

Lecture 17: Mutable Linked Lists

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Announcements

- Homework 6 is due today at 11:59pm
- Project 3 is due 7/26 at 11:59pm
 - Earn 1 EC point for completing it by 7/25
- Quiz 5 tomorrow at the beginning of lecture
 - May cover mutability, OOP I (Monday)
- Project 1 revisions due 7/27 at 11:59pm

Roadmap

Introduction

Functions

Data

Mutability

Objects

Interpretation

Paradigms

Applications

- This week (Objects), the goals are:
 - To learn the paradigm of *object-oriented programming*
 - To study applications of, and problems that can be solved using, OOP

Practical OOP

Checking Types (and Accounts) (demo)

- We often check the type of an object to determine what operations it permits
- The **type** built-in function returns the class that its argument is an instance of
- The **isinstance** built-in function returns whether its first argument (object) is an instance of the second argument (class) *or a subclass*
- `isinstance(obj, cls)` is usually preferred over `type(obj) == cls`

```
>>> a = Account('Brian')
>>> ch = CheckingAccount('Brian')

>>> type(a) == Account
True
>>> type(ch) == Account
False
>>> type(ch) == CheckingAccount
True

>>> isinstance(a, Account)
True
>>> isinstance(ch, Account)
True
>>> isinstance(a, CheckingAccount)
False
>>> isinstance(ch, CheckingAccount)
True
```

Python's Magic Methods (demo)

- How does the Python interpreter display values?
 - First, it evaluates the expression to some value
 - Then, it calls `repr` on that value and prints that string
- How do magic methods work?
- Are integers objects too? (Yep!)
- Are _____ objects too? (Yep!)

```
>>> x = Rational(3, 5)
>>> y = Rational(1, 3)
>>> y
Rational(1, 3)
>>> repr(y)
'Rational(1, 3)'
>>> print(repr(y))
Rational(1, 3)
>>> x * y
Rational(1, 5)
>>> x.__mul__(y)
Rational(1, 5)
```

Linked Lists

The Link Class

```
empty = 'X'

def link(first, rest=empty):
    return [first, rest]

def first(lnk):
    return lnk[0]

def rest(lnk):
    return lnk[1]

>>> link_adt = link(1,
                      link(2,
                            link(3)))
>>> first(rest(link_adt))
2
```

```
class Link:
    empty = ()

    def __init__(self, first,
                 rest=empty):
        self.first = first
        self.rest = rest

>>> link_cls = Link(1,
                     Link(2,
                           Link(3)))
>>> link_cls.rest.first
2
```

Mutable Linked Lists

(demo)

- Instances of user-defined classes are mutable *by default*

```
class Link:  
    empty = ()  
  
    def __init__(self, first, rest=empty):  
        self.first = first  
        self.rest = rest  
  
    def __repr__(self):  
        if self.rest is Link.empty:  
            return 'Link({0})'.format(  
                self.first)  
        else:  
            return 'Link({0}, {1})'.format(  
                self.first, repr(self.rest))
```

Linked Lists are Sequences

(demo)

Sneaky recursive call:
equivalent to
`self.rest.__getitem__(i-1)`

Another sneaky recursive
call: equivalent to
`self.rest.__len__()`

Where's the base case??

```
class Link:
    empty = ()
    ...
    def __getitem__(self, i):
        if i == 0:
            return self.first
        elif self.rest is Link.empty:
            raise IndexError('...')
        else:
            return self.rest[i - 1]
    def __len__(self):
        return 1 + len(self.rest)
```

The `__setitem__` Magic Method (demo)

```
>>> s = Link(1, Link(2, Link(3)))
>>> s[1] = 3
>>> s
Link(1, Link(3, Link(3)))
```

```
class Link:
    ...
    def __setitem__(self, i, val):
        if i == 0:
            self.first = val
        elif self.rest is Link.empty:
            raise IndexError('...')
        else:
            self.rest[i - 1] = val
```

Mutating Map

(demo)

```
>>> s = Link(1, Link(2, Link(3)))
>>> s.map(lambda x: x * x)
>>> s
Link(1, Link(4, Link(9)))
```

```
class Link:
    ...
    def map(self, f):
        for i in range(len(self)):
            self[i] = f(self[i])
```

Runtime?

Mutating Map

```
>>> s = Link(1, Link(2, Link(3)))           self[0] = f(self[0])
>>> s.map(lambda x: x * x)
>>> s
Link(1, Link(4, Link(9)))                 self[1] = f(self[1])
```

```
class Link:                                self[2] = f(self[2])
    ...
    def __getitem__(self, i):
        if i == 0:
            return self.first
        else:                               ...
            return self.rest[i - 1]
    ...
    def map(self, f):                    self[n-1] = f(self[n-1])
        for i in range(len(self)):
            self[i] = f(self[i])          Θ(n2)
```

Mutating Map (Improved) (demo)

```
>>> s = Link(1, Link(2, Link(3)))
>>> s.map(lambda x: x * x)
>>> s
Link(1, Link(4, Link(9)))
```

Runtime?

```
class Link:
    ...
    def map(self, f):
        self.first = f(self.first)
        if self.rest is not Link.empty:
            self.rest.map(f)
```

$\theta(n)$

contains and in

(demo)

```
class Link:  
    ...  
    def __contains__(self, e):  
        return self.first == e or e in self.rest  
  
>>> s = Link(1, Link(2, Link(3)))  
>>> 2 in s  
True  
>>> 4 in s  
False
```

Break!

Environments

Environment Frames

- An environment is a sequence of frames
 - Each frame has some data (bindings) and a parent, which points to another frame
- A linked list is a sequence of values
 - Each link has some data (first) and a rest, which points to another link
- An environment is just a special case of a linked list!

Environment Frames

(demo)

- An environment is a sequence of frames
 - Each frame has some data (**bindings**) and a **parent**, which points to another **frame**
- A linked list is a sequence of values
 - Each link has some data (**first**) and a **rest**, which points to another **link**
- An environment is just a special case of a linked list!

The Call Stack

(demo)

- A *stack* is a data structure that permits two operations
 - Add to the top of a stack ("push")
 - Remove from the top of a stack ("pop")
- Two new Link operations required: `insert_front` and `remove_front`
- A *call stack* keeps track of frames that are currently open
 - Calling a function adds a new frame to the stack
 - Returning from a function removes that frame from the stack
 - The current frame is always on the top of the stack



Python

Brython

- What if we could have Python functions use the environment frames and the call stack that we just defined?
- Two important parts:
 - What should happen when **defining** a Brython function?
 - What should happen when **calling** a Brython function?



Function Definitions

- What happens in a function definition?
 - Determine the current frame of execution: this is the function's parent frame
 - Bind the function name to the function value

Function Calls

(demo)

- What happens in a function call?
 - Create a brand new call frame (using the function parent as the parent of that frame) and insert it into the stack
 - Bind function's parameters to arguments
 - Execute the function in the environment of the call frame
 - Remember: the current frame is at the top of the stack
 - After executing the function, remove the frame from the stack

Summary

- Linked lists are one way to store sequential data
- An object-based implementation of the linked list abstraction allows for easy mutability
 - No more crazy nonlocal stuff!
- Implementing magic methods lets us hook into convenient Python syntax and built-in functions
- Linked lists can be used to implement some of the core ideas of this course!