## Midterm Review

**CS61A Summer 2016** 

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# Announcements

- Time: 5:00PM to 8:00PM, Thursday, 7/14
- Place: 2050 VLSB (right here!)
- Check <a href="https://piazza.com/class/ipkfex1ne3p56y?cid=773">https://piazza.com/class/ipkfex1ne3p56y?cid=773</a>
- You can bring an 8.5"x 11" cheat sheet, front and back
- These slides will be posted on Piazza

#### The Plan...



# **Topics**

- Environment diagrams
- While loops and for loops
- Higher order functions
- Lambda functions
- Recursion and tree recursion

- Orders of growth
- Lists & sequences
- Data abstraction
- Linked lists
- Trees

# **Environment Diagrams**

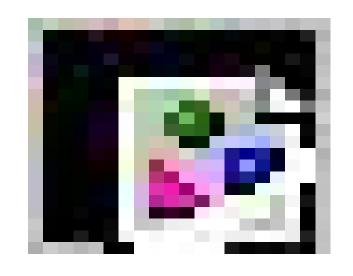
# Name of frame should be intrinsic name of function

```
def f():
    ...
def g():
    ...
f = g
f()
```

What is the name of the frame created by the last line?

#### Lambda functions are defined when...

```
def f(g):
    y = 2
    return g(2)
y = 1
print(f(lambda x: x + y))
```



What number is printed?

3

What is the parent of the lambda function?

Global

# **Environment Diagram Question**

```
def marvin(brain):
   cs61a = midterm+2
   return cs61a + brain(midterm+1)
def tammy(marvin):
   marvin, midterm = marvin+2, marvin+1
   return midterm // cs61a
midterm, cs61a = 3, 2
marvin(tammy)
```

## Python Tutor

## **Environment Diagram Pitfalls**

- 1. Name of frame should be **intrinsic** name of function
- 2. Lambda functions are defined where they are evaluated
- 3. Parent frame of a function never changes once you write it down
- 4. Don't conflate: function name vs. function call
- 5. Calling a function
  - a. Evaluate the operator (usually a lookup)
  - b. Evaluate the operands
  - c. Apply the operator on the operands (this is where you actually call the function and make a new frame)

# Lists and sequences

# **List and Sequences Pitfalls**

1. Whenever you see a negative number, like -n, just replace it with len(lst) - n

```
lst[-3] == lst[len(lst)-3]
lst[-2:3] == lst[len(lst)-2:3]
```



- 2. In list slicing, if you go out of bounds, you DON'T error, you just return as much as you can
- 3. List slicing ALWAYS returns a list

## **Deep Length**

The function deep\_len takes a deep list as input and returns the deep length of the list. Fill in the blanks.

```
def deep_len(lst):
11 11 11
>>> deep len([1, 2, 3]) # normal list
                                            if not 1st:
                                               return __ 0
>>> x = [1, [2, 3], 4] \# deep list
                                           elif type(lst[0]) == list:
>>> deep len(x)
                                                      deep len(lst[0]) +
                                               return deep_len(lst[1:])
>>> x = [[1, [1, 1]], 1, [1, 1]]
>>> deep len(x)
                                           else:
6
                                               return1 + deep_len(lst[1:])
11 11 11
```

# Higher Order Functions

# How are the following pieces of code different?

What would Python display for each?

```
t = "surprise!"
def outer(t):
    def inner():
        print(t)
    return inner
outer("boo!")()
```

```
t = "surprise!"
def inner():
    print(t)
def outer(t):
    return inner
outer("boo!")()
```

# Draw env diagrams to see what's different!

#### **PythonTutor**

# Fun Multiply

```
667777
>>> def func_a(num):
        return num + 1
>>> func_b1 = fun_mult(func_a, 3)
>>> func_b1(2)
4
>>> func_b2 = fun_mult(func_a, -2)
>>> func_b2(-3)
>>> func_b3 = fun_mult(func_a, -1)
>>> func_b3(4)
>>> func_b4 = fun_mult(func_a, 0)
>>> func_b4(3)
6
>>> func_b5 = fun_mult(func_a, 1)
>>> func_b5(4)
24
11 11 11
```

Fill in the blanks so that the doctests pass.

def fun\_mult(func\_a, start):

def func\_b(stop): i = **start** product = 1if start < 0: None return if start > stop: return func\_a(start) while i < stop: product = product \* func\_a(i) i += 1 return **product** return func b

# **Higher Order Functions Pitfalls**

- 1. Function name vs. function call
- 2. Parent of the function is the frame in which the function was defined
- 3. Don't be freaked out by things like f(3)(2)(6)

# Recursion and Tree Recursion

#### **Recursive Remove**

```
def remove (n , digit ):
    11 11 11
   Return a number that is identical to n, but with all instances
   of digit removed. Assume that DIGIT is a positive integer less
   than 10.
   66 22 22
   if n == 0:
       return 0
   if n % 10 == digit:
       return remove(n // 10, digit)
   else:
       return n % 10 + 10 * remove(n // 10, digit)
```

#### **FooBar**

```
Write the function foobar that behaves as follows:
>>> foobar(0)
"foo"
                                         def foobar(n):
>>> foobar(1)
                                            if n == 0:
"foobar"
                                              return "foo"
>>> foobar(2)
                                            elif n \% 3 == 0:
"foobarbar"
                                              return foobar(n-1) + "foo"
>>> foobar(3)
                                            else:
"foobarbarfoo"
                                              return foobar(n-1) + "bar"
>>> foobar(4)
"foobarbarfoobar"
>>> foobar(14)
"foobarbarfoobarbarfoobarbarfoobarbar"
```

#### **Recursion Pitfalls**

- 1. **PLEASE** consider the TYPE of input and output to the function
- 2. A recursive function must **ALWAYS** return a value of the same type!!!
  - a. **BAD**: returning first(link) when you should return a linked list
- 3. Take the leap of faith! Be confident thought is recursive. Assume your solution is correct and you'll be correct. Assume your solution fails and you will fail.
- 4. The input to the recursive call MUST be closer to the base case
  - a. Otherwise, you get stuck in recursive calls forever!

# Addup

```
Write a function that takes as input a
number n and a list of numbers 1st and
returns True if we can find a subsequence of
Ist that sums up to n
>>> addup(10, [1, 2, 3, 4, 5])
True
>>> addup(8, [1, 2, 3, 4, 5])
True
>>> addup(-1, [1, 2, 3, 4, 5])
False
>>> addup(100, [1, 2, 3, 4, 5])
False
```

```
def addup(n, lst):
    if n == 0:
        return True
    if lst == \Gamma 1:
        return False
    else:
        first, rest = lst[0], lst[1:]
        return addup(n-first, rest) or \
              addup(n, rest)
```

## **Tree Recursion Tips**

- 1. LOOK AT the TYPE of input and output to the function
  - a. BAD: calling f(children(tree)) when f takes in a tree
- 2. A recursive function must ALWAYS return a value of the same type!!!
- 3. Think of the *logic* of the function, think of what the function *should* return, **take the leap of faith**!

# Orders of growth

# **Orders of Growth Tips**

- 1. There is no sure and fast way to determine the order of growth of a function.
- 2. Read the function definition carefully and make sure you understand exactly what the function is doing.

### Find the Orders of Growth

return sum

```
def f(n):
   if not not False:
       return
                                       def fun(x):
                          Constant!
   else:
                                            for i in range(x):
       return f(n - 1)
                                                for j in range(x * x):
                                                    if j == 4:
def belgian waffle(n):
                                                        return -1
   i = 0
                                                    print("fun!")
   sum = 0
   while i < n:
                                                    Constant!
       for j in range (n**2):
           sum +=1
                             n^3
       i += 1
```

# **Linked Lists**

#### Count

Define a function count which takes in a linked list, lnk, and a list of numbers, nums, and returns the number of values in nums that appear in lnk Assume that all entries in nums are distinct.

```
[Hint: practice your list comprehensions! :)]
def count(lnk, nums):
    if lnk == empty:
        return 0
    if first(lnk) in nums:
        return 1 + count(rest(lnk),\
                             [x for x in nums if x != first(lnk)])
    return count(rest(lnk), nums)
```

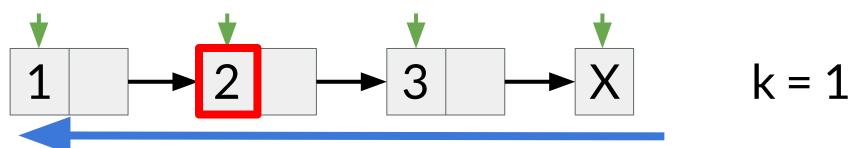
#### Kth to Last.

Write a function that returns the kth to last element of a linked list.

```
def kth_to_last(l):
   11 11 11
   >>> lst = link(1, link(2, link(3)))
   >>> kth_to_last(lst, 0)
   3
   >>> kth_to_last(lst, 1)
   >>> print(kth_to_last(lst, 5))
   None
   11 11 11
```

## Here's an approach

Recurse until you hit the empty list



Once k is 0, you must return the first element of the current list

When you return back to the front of the list through your recursive calls, decrement k by 1

#### Kth to Last.

```
def kth_last(lst, k):
   def unwind_rewind(lst):
      if lst == empty:
         return k, None
      previous_k, kth_element = unwind_rewind(rest(lst))
      if previous_k == 0:
         return previous_k - 1, first(lst)
      else:
         return previous_k - 1, kth_element
    return unwind_rewind(lst)[1]
```

# Trees

### **Tree Tips**

- 1. Children of a tree is a list of trees
- 2. Recursive calls go vertically in the tree, for loops go horizontally

# Find and Replace

kept\_children = []

for c in children(t):

if entry(t) == old:

Implement the function find\_and\_replace which takes in a tree t, and two values, old and new. The function returns a tree that is identical to the original, but with all instances of old replaced with new.

```
def find_and_replace(t, old, new):
```

```
Whole words only
                                          More Options ₹
                                                            Close
   kept_children += [find_and_replace(c, old, new)]
   return tree(new, kept_children)
return tree(entry(t), kept_children)
```

Eind Find All

Replace

ind & Replace

Search for

Replace with

Match case

# **Binary Tree**

Write a function that takes in a tree, t, and returns True if every node has at most two children and False otherwise.

```
def is_binary_tree(t):
    if len(children(t)) > 2:
        return False
    final_result = True
    for c in children(c):
        final_result = final_result and is_binary_tree(c)
    return final_result
```

# Thanks for coming!



Good luck on the midterm!