

1 Fill Grid

Given two one-dimensional arrays `LL` and `UR`, fill in the program on the next page to insert the elements of `LL` into the lower-left triangle of a square two-dimensional array `S` and `UR` into the upper-right triangle of `S`, without modifying elements along the main diagonal of `S`. You can assume `LL` and `UR` both contain at least enough elements to fill their respective triangles. (Spring 2020 MT1)

For example, consider

```
int[] LL = { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 0, 0 };
int[] UR = { 11, 12, 13, 14, 15, 16, 17, 18, 19, 20 };
int[][] S = {
    { 0, 0, 0, 0, 0 },
    { 0, 0, 0, 0, 0 },
    { 0, 0, 0, 0, 0 },
    { 0, 0, 0, 0, 0 },
    { 0, 0, 0, 0, 0 }
};
```

After calling `fillGrid(LL, UR, S)`, `S` should contain

```
{
  { 0, 11, 12, 13, 14 },
  { 1, 0, 15, 16, 17 },
  { 2, 3, 0, 18, 19 },
  { 4, 5, 6, 0, 20 },
  { 7, 8, 9, 10, 0 }
}
```

(The last two elements of `LL` are excess and therefore ignored.)

2 *Pointers*

```
1  /** Fill the lower-left triangle of S with elements of LL and the
2   * upper-right triangle of S with elements of UR (from left-to
3   * right, top-to-bottom in each case). Assumes that S is square and
4   * LL and UR have at least sufficient elements. */
5  public static void fillGrid(int[] LL, int[] UR, int[][] S) {
6      int N = S.length;
7      int kL, kR;
8      kL = kR = 0;
9
10     for (int i = 0; i < N; i += 1) {
11
12         -----
13
14         -----
15
16         -----
17
18         -----
19
20         -----
21
22         -----
23
24         -----
25
26         -----
27
28         -----
29     }
30 }
```

Solution:

```

1 public static void fillGrid(int[] LL, int[] UR, int[][] S) {
2     int N = S.length;
3     int kL, kR;
4     kL = kR = 0;
5     for (int i = 0; i < N; i += 1) {
6         for (int j = 0; j < N; j += 1) {
7             if (i < j) {
8                 S[i][j] = UR[kR];
9                 kR += 1;
10            } else if (i > j) {
11                S[i][j] = LL[kL];
12                kL += 1;
13            }
14        }
15    }
16 }

```

Alternate Solutions:

```

1 public static void fillGrid(int[] LL, int[] UR, int[][] S) {
2     int N = S.length;
3     int kL, kR;
4     kL = kR = 0;
5     for (int i = 0; i < N; i += 1) {
6         for (int j = 0; j < i; j += 1) {
7             S[i][j] = LL[kL];
8             kL += 1;
9         }
10        for (int j = i + 1; j < N; j += 1) {
11            S[i][j] = UR[kR];
12            kR += 1;
13        }
14    }
15 }

1 public static void fillGrid(int[] LL, int[] UR, int[][] S) {
2     int N = S.length;
3     int kL, kR;
4     kL = kR = 0;
5     for (int i = 0; i < N; i += 1) {
6         System.arraycopy(LL, kL, S[i], 0, i);
7         System.arraycopy(UR, kR, S[i], i + 1, N - i - 1);
8         kL += i;
9         kR += square.length - i - 1; /*
10    }
11 }

```

2 Even Odd

Implement the method `evenOdd` by *destructively* changing the ordering of a given `IntList` so that even indexed links **precede** odd indexed links.

For instance, if `lst` is defined as `IntList.list(0, 3, 1, 4, 2, 5)`, `evenOdd(lst)` would modify `lst` to be `IntList.list(0, 1, 2, 3, 4, 5)`.

You may not need all the lines.

Hint: Make sure your solution works for lists of odd and even lengths.

```
public class IntList {
    public int first;
    public IntList rest;
    public IntList (int f, IntList r) {
        this.first = f;
        this.rest = r;
    }

    public static void evenOdd(IntList lst) {

        if (-----) {
            return;
        }

        -----
        -----

        while (-----) {

            -----
            -----
            -----
            -----

        }

        -----
    }
}
```

Solution:

```

1 public static void evenOdd(IntList lst) {
2     if (lst == null || lst.rest == null) {
3         return;
4     }
5     IntList oddList = lst.rest;
6     IntList second = lst.rest;
7     while (lst.rest != null && oddList.rest != null) {
8         lst.rest = lst.rest.rest;
9         oddList.rest = oddList.rest.rest;
10        lst = lst.rest;
11        oddList = oddList.rest;
12    }
13    lst.rest = second;
14 }

```

Alternate Solution:

```

1 public static void evenOdd(IntList lst) {
2     if (lst == null || lst.rest == null || lst.rest.rest == null) {
3         return;
4     }
5     IntList second = lst.rest;
6     int index = 0;
7     while (!(index % 2 == 0 && (lst.rest == null || lst.rest.rest == null))) {
8         IntList temp = lst.rest;
9         lst.rest = lst.rest.rest;
10        lst = temp;
11        index++;
12    }
13    lst.rest = second;
14 }

```

Explanation: For any linked list, observe that we simply want to change the `rest` attribute of each `IntList` instance to skip an `IntList` instance. Looking at `lst`, we want to link 0 to 1, 3 to 4, and so on. This will constitute the work of the body of the `while` loop, so we just need to figure out how to link the last even indexed `IntList` instance to the first odd indexed `IntList` instance. To keep track of the first odd indexed `IntList` instance, we can use `second`. Now, we just need to exit the `while` loop when we are at the last even indexed `IntList` instance. This occurs when the index is even and we are either at the second to last element (`lst.rest.rest == null`) or the last element (`lst.rest == null`).

3 Partition

Implement `partition`, which takes in an `IntList lst` and an integer `k`, and *destructively* partitions `lst` into `k` `IntList`s such that each list has the following

properties: Firstly, It is the **same** length as the other lists. If this is not possible, i.e. `lst` cannot be equally partitioned, then the later lists should be **one** element smaller. For example, partitioning an `IntList` of length 25 with $k = 3$ would result in partitioned lists of lengths 9, 8, and 8. Secondly, its ordering is consistent with the ordering of `lst`, i.e. items in earlier in `lst` must **precede** items that are later.

These lists should be put in an array of length k , and this array should be returned. For instance, if `lst` contains the elements 5, 4, 3, 2, 1, and $k = 2$, then a **possible** partition (note that there are many possible partitions), is putting elements 5, 3, 2 at index 0, and elements 4, 1 at index 1.

You may assume you have the access to the method `reverse`, which destructively reverses the ordering of a given `IntList` and returns a pointer to the reversed `IntList`. You may not create any `IntList` instances. You may not need all the lines.

Hint: You may find the `%` operator helpful.

```

1 public static IntList[] partition(IntList lst, int k) {
2     IntList[] array = new IntList[k];
3     int index = 0;
4     IntList L = _____
5     while (L != null) {
6
7         _____
8
9         _____
10
11        _____
12
13        _____
14
15        _____
16
17        _____
18
19        _____
20    }
21    return array;
22 }
```

Solution: [Here is a video walkthrough of the solution.](#)

```

1 public static IntList[] partition(IntList lst, int k) {
2     IntList[] array = new IntList[k];
3     int index = 0;
4     IntList L = reverse(lst);
5     while (L != null) {
6         IntList prevAtIndex = array[index];
7         IntList next = L.rest;
```

```
8     array[index] = L;
9     array[index].rest = prevAtIndex;
10    L = next;
11    index = (index + 1) % array.length;
12  }
13  return array;
14 }
```

Explanation: We reverse our `IntList` so that we can build up each element of the `IntList[]` array backwards—in general, it is much easier to build an `IntList` backward than forward.

The general idea is to initialize each element in the array to `null`, then put an element of `L` inside the correct index by assigning `array[index] = L`. Then, we get whatever we've built up so far (`prevAtIndex`) and add it to the end of our `rest` element so that we have the entire `IntList` again with one element at the front.

Afterwards, we advance `L` to the next element and increment the index.