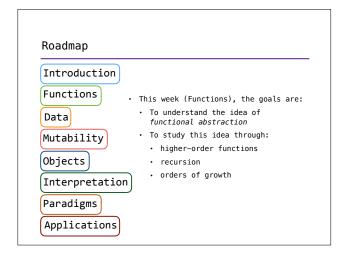
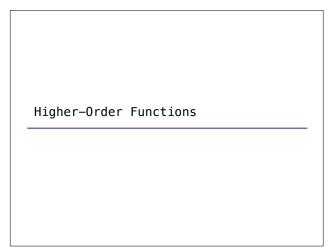
Lecture 5: Higher-Order Functions

Brian Hou June 27, 2016

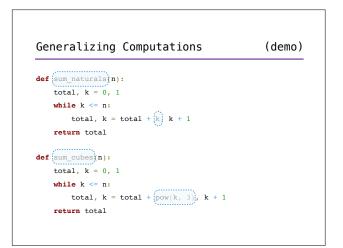
Announcements

- Homework 2 is due Wednesday 6/29
- + Project 1 is due Thursday 6/30
- Earn 1 EC point for completing it by Wednesday 6/29
- + Quiz 2 is on Thursday 6/30 at the beginning of lecture
- Environment Diagrams and Higher-Order Functions
- Group Tutoring is available! See Piazza for details

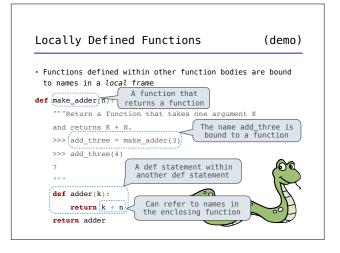


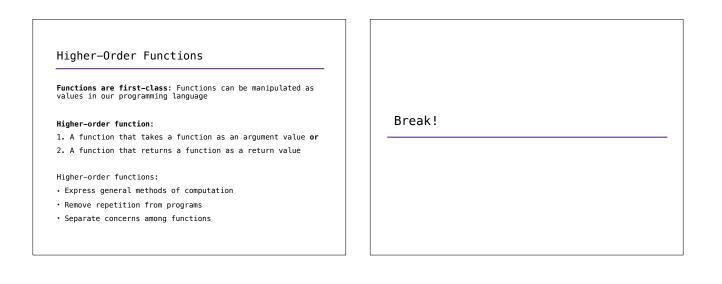


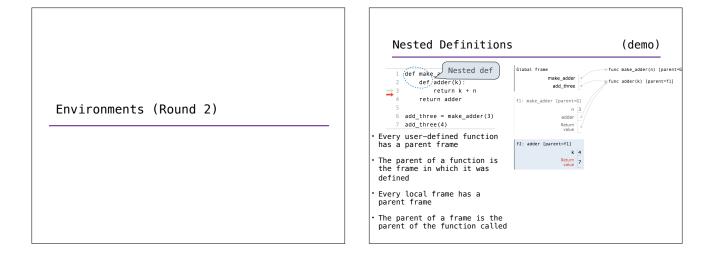
Generalizing Computations	(demo
$\sum_{k=1}^{5} k = 1 + 2 + 3 + 4 + 5$	= 15
$\sum_{k=1}^{5} \widehat{k^3} = 1^3 + 2^3 + 3^3 + 4^3 + 5^3$	= 225
$\sum_{k=1}^{5} \left[\frac{8}{(4k-3) \cdot (4k-1)} \right] = \frac{8}{3} + \frac{8}{35} + \frac{8}{99} + \frac{8}{195} + \frac{8}{323}$	= 3.04

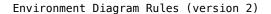


<pre>Function of a single argument (not called "term") A parameter that will be bound to a function """Sum the first N terms of a sequence.</pre>	,)
def summation(n, term) bound to a function	
>>> summation(5, cube)	
225 The cube function is passed as an argument value	
<pre>total, k = 0, 1 The function bound to term gets called here</pre>	









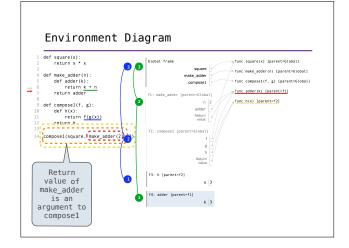
Rules for def Statements:

- Create a function with signature <name>(<parameters>) and parent [parent=<label>] (parent is the current frame)
 fi: make adder func adder(k) [parent=f1]
- Set the body of that function to be everything indented after the first line
- 3. Bind <name> to that function in the current frame

Rules for calling user-defined functions:

- 1. Create a new environment frame
- Copy the parent of the function to the local frame: [parent=<label>]
- 3. Bind the function's parameters to its arguments in that frame
- 4. Execute the body of the function in the new environment

Function Composition



Application: Currying

- $\boldsymbol{\cdot}$ add is a two-argument function that returns the sum of the two arguments
- make_adder is a one-argument function that returns a oneargument function that returns the sum of the two arguments
- \cdot Currying allows us to represent functions with multiple variables as chains of functions with single variables
- It is named after mathematician and logician Haskell Brooks Curry (who rediscovered it after Moses Schönfinkel)

(lambda x, y: x * y + 1)(3, 4) (lambda x: lambda y: x * y + 1)(3)(4)