## CS61A Notes 11 - My Body's Floating Down The Muddy Stream [Solutions v1.0]

## Streaming Along

1. Define a procedure (ones) that, when run with no arguments, returns a cons pair whose car is 1 , and whose cdr is a procedure that, when run, does the same thing.
```
(define (ones) (cons 1 (lambda() (ones)))), or, just
(define (ones) (cons 1 ones))
```

2. Define a procedure (integers-starting $n$ ) that takes in a number $n$ and, when run, returns a cons pair whose car is $n$, and whose cdr is a procedure that, when run with no arguments, does the same thing for $\mathrm{n}+1$.
```
(define (integers-starting n)
    (cons n (lambda() (integers-starting (+ n 1)))))
```


## Constructing Streams Directly

Describe what the following expressions define:

1. (define s1 (add-stream (stream-map (lambda (x) (* x 2)) s1) s1)) infinite loop! We didn't specify a first element. Even the define statement will go into infinite loop.
2. (define s2
(cons-stream 1
(add-stream (stream-map (lambda (x) (* x 2)) s2) s2)))
```
this is:
```

1
$\left.\begin{array}{ccccc} & & 2 & 6 & 18\end{array}\right]$.

```
So powers of 3.
```

3. (define s3
(cons-stream 1
(stream-filter (lambda(x) (not (= x 1))) s3)))
Remember:
(define (stream-filter pred? s)
(cond ((stream-null? s) the-empty-stream) ((pred? (stream-car s))
(cons-stream (stream-car s)
(stream-filter pred? (stream-cdr s))))
(else (stream-filter pred? (stream-cdr s)))))

Infinite loop! stream-filter will keep trying to look for a number that's not 1. Or, more specifically, stream-filter, failing to find a non-1 element in stream-car, will call stream-filter again, which will call stream-filter again, and so on.
4. (define s4
(cons-stream 1
(cons-stream 2
(stream-filter (lambda(x) (not (= x 1))) s4))))
(1 222 2...)
Rather counter-intuitive, but... well, we know that it starts with 1 and 2, since we said so. Then, the stream-cddr will be a stream that is produced by the stream-filter. stream-filter returns a stream whose first element is the first non-1 element of s4 (namely, 2), and whose promise is (stream-filter pred? (stream-cdr s)), where pred? is the lambda, and s is s4. What's (stream-cdr s4)? Well, it's a stream containing the element 2 and a promise to evaluate (stream-filter pred? s4). And we already know what that returns - a stream starting with 2, with a promise to evaluate (stream-filter pred? (stream-cdr s)), etc.
5. (define s5
(cons-stream 1
(add-streams s5 integers)))
Well, so,
1

|  | 1 | 2 | 4 | $\ldots$ |
| :--- | :--- | :--- | :--- | :--- |
| + | 1 | 2 | 3 | 4 |

=======================
$124 \quad 7 \quad 111622 \quad 29 \ldots$

So, starting from 1, add 1, add 2, add 3, etc.
6. Define facts without defining any procedures; the stream should be a stream of $1!, 2!, 3!, 4!$, etc. More specifically, it returns a stream with elements (1 $2624 \ldots$...)
(define facts
(cons-stream 1
(stream-map * (stream-cdr integers) facts)))
7. (HARD!) Define powers; the stream should be $1^{1}, 2^{2}, 3^{3}, \ldots$, or, ( $141664 \ldots$ ). Of course, you cannot use the exponents procedure. I've given you a start, but you don't have to use it.

```
(define powers (helper integers integers))
(define (helper s t)
    (cons-stream (stream-car s)
    (helper (stream-map * (stream-cdr s) (stream-cdr t))
        (stream-cdr t))))
```


## Constructing Streams Through Procedures

1. Define a procedure, (list->stream ls) that takes in a list and converts it into a stream. (define (list->stream ls)
(cond ((null? ls) the-empty-stream) (else (cons-stream (car ls) (list->stream (cdr ls))))))
2. Define a procedure (lists-starting $n$ ) that takes in $n$ and returns a stream containing ( $n$ ), ( $n \mathrm{n}+1$ ), ( $\mathrm{n} \mathrm{n}+1 \mathrm{n}+2$ ), etc. For example, (lists-starting 1) returns a stream containing (1) (1 2) (1 2 3) (1 234 4)...
(define (lists-starting n)
(cons-stream (list n)
(stream-map (lambda(ls) (cons n ls)) (lists-starting (+ n l)))))
3. Define a procedure (chocolate name) that takes in a name and returns a stream like so: (chocolate 'chung) ==> (chung really likes chocolate chung really really likes chocolate chung really really really likes chocolate ...)

You'll want to use helper procedures.

```
(define (chocolate name)
    (define (helper n)
        (cons-stream name
            (stream-append (really n) (helper (+ n l)))))
    (define (really n)
        (cond ((= n 0)
            (cons-stream `likes
                        (cons-stream 'chocolate the-empty-stream))
                (else (cons-stream `really (really (- n l))))))
    (helper 1))
```


## Stream-Processing

1. Define a procedure, (stream-censor s replacements) that takes in a stream sand a table replacements and returns a stream with all instances of all the car of entries in replacements replaced with the cadr of the entries.
```
(stream-censor (hello you weirdo ...) ((you I-am) (weirdo an-idiot)))
            ==> (hello I-am an-idiot ...)
(define (stream-censor s replacements)
    (if (stream-null? s)
            the-empty-stream
            (let ((match (assoc (stream-car s) replacements)))
            (if match
                (cons-stream (cadr match)
                            (stream-censor (stream-cdr s) replacements))
                    (cons-stream (stream-car s)
                        (stream-censor (stream-cdr s) replacements))))))
```

2. Define a procedure (make-alternating s) that takes in a stream of positive numbers and alternate their signs. So (make-alternating ones) $==>\left(\begin{array}{llll}1 & -1 & 1 & -1 \ldots\end{array}\right)$ and (makealternating integers $)==>\left(\begin{array}{llll}1 & -2 & 3 & -4 \ldots\end{array}\right)$. Assume $s$ is an infinite stream.
(define (make-alternating s)
(cons-stream (stream-car s)
(cons-stream (* -1 (stream-car (stream-cdr s)))
(make-alternating (stream-cdr (stream-cdr s))))))
or, a cooler way:
(define (make-alternating s)
(cons-stream (stream-car s)
(stream-map (lambda (x) (* -1 x))
(make-alternating (stream-cdr s)))))

## My Body's Floating Down The Muddy Stream

1. Given streams ones, twos, threes and fours, write down the first ten elements of: (interleave ones (interleave twos (interleave threes fours))) (interleave threes fours) $==>\left(\begin{array}{lllllll}3 & 4 & 3 & 4 & 3 & 4\end{array}\right.$...)
(interleave twos threes-fours) ==> ( $\begin{array}{llllllll}2 & 3 & 2 & 4 & 2 & 3 & 2 & 4\end{array}$...)
(interleave ones twos-threes-fours) $==>\left(\begin{array}{lllllllllllll}1 & 2 & 1 & 3 & 1 & 2 & 1 & 4 & 1 & 2 & 1 & 3\end{array}\right.$...)
2. Construct a stream all-integers that includes 0 and both the negative and positive integers.
(define all-integers

$$
\begin{aligned}
(\text { interleave } & \text { (make-alternating } \\
& (\text { make-alternating } \\
& \text { (integers-starting } 1)) \text { )) })
\end{aligned}
$$

Or, you could've interleaved the positives and the negatives.
3. Suppose we were foolish enough to try to implement stream-accumulate:
(define (stream-accumulate combiner null-value s)
(cond ((stream-null? s) null-value)
(else (combiner
(stream-car s)
(stream-accumulate
combiner null-value (stream-cdr s))))))
What happens when we do:
a. (define foo (stream-accumulate +0 integers))

The define statement goes into an infinite loop. When we evaluate stream-accumulate, we'll go into the else clause, and have to call stream-accumulate again on the stream-cdr of integers, which does the same thing again. The problem is, NOTHING IS DELAYED.
b. (define bar (cons-stream 1 (stream-accumulate +0 integers))) The define statement is fine (since stream-accumulate is delayed). But when you call stream-cdr on bar, all hell breaks lose again.
c. (define baz (stream-accumulate
(lambda ( x y) (cons-stream $\mathrm{x} y$ ))
the-empty-stream integers))
So the question is, does THIS delay anything? It looks like it does. If the combiner uses cons-stream, then it seems that we'll delay the evaluation of $y$, which is the next call to accumulate. Alas, that's making the same mistake as believing new-if would work. Whereas cons-stream is a special form, the combiner is NOT, and so it will evaluate both of its arguments - including the call to accumulate - before evaluating its body. So the problem persists.
4. SICP Ex. 3.68, page 341. If you understand this, you'll be fine.

This doesn't work. Let's try (pairs integers integers). We start with a call to interleave. Well, interleave is not a special form, so evaluate both arguments. What's the first argument, the call to stream-map? It returns a stream starting with (11). What's the second argument, the call to pairs? Well, what's (pairs (stream-cdr integers) (stream-cdr integers)? It's a call to interleave. The first argument to interleave is (2 2), and the second argument is a call to pairs again... and so on.

