

Priority Queues, Heaps

are defined by operations "add," "find largest," "remove

and scheduling long streams of actions to occur at various

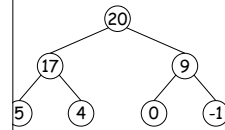
times or sorting (keep removing largest).

Implementation is the *heap*, a kind of tree.

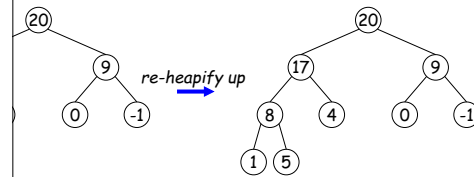
(The same term is used to describe the pool of storage an operator uses. Sorry about that.)

Example: Inserting into a simple heap

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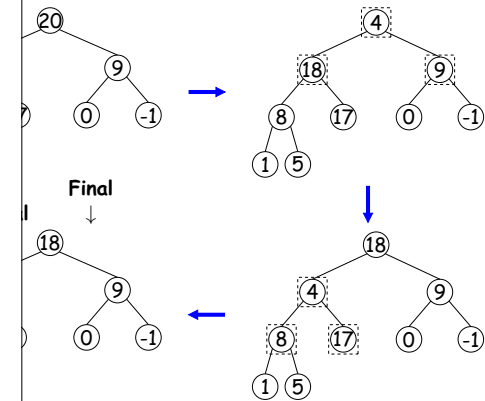


boxes show where heap property violated



Removing Largest from Heap

to remove largest: Move bottommost, rightmost node to top, then swap as needed (swap offending node with larger child) to restore heap property.



CS61B Lecture #23

Priority Queues (Data Structures §6.4, §6.5)

Heaps (§6.2)

Implementations: SortedSet, Map, etc.

Hashing (Data Structures Chapter 7).

Heaps

A heap is a binary tree that enforces the

heap property: Both labels in both children of each node are less than or equal to the node's label.

The root node has the largest label.

The heap property is a binary search property, which allows us to keep tree

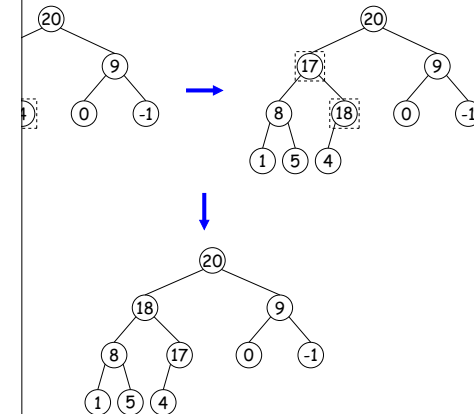
operations always valid to put the smallest nodes anywhere at the bottom of the tree.

A heap can be made **nearly complete**: all but possibly the last level may have as many nodes as possible.

The insertion of new value and deletion of largest value are both operations that take time proportional to $\lg N$ in worst case.

Min-heaps are basically the same, but with the minimum value at the root and children having larger values than their parents.

Heap insertion continued



Ranges

looked for specific items

need an ordering anyway, and can also support looking for values.

perform some action on all values in a BST that are within in natural order):

```

// TODO to all labels in T that are
// < U, in ascending natural order. */
void visitRange (BST T, Comparable<Key> L, Comparable<Key> U,
                Action whatToDo)
{
    if (!T) return;
    int left = L.compareTo (T.label ()),
        right = U.compareTo (T.label ());
    if (left < 0) /* L < label */
        visitRange (T.left (), L, U, whatToDo);
    if (left <= 0 && compRight > 0) /* L <= label < U */
        whatToDo.action (T);
    if (right > 0) /* label < U */
        visitRange (T.right (), L, U, whatToDo);
}
    
```

Red Sets and Range Queries in Java

Set supports range queries with views of set:

headSet(U): subset of S that is < U.

tailSet(L): subset that is ≥ L.

subSet(L,U): subset that is ≥ L, < U.

Views modify S.

e.g., add to a headSet beyond U are disallowed.

Use a view to process a range:

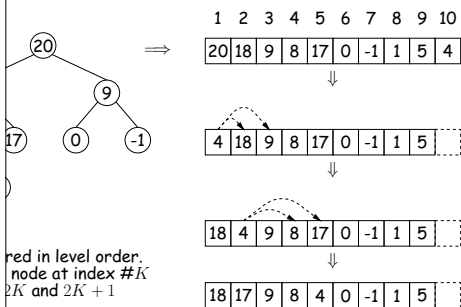
```

String> fauna = new TreeSet<String>
    (.asList ("axolotl", "elk", "dog", "hartebeest", "duck"));
// item : fauna.subSet ("bison", "gnu")
// .out.printf ("%s, ", item);
// dog, duck, elk, "
// type TreeSet<T> requires either that T be Comparable,
// or provide a Comparator:
String> rev_fauna = new TreeSet<String> (Collections.reverseOrder());
    
```

Heaps in Arrays

are nearly complete (missing items only at bottom level),
useful for compact representation.

removal from last slide (dashed arrows show children):



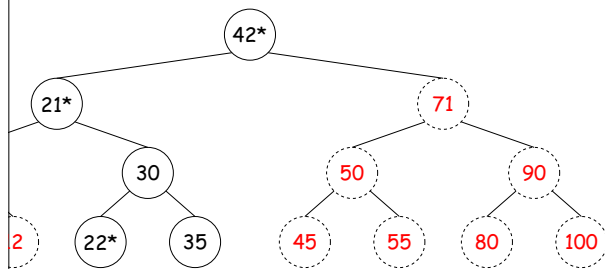
read in level order.
node at index #K
has children at 2K and 2K + 1

Time for Range Queries

range query ∈ O(h + M), where h is height of tree, and M
is number of data items that turn out to be in the range.

Traversing the tree below for all values, x, such that 25 ≤ x ≤ 75

For example, the h comes from the starred nodes; the M comes from
the non-dashed nodes. Dashed nodes are never looked at.



Example of Representation: BSTSet

Representation for
disjoint subsets.

BST, plus
lazy deletion.

```

SortedSet<String>
fauna = new BSTSet<String>(stuff);
subset1 = fauna.subSet("bison","gnu");
subset2 = subset1.subSet("axolotl","dog");
    
```

Expensive!

