## COMPUTER SCIENCE 61A

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# 1 Linked Lists in OOP

## 1.1 A New Implementation

Linked lists are data abstractions that can have multiple implementations. Previously, we saw linked lists implemented using Python lists. Today, we will look at linked lists implemented using Object-Oriented Programming. Here it is:

```
class Link:
```

```
empty = ()
def __init__(self, first, rest=empty):
    assert rest is Link.empty or isinstance(rest, Link)
    self.first = first
    self.rest = rest
def __getitem__(self, i):
    if i == 0:
        return self.first
    return self.rest[i-1]
def __len__(self):
    return 1 + len(self.rest)
```

When we implemented linked lists using Python lists, we called first (lnk) and rest (lnk) to access the first and rest elements. This time, we can write lnk.first and lnk.rest instead. In the former, we could access the elements, but we could not modify them. In the latter, we can access and also modify the elements. In other words, linked lists implemented using OOP is mutable.

In addition to the constructor \_\_init\_\_, we have the special Python methods \_\_getitem\_\_ and \_\_len\_\_. Note that any method that begins and ends with two underscores is a special Python method. Special Python methods may be invoked using built-in functions and special notation. The built-in Python element selection operator, as in lst[i], invokes lst.\_\_getitem\_\_(i). Likewise, the built-in Python function len, as in len(lst), invokes lst.\_\_len\_\_().

### 1.2 Questions

1. Write sum\_nums, which takes in a linked list lnk and sums up all elements in lnk. You may assume all elements in lnk are integers. sum\_nums should return the sum, an integer.

```
def sum_nums(lnk):
    """
    >>> a = Link(1, Link(6, Link(7)))
    >>> sum_nums(a)
    14
    """
```

2. Write multiply\_lnks, which takes in a Python list of Link objects and multiplies them element-wise. It should return a new linked list. If not all of the Link objects are of equal length, return a linked list whose length is that of the shortest linked list given. You may assume the Link objects are shallow linked lists, and that lst\_of\_lnks contains at least one linked list.

```
def multiply_lnks(lst_of_lnks):
    """

    >>> a = Link(2, Link(3, Link(5)))
    >>> b = Link(6, Link(4, Link(2)))
    >>> c = Link(4, Link(1, Link(0, Link(2))))
    >>> p = multiply_lnks([a, b, c])
    >>> p.first
    48
    >>> p.rest.first
    12
    >>> p.rest.rest.rest
    ()
    """
```

#### 1.3 Extra Questions

1. Define reverse, which takes in a linked list and reverses the order of the links. The function may *not* return a new list; it must mutate the original list. Return a pointer to the head of the reversed list.

```
def reverse(lnk):
    """
    >>> a = Link(1, Link(2, Link(3)))
    >>> r = reverse(a)
    >>> r.first
    3
    >>> r.rest.first
    2
    """
```

2. Write a function remove\_duplicates that takes as input a sorted linked list of integers, lnk, and mutates lnk so that all duplicates are removed.

```
def remove_duplicates(lnk):
    """

>>> lnk = Link(1, Link(1, Link(1, Link(5)))))
>>> unique = remove_duplicates(lnk)
>>> len(unique)
2
>>> len(lnk)
2
"""
```

### 2.1 Another New Implementation

Trees are also data abstractions that can have multiple implementations. Previously, we implemented the tree abstraction using Python lists. Let's look at another implementation using objects instead. With this implementation, we can easily specify specialized tree types, such as binary trees, using inheritance.

```
class Tree:
    def __init__(self, entry, children=[]):
        for c in children:
            assert isinstance(c, Tree)
        self.entry = entry
        self.children = children

def is_leaf(self):
    return not self.children
```

Notice that with this implementation we can mutate the entry of a tree by reassigning tree.entry. In the previous implementation using lists, this was not possible, because the abstraction barrier prevented us from seeing how the tree was implemented.

#### 2.2 Questions

1. Consider the following definitions and assignments and determine what Python would output for each of the calls below *if they were evaluated in order*.

```
>>> t0 = Tree(0)
>>> t0.entry

>>> t0.children

>>> t1 = Tree(0, [1, 2]) #Is this a valid tree?

>>> t2 = Tree(0, [Tree(1), Tree(2, [Tree(3)])])
>>> t2.children[0]

>>> t2.children[1].children[0].entry
```

2. Define a function make\_even which takes in a tree t whose entries are integers, and mutates the tree such that all the odd integers are increased by 1 and all the even integers remain the same.

```
def make_even(t):
    """"
    >>> t = Tree(1, [Tree(2, [Tree(3)]), Tree(4), Tree(5)])
    >>> make_even(t)
    >>> t.entry
    2
    >>> t.children[0].children[0].entry
    4
    """"
```

#### 2.3 Extra Question

1. Write a function that combines the entries of two trees t1 and t2 together with the combiner function. Assume that t1 and t2 have identical structure. This function should return a new tree.

```
def combine_tree(t1, t2, combiner):
    """

>>> a = Tree(1, [Tree(2, [Tree(3)])])
>>> b = Tree(4, [Tree(5, [Tree(6)])])
>>> combined = combine_tree(a, b, mul)
>>> combined.entry
4
>>> combined.children[0].entry
10
"""
```

### 3.1 Intro to Binary Search Trees

A Binary Search Tree (BST) is a special kind of tree that satisfies the following properties:

- Every node of a BST has at most two children called left and right. The children are also BST's.
- For every node, the left child's entry is less than or equal to the parent's entry.
- For every node, the right child's entry is greater than the parent's entry.

```
# Binary Search Tree (BST) Class
class BST:
    empty = ()
    def __init__(self, entry, left=empty, right=empty):
        assert left is BST.empty or isinstance(left, BST)
        assert right is BST.empty or isinstance (right, BST)
        self.entry = entry
        self.left = left
        self.right = right
        if left is not BST.empty:
            assert left.max <= entry
        if right is not BST.empty:
            assert entry < right.min
    @property
    def max(self):
        if self.right is BST.empty:
            return self.entry
        return self.right.max
    @property
    def min(self):
        if self.left is BST.empty:
            return self.entry
        return self.left.min
```

### 3.2 Questions

1. Define a function insert that takes in a BST, bst, and a number, n, and mutates bst by inserting a new node. insert should place the new node as a leaf in the correct position. If t is the BST on the left, then calling insert (t, 3) will change t to the BST on the right. Do not return a new BST unless bst is empty, in which case return a BST containing only n.

