

Lecture 21: Interpreters I

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07/27/2016

Announcements

Roadmap

Introduction

Functions

Data

Mutability

Objects

Interpretation

Paradigms

Applications

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Applications

- This week (Interpretation), the goals are:

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 - To learn a new language, Scheme, in two days!

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Applications

- This week (Interpretation), the goals are:
 - To learn a new language, Scheme, in two days!
 - To understand how interpreters work, using Scheme as an example

Programming Languages

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Python 3

```
def square(x):  
    return x * x
```

```
from dis import dis  
dis(square)
```

Python 3 Bytecode

```
LOAD_FAST          0 (x)  
LOAD_FAST          0 (x)  
BINARY_MULTIPLY  
RETURN_VALUE
```

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 - *Specification* of the syntax and semantics of the language
 - *Canonical implementation* of either a compiler or interpreter for the language

The Scheme Interpreter

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- An interpreter for Scheme must take in text (Scheme code) as input and output the values from interpreting the text

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- The job of the parser is to take in text and perform *syntactic analysis* to convert it into expressions that the evaluator can understand
- The job of the evaluator is to read in expressions and perform *semantic analysis* to evaluate the expressions and output the corresponding values

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calc> (/ (+ 8 7) 5)
```

```
3.0
```


Calculator

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calc> (/ (+ 8 7) 5)  
3.0
```

```
calc> (+ (* 3  
          (+ (* 2 4)  
              (+ 3 5)))  
        (+ (- 10 7)  
            6))
```

Parsing

From text to expressions

Parsing

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- The parser converts text into expressions

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Text

Expressions



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Text

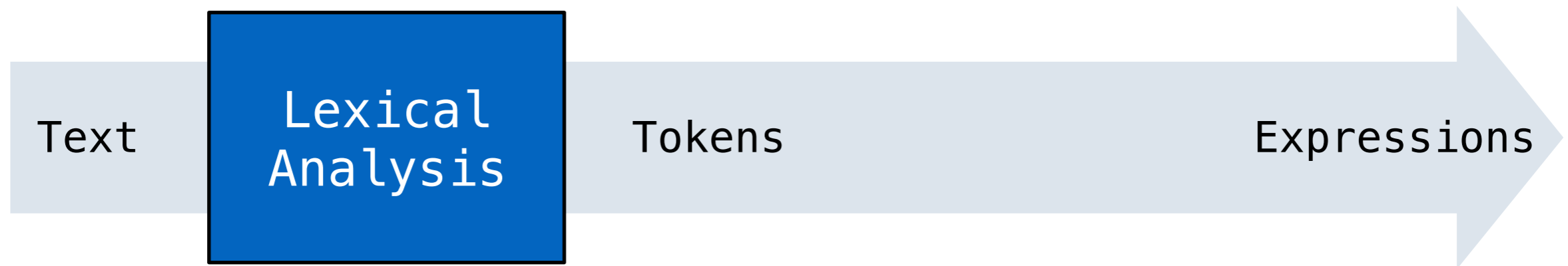
Tokens

Expressions



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'(+ 1'

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'(+ 1'
' (- 23)'

Parsing

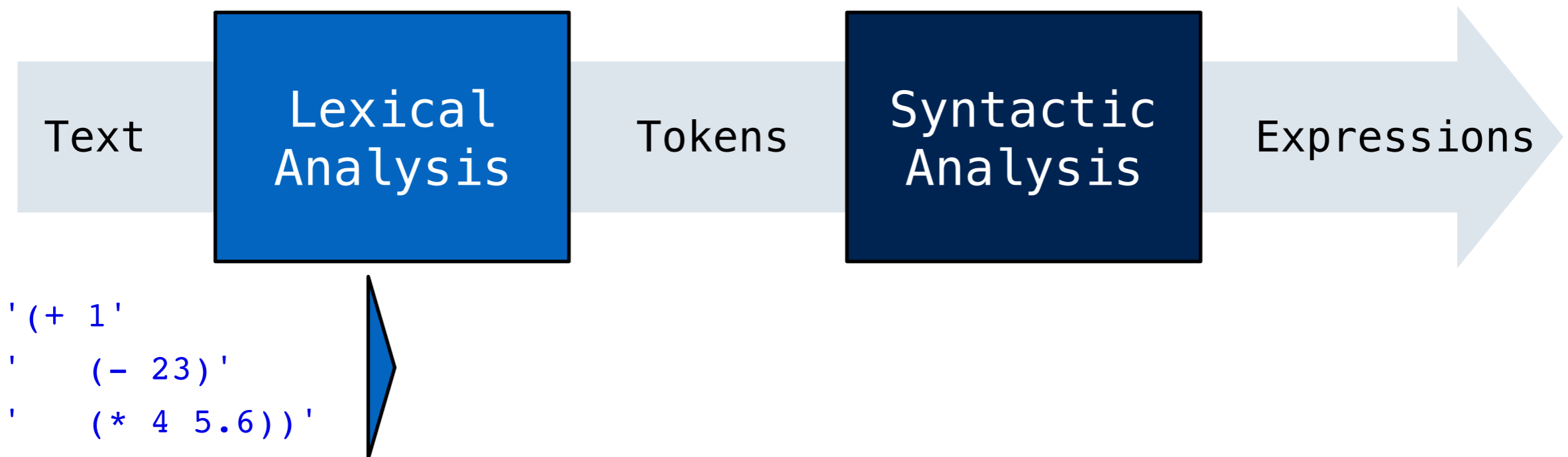
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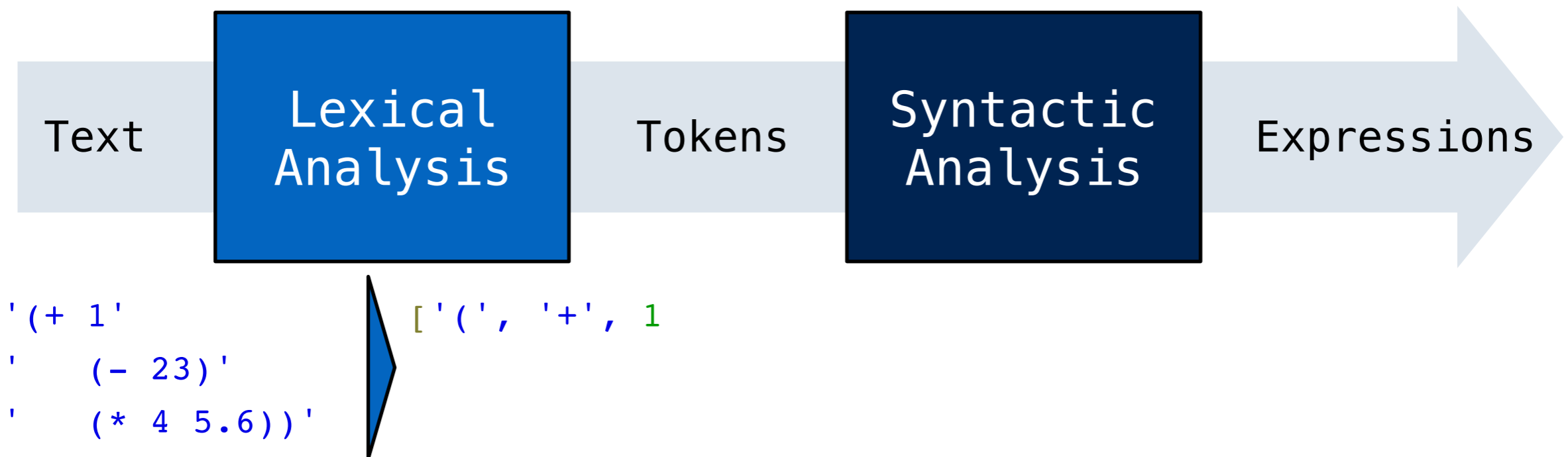
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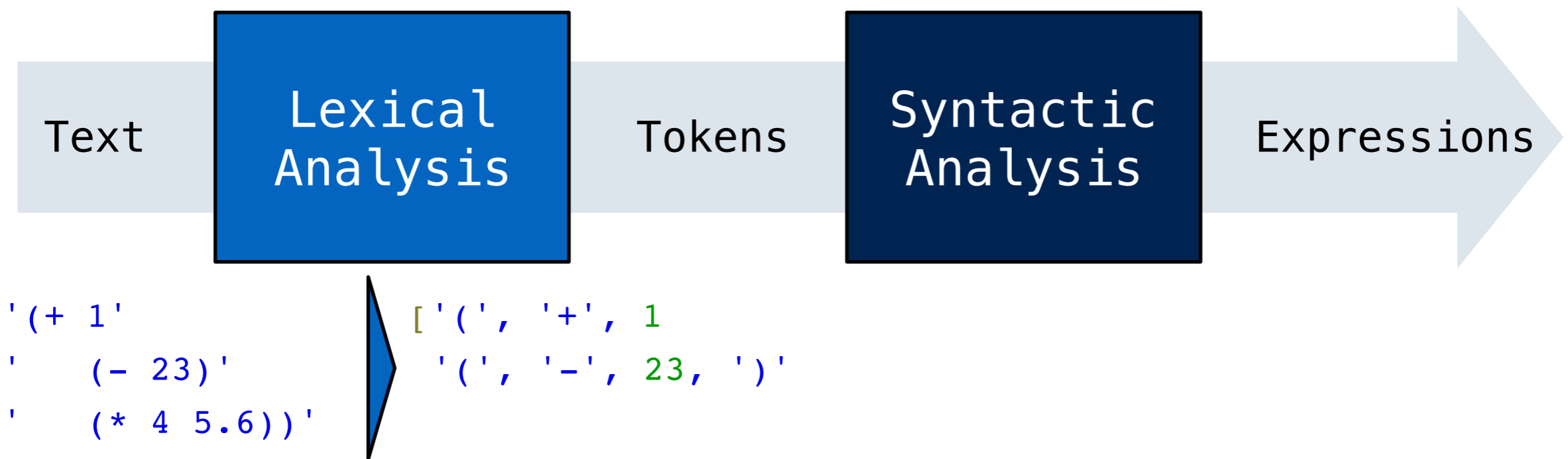
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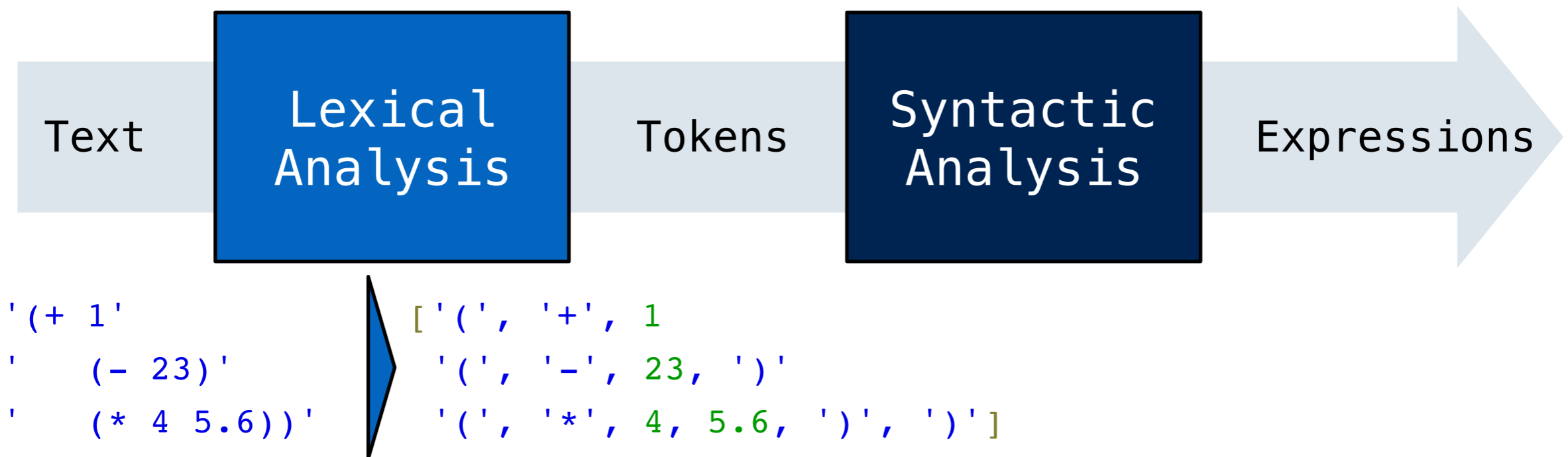
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' (- 23) '  
' (* 4 5.6)) '  
['(', '+', 1  
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- Iterative process

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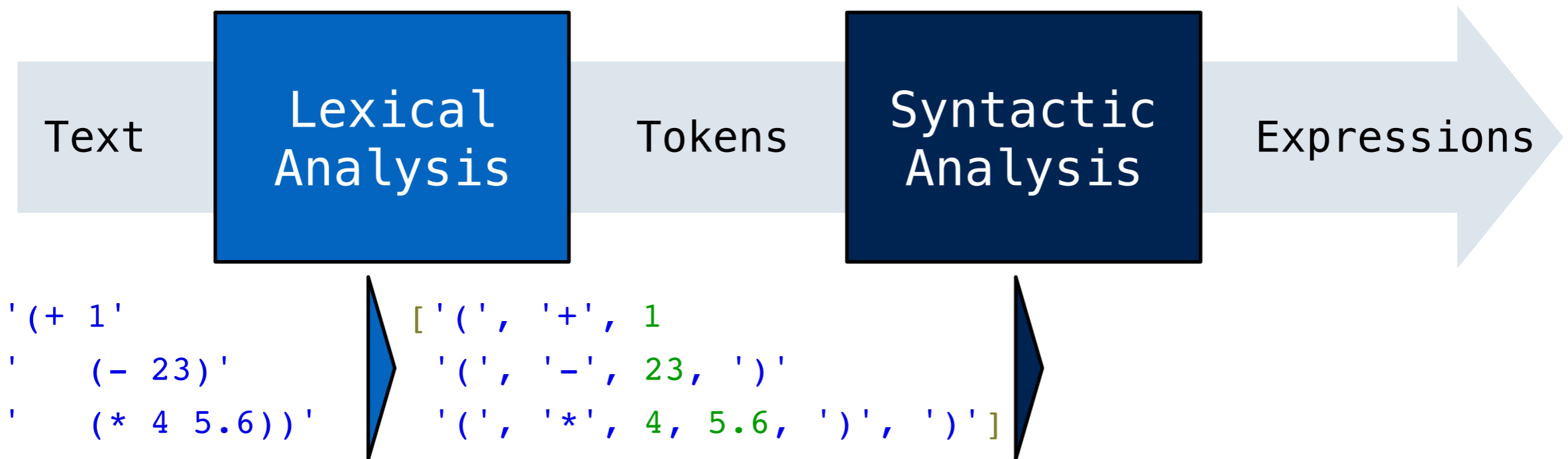


```
'(+ 1'  
' (- 23) '  
' (* 4 5.6) ) '  
[ '(' , '+' , 1  
' (' , '-' , 23 , ')' '  
' (' , '*' , 4 , 5.6 , ')' , ')' ' ]
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- Iterative process
- Checks number of parentheses
- Checks for malformed tokens
- Determines types of tokens

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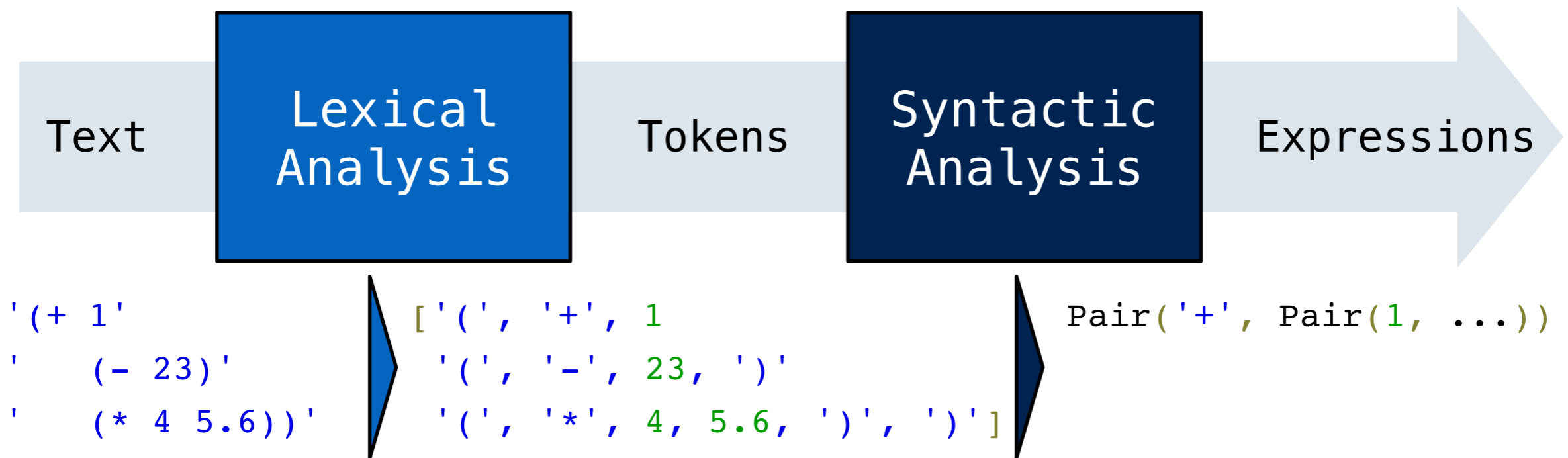
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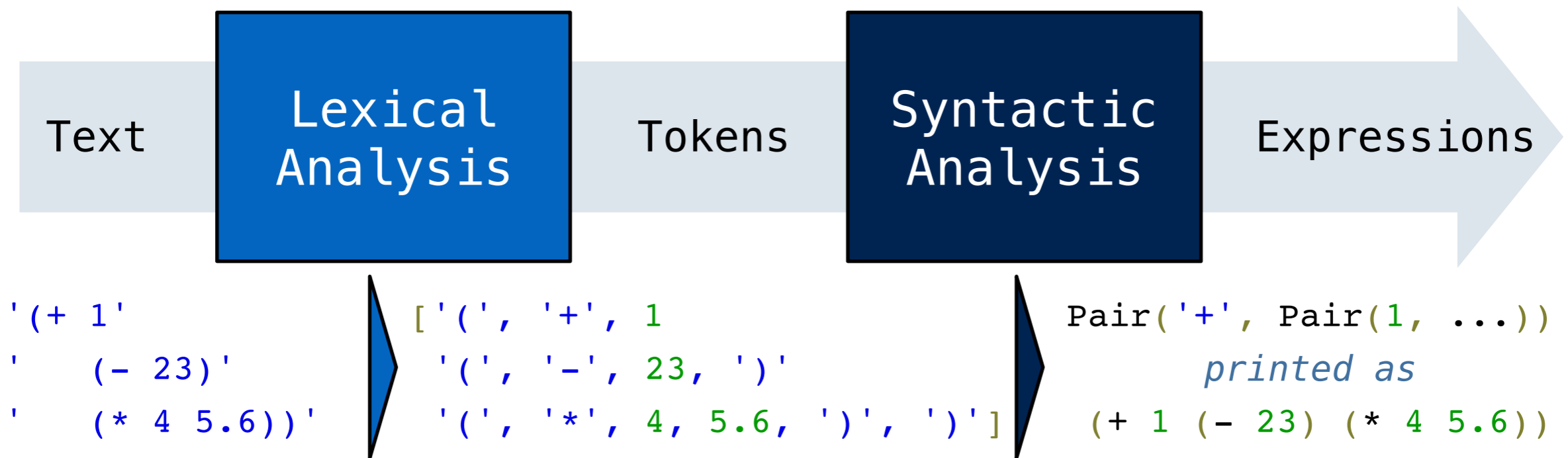
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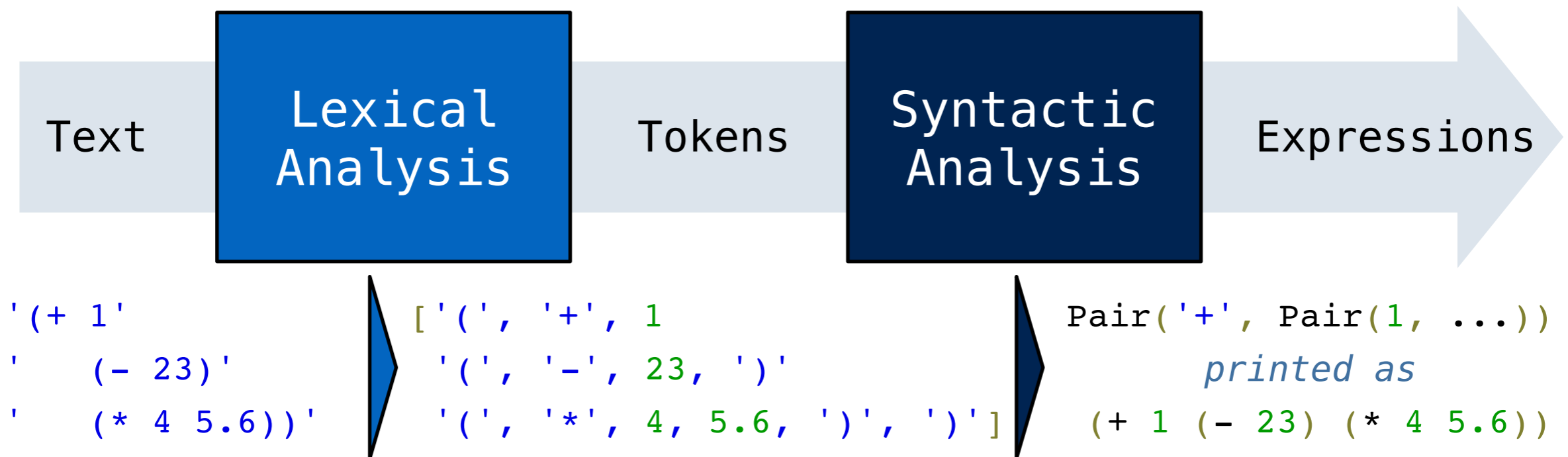
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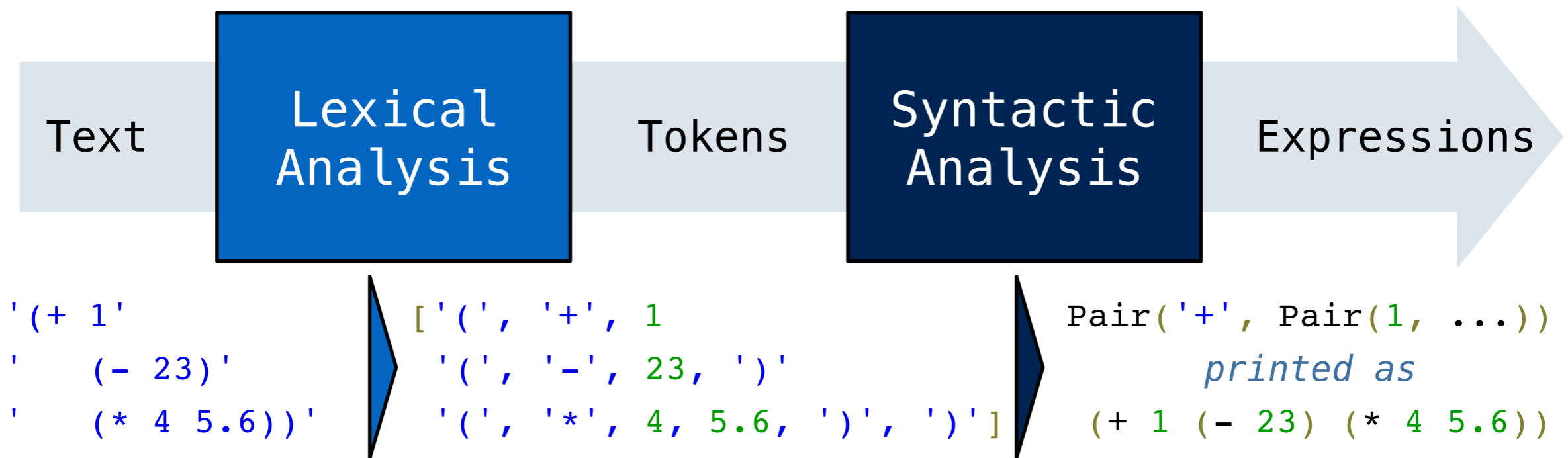


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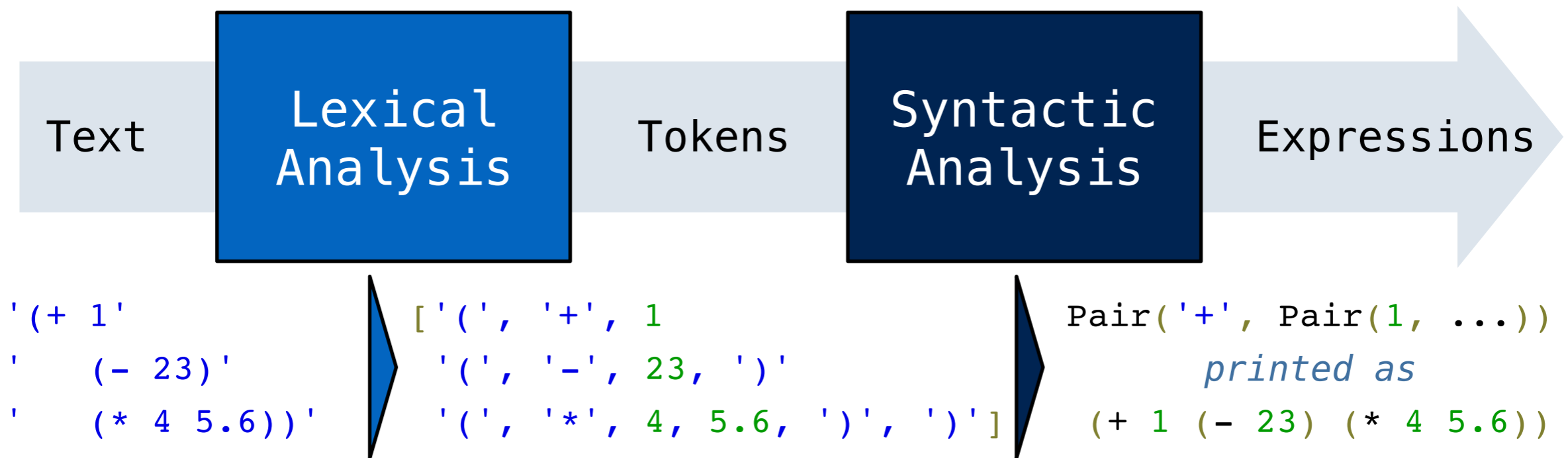


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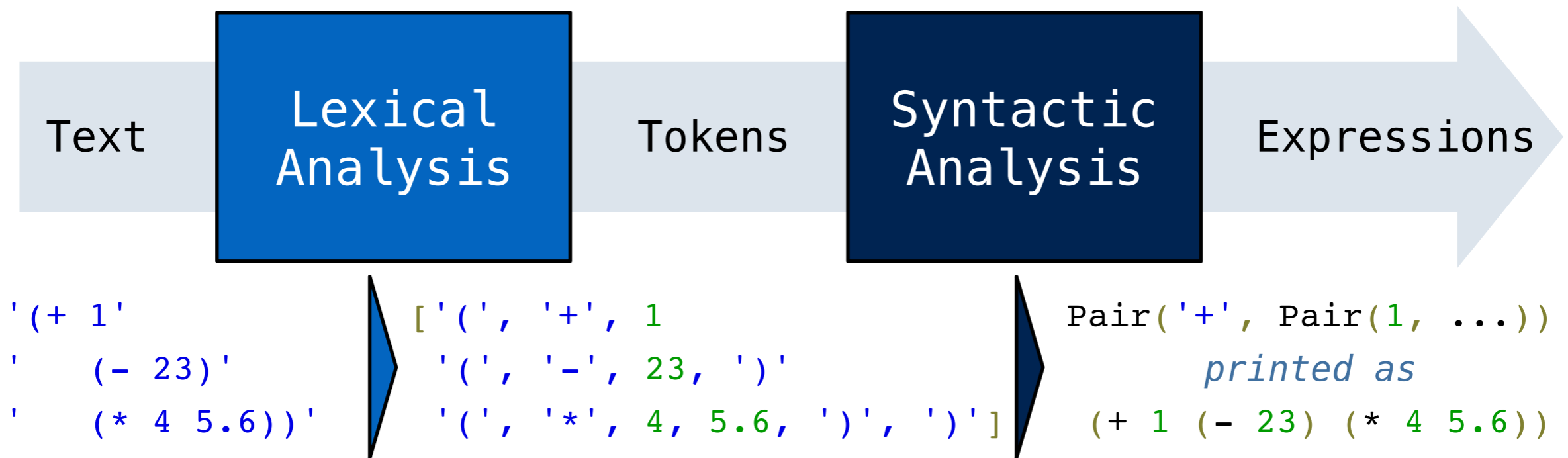


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- Returns expression as a Pair

Lexical Analysis

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Resulting expression: (+ 1 (- 23))
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Evaluation

From expressions to values

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 2. *Evaluate* the operands to get its values

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        return calc_apply(calc_eval(exp.first),
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 - With user-defined functions, the apply function has to call the evaluate function! This mutual recursion is called the *eval-apply loop*

Putting it all together

A Calculator interactive interpreter!

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 - The evaluator takes in an expression and outputs the corresponding value
 - The *read-eval-print loop* completes our interpreter