

Efficient Use of Keys: the Trie

Efficient use of keys depends on cost of comparisons.

Worst case is length of string.

Should throw extra factor of key length, L , into costs:

Comparisons really means $\Theta(ML)$ operations.

For key X , keep looking at same chars of X M times.

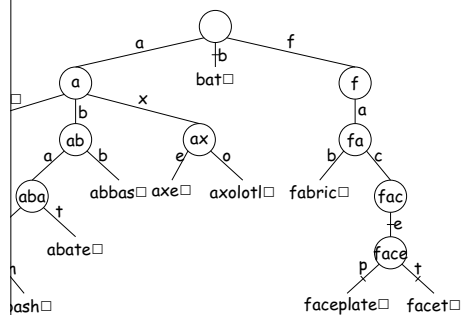
Better? Can we get search cost to be $O(L)$?

Multi-way decision tree, with one decision per character

Adding Item to a Trie

Adding bat and faceplate.

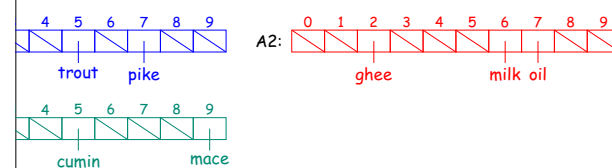
Updated.



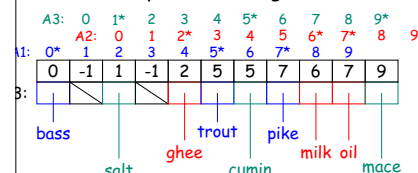
Scrunching Example

(unrelated to Tries on preceding slides)

Arrays, each indexed 0..9



them, but keep track of original index of each item:



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Ordered search structures (*DS(IJ)*, Chapter 9)

Hash Tables (*DS(IJ)*, Chapter 11)

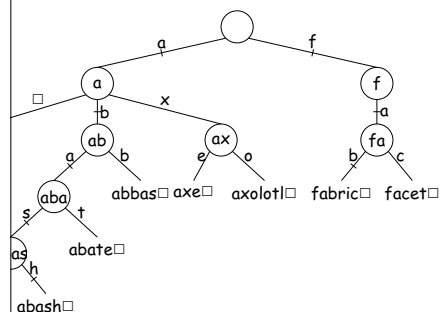
The Trie: Example

Example keys: {abash, abate, abbas, axolotl, axe, fabric, facet}

Show paths followed for "abash" and "fabric"

Each node corresponds to a possible prefix.

Path from root to node = that prefix.



A Side-Trip: Scrunching

Obvious implementation for internal nodes is array in character.

Performance, L length of search key.

Independent of N , number of keys. Is there a dependency?

Arrays are sparsely populated by non-null values—waste of space.

Storing multiple arrays on top of each other!

Using (empty) entries of one array to hold non-null elements of another.

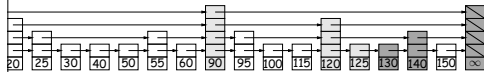
Need markers to tell which entries belong to which array.

Probabilistic Balancing: Skip Lists

can be thought of as a kind of n -ary search tree in which we put the keys at "random" heights.

can be thought of as an ordered list in which one can skip large

example:



start at top layer on left, search until next step would then go down one layer and repeat.

for example, we search for 125 and 127. Gray nodes are looked at; nodes above are overshoots.

because the nodes were chosen randomly so that there are about k nodes that are $> k$ high as there are that are k high.

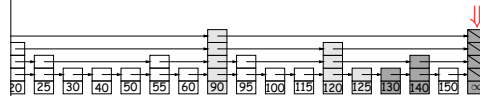
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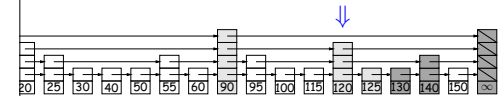
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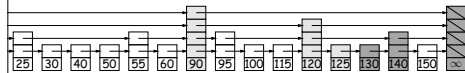
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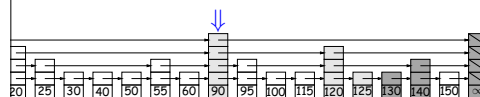
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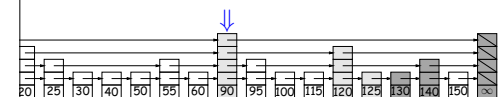
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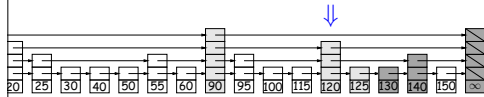
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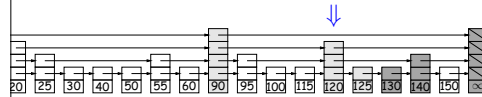
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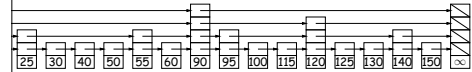
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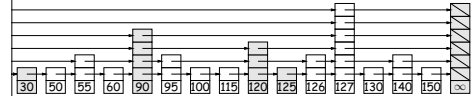
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Example: Adding and deleting

initial list:



for example, we add 126 and 127 (choosing random heights for them) and remove 20 and 40:



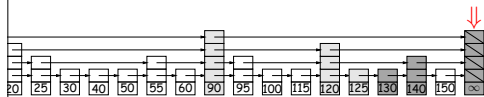
nodes 126 and 127 here have been modified.

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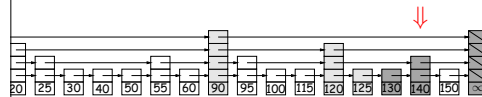
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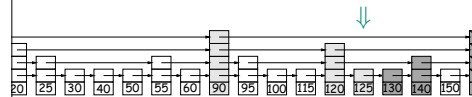
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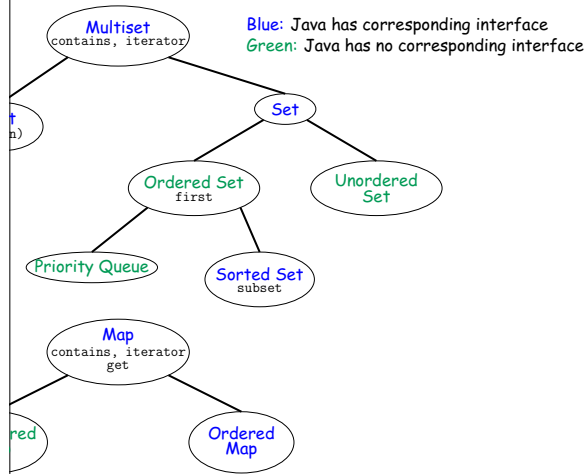
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Summary of Collection Abstractions



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Corresponding Classes in Java

action)
list, LinkedList, Stack, ArrayBlockingQueue,

Set
Queue: PriorityQueue
Set (SortedSet): TreeSet
Sorted Set: HashSet

Map: HashMap
SortedMap: TreeMap

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Summary

Search trees allows us to realize $\Theta(\lg N)$ performance.

Red-black trees:

$\Theta(\lg N)$ performance for searches, insertions, deletions.

Good for external storage. Large nodes minimize # of nodes

$\Theta(\lg N)$ performance for searches, insertions, and deletions, independent of length of key being processed.

Used to manage space efficiently.

Key idea: crunched arrays share space.

Red-black trees allow $\Theta(\lg N)$ performance for searches, insertions, deletions.

Implement.

Look for interesting ideas: probabilistic balance, random structures.

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Structures that Implement Abstractions

Priority Queue: linked lists, circular buffers

Set

Queue: heaps

Set: binary search trees, red-black trees, B-trees, arrays or linked lists

Sorted Set: hash table

Map: hash table

SortedMap: red-black trees, B-trees, sorted arrays or linked lists

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