CS61B Lecture #23

Today:

- Priority queues (Data Structures §6.4, §6.5)
- Range queries ($\S6.2$)
- Java utilities: SortedSet, Map, etc.

Next topic: Hashing (Data Structures Chapter 7).

Priority Queues, Heaps

- Priority queue: defined by operations "add," "find largest," "remove largest."
- Examples: scheduling long streams of actions to occur at various future times.
- Also useful for sorting (keep removing largest).
- Common implementation is the *heap*, a kind of tree.
- (Confusingly, this same term is used to described the pool of storage that the **new** operator uses. Sorry about that.)

Heaps

• A max-heap is a binary tree that enforces the

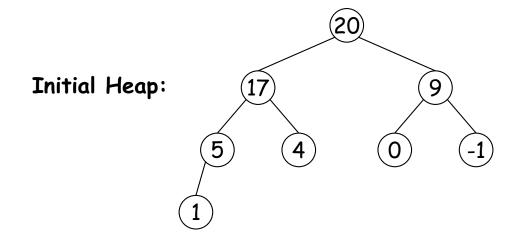
Heap Property: Labels of both children of each node are less than node's label.

- So node at top has largest label.
- Looser than binary search property, which allows us to keep tree "bushy".
- That is, it's always valid to put the smallest nodes anywhere at the bottom of the tree.
- Thus, heaps can be made *nearly complete*: all but possibly the last row have as many keys as possible.
- \bullet As a result, insertion of new value and deletion of largest value always take time proportional to $\lg N$ in worst case.
- A *min-heap* is basically the same, but with the minimum value at the root and children having larger values than their parents.

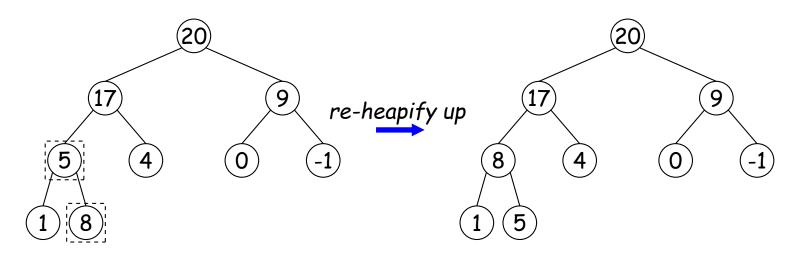
Example: Inserting into a simple heap

Data:

1 17 4 5 9 0 -1 20

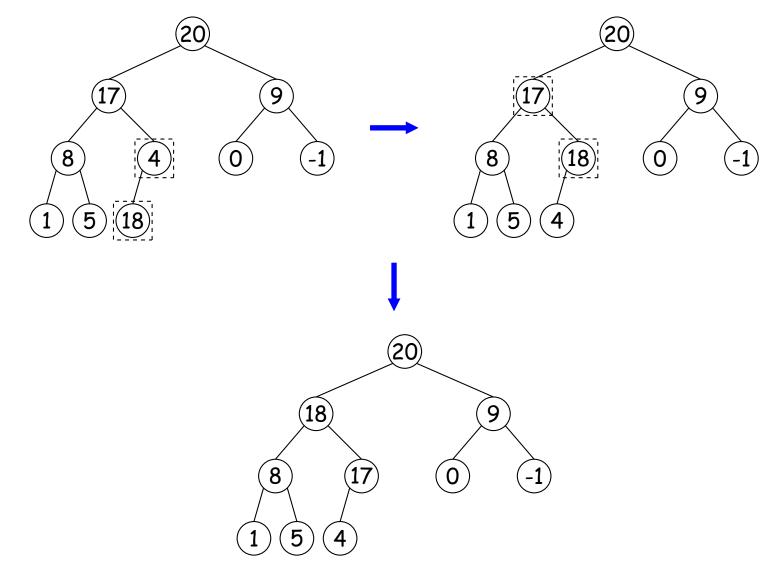


Add 8: Dashed boxes show where heap property violated



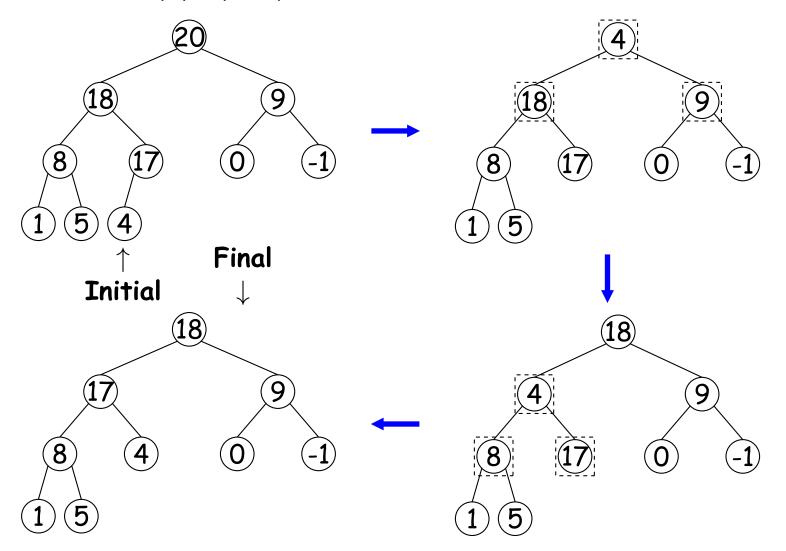
Heap insertion continued

Now insert 18:



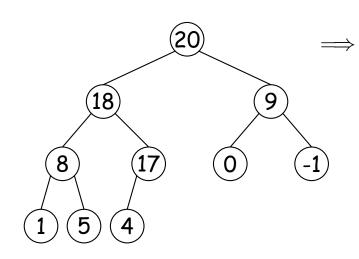
Removing Largest from Heap

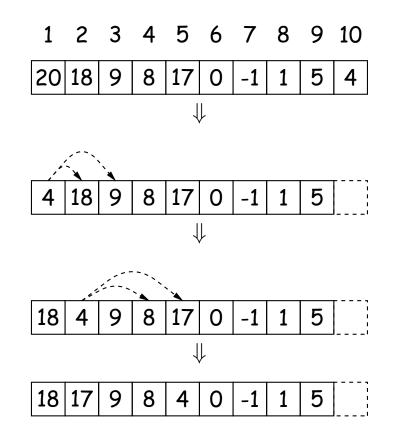
To remove largest: Move bottommost, rightmost node to top, then re-heapify down as needed (swap offending node with larger child) to re-establish heap property.



Heaps in Arrays

- Since heaps are nearly complete (missing items only at bottom level), can use arrays for compact representation.
- Example of removal from last slide (dashed arrows show children):





Nodes stored in level order. Children of node at index #K are in 2K and 2K + 1 if numbering from 1, or 2K + 1 and 2K + 2 if from 0.

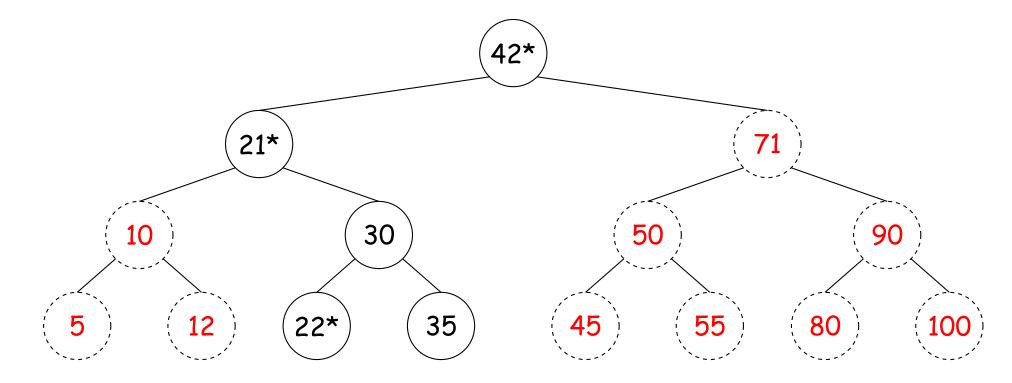
Ranges

- So far, have looked for specific items
- But for BSTs, need an ordering anyway, and can also support looking for *ranges of values*.
- Example: perform some action on all values in a BST that are within some range (in natural order):

```
/** Apply WHATTODO to all labels in T that are \geq L and < U,
* in ascending natural order. */
static void visitRange(BST<String> T, String L, String U,
                       Consumer<BST<String>> whatToDo) {
 if (T != null) {
    int compLeft = L.compareTo(T.label ()),
        compRight = U.compareTo(T.label ());
    if (compLeft < 0)</pre>
                                        /* L < label */
     visitRange (T.left(), L, U, whatToDo);
    if (compLeft <= 0 && compRight > 0) /* L <= label < U */
     whatToDo.accept(T);
   if (compRight > 0)
                                 /* label < U */
     visitRange (T.right (), L, U, whatToDo);
```

Time for Range Queries

- Time for range query $\in O(h + M)$, where h is height of tree, and M is number of data items that turn out to be in the range.
- Consider searching the tree below for all values $25 \le x < 40$.
- Dashed nodes are never looked at. Starred nodes are looked at but not output. The h comes from the starred nodes; the M comes from unstarred non-dashed nodes.



Ordered Sets and Range Queries in Java

- Class SortedSet supports range queries with views of set:
 - S.headSet(U): subset of S that is < U.
 - S.tailSet(L): subset that is \geq L.
 - S.subSet(L,U): subset that is \geq L, < U.
- Changes to views modify S.
- Attempts to, e.g., add to a headSet beyond U are disallowed.
- Can iterate through a view to process a range:

```
SortedSet<String> fauna = new TreeSet<String>
    (Arrays.asList ("axolotl", "elk", "dog", "hartebeest", "duck"));
for (String item : fauna.subSet ("bison", "gnu"))
    System.out.printf ("%s, ", item);
```

```
would print "dog, duck, elk,"
```

TreeSet

• Java library type TreeSet<T> requires either that T be Comparable, or that you provide a Comparator, as in:

```
SortedSet<String> rev_fauna = new TreeSet<String>(Collections.reverseOrder());
```

• Comparator is a type of function object:

```
interface Comparator<T> {
    /** Return <0 if LEFT<RIGHT, >0 if LEFT>RIGHT, else 0. */
    int compare(T left, T right);
}
```

(We'll deal with what Comparator<T extends Comparable<T>> is all about later.)

• For example, the reverseOrder comparator is defined like this:

```
/** A Comparator that gives the reverse of natural order. */
static <T extends Comparable<T>> Comparator<T> reverseOrder() {
    // Java figures out this lambda expression is a Comparable<T>.
    return (x, y) -> y.compareTo(x);
}
```

Example of Representation: BSTSet

- Same representation for both sets and subsets.
- Pointer to BST, plus bounds (if any).
- SortedSet<String>
 fauna = new BSTSet<String>(stuff);
 subset1 = fauna.subSet("bison","gnu");
 subset2 = subset1.subSet("axolotl","dog");
- .size() is expensive!

