

1 Fill in the Blanks

Fill in the following blanks related to min-heaps. Let N is the number of elements in the min-heap. For the entirety of this question, assume the elements in the min-heap are **distinct**.

1. `removeMin` has a best case runtime of _____ and a worst case runtime of _____.
2. `insert` has a best case runtime of _____ and a worst case runtime of _____.
3. A _____ or _____ traversal on a min-heap *may* output the elements in sorted order. Assume there are at least 3 elements in the min-heap.
4. The fourth smallest element in a min-heap with 1000 elements can appear in _____ places in the heap.
5. Given a min-heap with $2^N - 1$ distinct elements, for an element
 - to be on the second level it must be less than _____ element(s) and greater than _____ element(s).
 - to be on the bottommost level it must be less than _____ element(s) and greater than _____ element(s).

Hint: A complete binary tree (with a full last-level) has $2^N - 1$ elements, with N being the number of levels.

2 Heap Mystery

We are given the following array representing a min-heap where each letter represents a **unique** number. Assume the root of the min-heap is at index zero, i.e. A is the root. Note that there is **no** significance of the alphabetical ordering, i.e. just because B precedes C in the alphabet, we do not know if B is less than or greater than C.

Array: [A, B, C, D, E, F, G]

Four unknown operations are then executed on the min-heap. An operation is either a `removeMin` or an `insert`. The resulting state of the min-heap is shown below.

Array: [A, E, B, D, X, F, G]

- (a) Determine the operations executed and their appropriate order. The first operation has already been filled in for you!

1. `removeMin()`
2. _____
3. _____
4. _____

- (b) Fill in the following comparisons with either $>$, $<$, or $?$ if unknown. We recommend considering which elements were compared to reach the final array.

1. X _____ D
2. X _____ C
3. B _____ C
4. G _____ X

3 Hashing Gone Crazy

For this question, use the following TA class for reference.

```

1      public class TA {
2          int charisma;
3          String name;
4          TA(String name, int charisma) {
5              this.name = name;
6              this.charisma = charisma;
7          }
8          @Override
9          public boolean equals(Object o) {
10             TA other = (TA) o;
11             return other.name.charAt(0) == this.name.charAt(0);
12         }
13         @Override
14         public int hashCode() {
15             return charisma;
16         }
17     }

```

Assume that the hashCode of a TA object returns charisma, and the equals method returns true if and only if two TA objects have the same first letter in their name.

Assume that the ECHashMap is a HashMap implemented with external chaining as depicted in lecture. The ECHashMap instance begins at size 4 and, for simplicity, does not resize. Draw the contents of map after the executing the insertions below:

```

1      ECHashMap<TA, Integer> map = new ECHashMap<>();
2      TA sohum = new TA("Sohum", 10);
3      TA vivant = new TA("Vivant", 20);
4      map.put(sohum, 1);
5      map.put(vivant, 2);
6
7      vivant.charisma += 2;
8      map.put(vivant, 3);
9
10     sohum.name = "Vohum";
11     map.put(vivant, 4);
12
13     sohum.charisma += 2;
14     map.put(sohum, 5);
15
16     sohum.name = "Sohum";
17     TA shubha = new TA("Shubha", 24);
18     map.put(shubha, 6);

```

4 Buggy Hash

The following classes may contain a bug in one of its methods. Identify those errors and briefly explain why they are incorrect and in which situations would the bug cause problems.

```
(a)  class Timezone {
2      String timeZone; // "PST", "EST" etc.
3      boolean daylight;
4      String location;
5      ...
6      public int currentTime() {
7          // return the current time in that time zone
8      }
9      public int hashCode() {
10         return currentTime();
11     }
12     public boolean equals(Object o) {
13         Timezone tz = (Timezone) o;
14         return tz.timeZone.equals(timeZone);
15     }
16 }

(b)  class Course {
2      int courseCode;
3      int yearOffered;
4      String[] staff;
5      ...
6      public int hashCode() {
7          return yearOffered + courseCode;
8      }
9      public boolean equals(Object o) {
10         Course c = (Course) o;
11         return c.courseCode == courseCode;
12     }
13 }
```