## 1 Basic Algorithmic Analysis

For each of the following function pairs $f$ and $g$, list out the $\Theta, \Omega, O$ relationships between $f$ and $g$, if any such relationship exists. For example, $f(x) \in O(g(x))$.

1. $f(x)=x^{2}, g(x)=x^{2}+x$
2. $f(x)=5000000 x^{3}, g(x)=x^{5}$
3. $f(x)=\log (x), g(x)=5 x$
4. $f(x)=e^{x}, g(x)=x^{5}$
5. $f(x)=\log \left(5^{x}\right), g(x)=x$

## 2 Practice with Runtime

For each of the following functions, find the Big-Theta expression for the runtime of the function in terms of the input variable $n$.

1. For this problem, assume that the static method constant runs in $\Theta(1)$ time.
```
public static void bars(int n) {
    for (int i = 0; i < n; i += 1) {
        for (int j = 0; j < i; j += 1) {
            system.out.println(i + j);
        }
    }
    for (int k = 0; k < n; k += 1) {
        constant(k);
    }
}
2. public static void barsRearranged(int \(n\) ) \{
        for (int i = 1; i <= n; i *= 2) {
        for (int j = 0; j < i; j += 1) {
                System.out.println("mooove");
            }
    }
}
```


## 3 A Bit with some Bits

Complete the following method. When given a list of integers, bitVote returns an integer such that the $i^{t h}$ bit of the return value is 1 if and only if more than half of the integers in the list have 1 in the $i^{\text {th }}$ bit. Keep in mind that Java ints are 32 bits long!
For example, if bitList was $[1,3]$, then in binary this would be $\left[(01)_{2},(11)_{2}\right]$ (with 30 more zeros in front of each number), and the result would be $(01)_{2} \Longrightarrow 1$, since the right-most digit was 1 for more than half the numbers, but the second-from-the-right digit was not 1 for more than half the numbers.
Note: the solution to this question isn't very complicated, but it's not short! Try breaking it down into components, and ask your neighbors for help!

```
public static int bitVote(int[] bitList) {
```

for (int i $=0$; $i<32$ i++) $\{$ For each bit index
for (int k : bitList) \{ // For each integer
\}
\}
\}

