

# MUTABLE FUNCTIONS AND MIDTERM REVIEW 6

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COMPUTER SCIENCE 61A

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## 1 Nonlocal

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Until now, you've been able to access variables in parent frames, but you have not been able to modify them. The `nonlocal` keyword can be used to modify a variable in the parent frame outside the current frame. For example, consider `stepper`, which uses `nonlocal` to modify `num`:

```
def stepper(num) :  
    def step() :  
        nonlocal num # declares num as a nonlocal variable  
        num = num + 1 # modifies num in the stepper frame  
        return num  
    return step
```

However, there are two important caveats with `nonlocal` variables:

- **Global variables** cannot be modified using the `nonlocal` keyword.
- **Variables in the current frame** cannot be overridden using the `nonlocal` keyword.

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## 1.1 Environment Diagrams

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1. Draw the environment diagram for the code below:

```
def stepper(num):  
    def step():  
        nonlocal num  
        num = num + 1  
        return num  
    return step
```

```
s = stepper(3)  
s()  
s()
```

2. Given the definition of `make_shopkeeper` below, draw the environment diagram.

```
def make_shopkeeper(total_gold):  
    def buy(cost):  
        nonlocal total_gold  
        if total_gold < cost:  
            return 'Go farm some more champions'  
        total_gold = total_gold - cost  
        return total_gold  
    return buy
```

```
infinity_edge, zeal, gold = 3800, 1100, 3800  
shopkeeper = make_shopkeeper(gold - 1000)  
shopkeeper(zeal)  
shopkeeper(infinity_edge)
```

## 1.2 Some Common Misconceptions

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1. What is wrong with the following code?      2. What is wrong with the following code?

```
a = 5
def another_add_one():
    nonlocal a
    a += 1
another_add_one()
```

```
def adder(x):
    def add(y):
        nonlocal x, y
        x += y
        return x
    return add
adder(2)(3)
```

## 1.3 Fill in the Blank

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1. The bathtub below simulates an epic battle between Finn and Kylo Ren over a populace of rubber duckies. Fill in the body of `ducky` so that all doctests pass.

```
def bathtub(n):
    """
    >>> annihilator = bathtub(500) # the force awakens...
    >>> kylo_ren = annihilator(10)
    >>> kylo_ren()
    490 rubber duckies left
    >>> finn = annihilator(-20)
    >>> finn()
    510 rubber duckies left
    >>> kylo_ren()
    500 rubber duckies left
    """
    def ducky_annihilator(rate):
        def ducky():
            # your code here

        return ducky
    return ducky_annihilator
```

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## 2 Midterm Review

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### 2.1 Environment Diagrams

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1. Draw the environment diagram that results from executing the code below.

```
def this(x):  
    return 2*that(x)
```

```
def that(x):  
    x = y + 1  
    this = that  
    return x
```

```
x, y = 1, 2  
this(that(y))
```

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## 2.2 Lambdas

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1. Fill in the blanks with one-line lambda expressions so that each call expression that follows returns 3.

```
>>> f1 = _____
>>> f1 ()
3
```

```
>>> f2 = _____
>>> f2 () ()
3
```

```
>>> f3 = _____
>>> f3 () (3)
3
```

```
>>> f4 = _____
>>> f4 () () (3) ()
3
```

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## 2.3 Lists and List Comprehension

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1. Write a function that rotates the elements of a list to the right by  $k$ . Elements should not "fall off"; they should wrap around the beginning of the list. `rotate` should return a new list. To make a list of  $n$  0's, you can do this: `[0] * n`

```
def rotate(lst, k):
    """ Return a new list, with the same elements
        of lst, rotated to the right k.
    """
    >>> x = [1, 2, 3, 4, 5]
    >>> rotate(x, 3)
    [3, 4, 5, 1, 2]
    """
```

2. Define a function `foo` that takes in a list `lst` and returns a new list that keeps only the even-indexed elements of `lst` and multiplies each of those elements by the corresponding index.

```
def foo(lst):
```

```
    """
```

```
    >>> x = [1, 2, 3, 4, 5, 6]
```

```
    >>> foo(x)
```

```
    [0, 6, 20]
```

```
    """
```

```
    return [_____]
```

3. Implement the functions `max_product`, which takes in a list and returns the maximum product that can be formed using nonconsecutive elements of the list. The input list will contain only numbers greater than or equal to 1.

```
def max_product(lst):
```

```
    """Return the maximum product that can be formed using lst
    without using any consecutive numbers
```

```
    >>> [10, 3, 1, 9, 2] # 10 * 9
```

```
    90
```

```
    """
```

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## 2.4 Trees

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1. An **expression tree** is a tree that contains a function for each non-leaf root, which can be either '+' or '\*'. All leaves are numbers. Implement `eval_tree`, which evaluates an expression tree to its value. You may want to use the functions `sum` and `prod`, which take a list of numbers and compute the sum and product respectively.

```
def eval_tree(tree):  
    """Evaluates an expression tree with functions as root  
>>> eval_tree(tree(1))  
1  
>>> expr = tree('*', [tree(2), tree(3)])  
>>> eval_tree(expr)  
6  
>>> eval_tree(tree('+', [expr, tree(4)]))  
10  
"""
```