1 PreOrder and Friends

(a) Write the preorder, inorder, and postorder traversals of the following binary search tree.

```
        10
       /  \
      3    12
     / \    \
    1   7    13
               \
                15
```

(b) Draw the result of deleting 3 and then 10 from the binary search tree shown above (using the deletion strategy shown in lecture).

2 Is This a BST?

The following code is meant to check if a given binary tree is a binary search tree. However, for some binary trees it is returning the wrong answer.

```
public static boolean isBST(TreeNode T) {
    if (T == null) {
        return true;
    } else if (T.left != null && T.left.val > T.val) {
        return false;
    } else if (T.right != null && T.right.val < T.val) {
        return false;
    } else {
        return isBST(T.left) && isBST(T.right);
    }
}
```

(a) Give an example of a binary tree for which the method fails.

(b) Rewrite `isBST` so that it is correct. You may find it helpful to define a helper method.

3 Sum Paths

Define a root-to-leaf path as a sequence of nodes from the root of a tree to one of its leaves. Write a method `printSumPaths(TreeNode T, int k)` that prints out all root-to-leaf paths whose values sum to k. For example, if RootNode is the binary tree rooted in 10 in the diagram below and k is 13, then the program will print out `10 2 1` on one line and `10 4 -1` on another.

```
      10
     /  \
    2    4
   / \    \
  5   1    -1
```

(a) Provide your solution by filling in the code below:

```
public static void printSumPaths(TreeNode T, int k) {
    if (T != null) {
        sumPaths(                                   );
    }
}

public static void sumPaths(                                    ) {









}
```

(b) What is the worst case running time of the `printSumPaths` in terms of N, the number of nodes in the tree? What is the worst case running time in terms of h, the height of the tree?