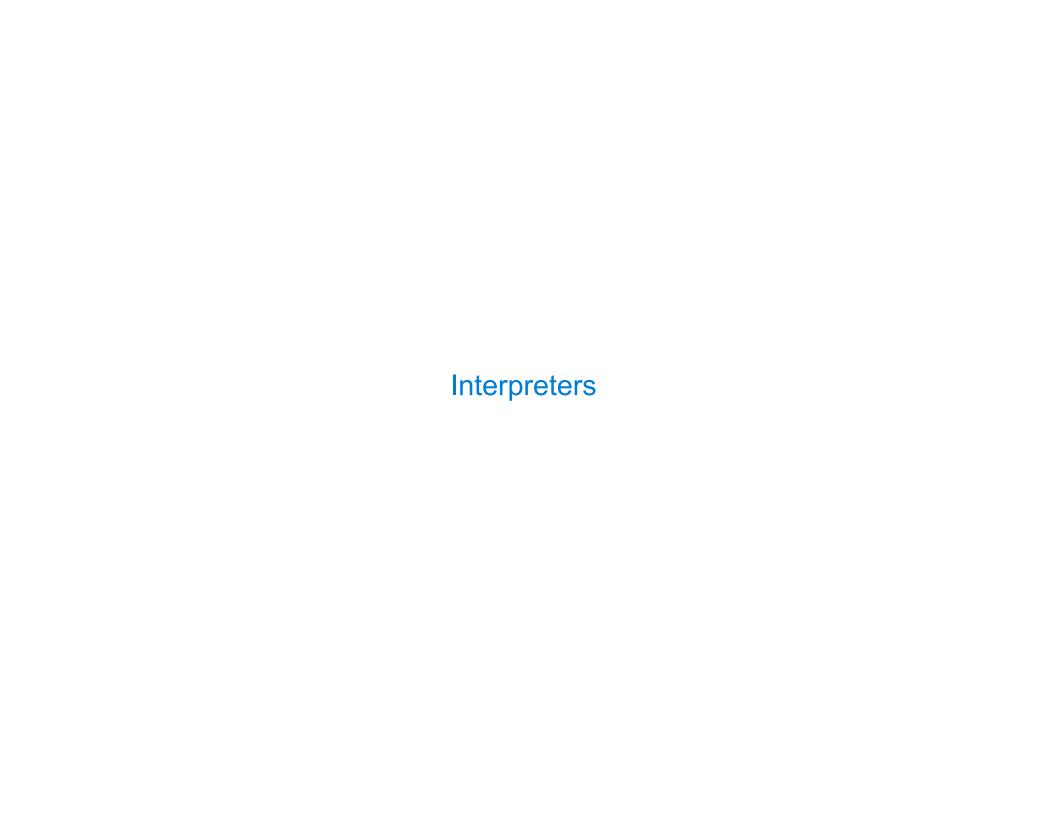




Designing a Function

Implement smalls, which takes a Tree instance t containing integer labels. It returns the non-leaf nodes in t whose labels are smaller than any labels of their descendant nodes.

```
Signature: Tree -> List of Trees
   def smalls(t):
       """Return a list of the non-leaf nodes in t that are smaller than all descendants.
       >>> a = Tree(1, [Tree(2, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(6)])])])
       >>> sorted([t.label for t in smalls(a)])
       [0, 2]
       0.000
                             Signature: Tree -> number
       result = []
       def process(t):
                             "Find smallest label in t & maybe add t to result"
           if t.is_leaf():
                                        t.label
               return
           else:
                           min([process(b) for b in t.branches])
smallest label 7; f
                        t.label < smallest</pre>
in a branch of t
                       result.append( t )
               return min(smallest, t.label)
       process(t)
        return result
```



Interpreter Analysis

What expressions are passed to scheme_eval when evaluating the following expressions?

