## CS61A Notes 05 – Fake Plastic Trees (v1.1)

#### **Fake Plastic Trees**

A tree is, abstractly, an acyclic, connected set of nodes (of course, that's not a very friendly definition). Usually, it is a node that contains two kinds of things – data and children. Data is whatever information may be associated with a tree, and children is a set of subtrees with this node as the parent. Concretely, it's often just a list of lists of lists of lists in Scheme, but it's best NOT to think of trees as lists at all. Trees are trees, lists are lists. They are completely different things, and if you, say, call (car tree) or something like that, we'll yell at you for violating data abstraction. car, cdr, list and append are for lists, not trees! And don't bother with box-and-pointer diagrams – they get way too complicated for trees. Just let the data abstraction hide the details from you, and trust that the procedures like make-tree work as intended.

Of course, that means we need our own procedures for working with trees analogous to car, cdr, etc. Different representations of trees use different procedures. You're already seen the ones for a general tree, which is one that can have any number of children (not just two) in any order (not grouped into smaller-than and larger-than). Its operators are things like:

Note that foo-tree calls foo-forest, and foo-forest calls foo-tree! Mutual recursion is absolutely mind-boggling if you think about it too hard. The key thing to do here is – of course – **TRUST THE RECURSION!** If when you're writing foo-tree, you BELIEVE that foo-forest is already written, then foo-tree should be easy to write. Same thing applies the other way around.

# **QUESTIONS**

1. Write (square-tree tree), which returns the same tree structure, but with every element squared. Don't use "map"!

2. Write (max-of-tree tree) that does the obvious thing. The tree has at least one element.

3. Write (listify-tree tree) that turns the tree into a list in any order. (This one you can't use map even if you tried... Muwahahaha)

### **Binary Search Trees**

A binary search tree is a special kind of tree with an interesting restriction — each node only has two children (called the "left subtree" and the "right subtree", and every node in the left subtree has datum smaller than the node of the root, and every node in the right subtree has datum larger than the node of the root. Here are some operators:

```
;; takes a datum, a left subtree and a right subtree and make a bst
(define (make-tree datum left-branch right-branch) ...)

;; returns the datum at this node
(define (datum bst) ...)

;; returns the left-subtree of this bst
(define (left-subtree bst) ...)

;; returns the right-subtree of this bst
(define (right-subtree bst) ...)
So then, let's get to it!
```

#### **QUESTIONS**

1. Jimmy the Smartass was told to write (valid-bst? bst) that checks whether a tree satisfies the binary-search-tree property – elements in left subtree are smaller than datum, and elements in right subtree are larger than datum. He came up with this:

	Why will Jimmy never succeed in life? Give an example that would fool his pitiful procedure.
2.	Write (sum-of bst) that takes in a binary search tree, and returns the sum of all the data in the tree.
3.	Write (max-of bst) that takes in a binary search tree, and returns the maximum datum in the tree. The tree has at least one element.
4.	Write (listify bst) that converts elements of the given bst into a list. The list should be in NON-DECREASING ORDER!
5.	Write (remove-leaves bst) that takes in a bst and returns the bst with all the leaves removed.

6. Write (height-of tree) that takes in a tree and returns the height – the length of the longest path from the root to a leaf.

# **Deep Lists**

"Deep lists" are lists that contain sublists. You've already been working with them in the lab with deep-reverse, and in homeworks with substitute2. You'll find, however, that sometimes, they'll have recursive properties rather like those of general trees. Here's an example.

#### **QUESTION**

Consider the following Scheme representation for a hierarchical file system. A "file-entry" can either be a file or a directory, and it is represented by a list. The file entry for a file is a list whose first element is the word FILE, and the second element is the name of the file. The file entry for a directory is a list whose first two elements are the word DIRECTORY and the name of the directory, and whose remaining elements are file entries for the files within the directory (which may be directories themselves. For example,

```
(DIRECTORY proj2
  (DIRECTORY test)
  (FILE proj2.scm)
  (DIRECTORY cheat
       (DIRECTORY my-friends-proj2
             (FILE proj2-2.scm)
             (FILE readme)
             (FILE transcript))
        (FILE proj2-copy.scm)))
```

Write a procedure (file-list file-entry) that, given a file entry for a directory, returns a list of names of the non-directory files anywhere in the corresponding directory tree. For example, given the file entry above, file-list should return the list

```
(proj2.scm proj2-2.scm readme transcript proj2-copy.scm), not necessarily in that order.
```