

Priority Queues, Heaps

are defined by operations "add," "find largest," "remove

scheduling long streams of actions to occur at various

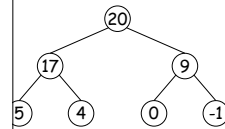
times or sorting (keep removing largest).

Implementation is the *heap*, a kind of tree.

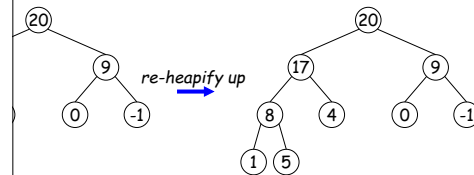
(This same term is used to describe the pool of storage an operator uses. Sorry about that.)

Example: Inserting into a simple heap

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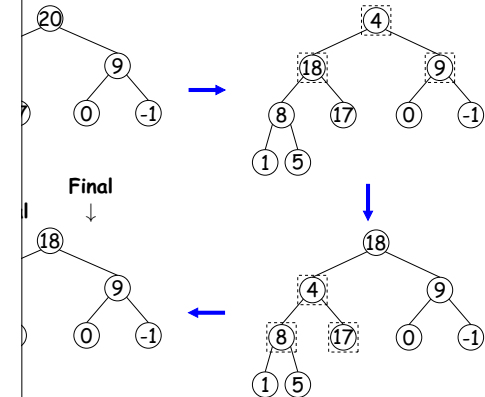


Red boxes show where heap property is violated



Removing Largest from Heap

Algorithm: Move bottommost, rightmost node to top, then bubble up as needed (swap offending node with larger child) to restore heap property.



CS61B Lecture #23

Priority Queues (Data Structures §6.4, §6.5)

Heaps (§6.2)

Priority Queues: SortedSet, Map, etc.

Hashing (Data Structures Chapter 7).

Heaps

A heap is a binary tree that enforces the

heap property: Labels of *both* children of each node are less than its label.

The root node has the largest label.

The heap property is a binary search property, which allows us to keep tree

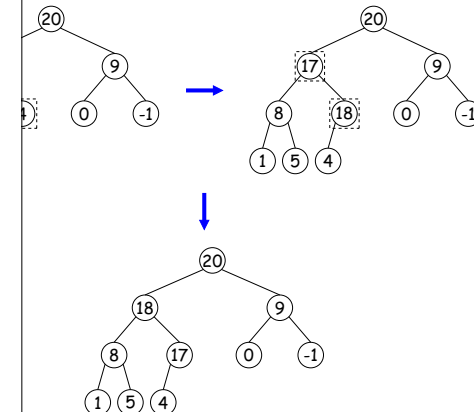
operations always valid to put the smallest nodes anywhere at the bottom of the tree.

A heap can be made *nearly complete*: all but possibly the last level may have as many keys as possible.

The time complexity of insertion of new value and deletion of largest value are both proportional to $\lg N$ in worst case.

Min-heaps are basically the same, but with the minimum value at the root and children having larger values than their parents.

Heap insertion continued



Ranges

looked for specific items

sets, need an ordering anyway, and can also support looking for values.

perform some action on all values in a BST that are within in natural order):

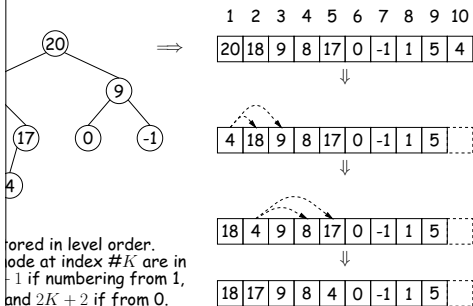
```

TODO to all labels in T that are >= L and < U,
printing natural order. */
visitRange(BST<String> T, String L, String U,
            Consumer<BST<String>> whatToDo) {
    visit(
        T, L, U, whatToDo);
}
visit(BST<String> T, String L, String U,
      Consumer<BST<String>> whatToDo) {
    if (L.compareTo(T.label()) < 0)
        visitRange(T.left(), L, U, whatToDo);
    if (L.compareTo(T.label()) <= 0 && U.compareTo(T.label()) > 0)
        whatToDo.accept(T.label());
    if (U.compareTo(T.label()) > 0)
        visitRange(T.right(), L, U, whatToDo);
}
    
```

Heaps in Arrays

are nearly complete (missing items only at bottom level),
arrays for compact representation.

removal from last slide (dashed arrows show children):



stored in level order.
node at index #K are in
-1 if numbering from 1,
and 2K + 2 if from 0.

Red Sets and Range Queries in Java

Set supports range queries with views of set:

subset(U): subset of S that is < U.

subset(L): subset that is ≥ L.

subset(L,U): subset that is ≥ L, < U.

views modify S.

e.g., add to a headSet beyond U are disallowed.

through a view to process a range:

```

String> fauna = new TreeSet<String>();
fauna.addAll("axolotl", "elk", "dog", "hartebeest", "duck");
String> subset = fauna.subSet("bison", "gnu");
subset.forEach(item -> out.printf("%s, ", item));
    
```

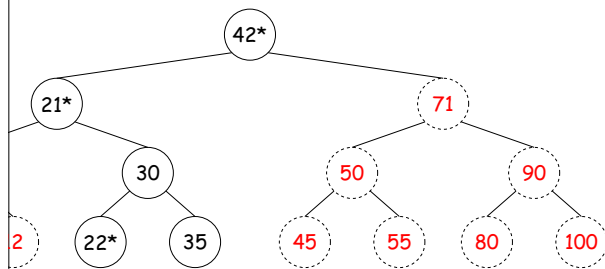
dog, duck, elk,"

Time for Range Queries

range query ∈ O(h + M), where h is height of tree, and M
data items that turn out to be in the range.

traversing the tree below for all values 25 ≤ x < 40.

nodes are never looked at. Starred nodes are looked at but
the h comes from the starred nodes; the M comes from
n-dashed nodes.



Example of Representation: BSTSet

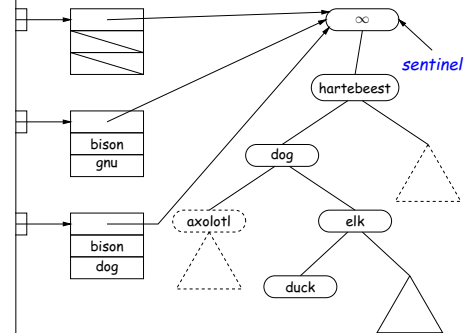
representation for

sorted subsets.

BST, plus

view).

expensive!



TreeSet

type TreeSet<T> requires either that T be Comparable,
or provide a Comparator, as in:

```

String> rev_fauna = new TreeSet<String>(Collections.reverseOrder());
    
```

is a type of function object:

```

Comparator<T> {
    return <0 if LEFT<RIGHT, >0 if LEFT>RIGHT, else 0. */
    compare(T left, T right);
}
    
```

with what Comparator<T extends Comparable<T>> is all

the reverseOrder comparator is defined like this:

```

Comparator that gives the reverse of natural order. */
Comparator<T> reverseOrder() {
    return (x, y) -> y.compareTo(x);
}
    
```