

CS61B Lecture #4: Simple Pointer Manipulation

Recreation Prove that for every acute angle $\alpha > 0$,

$$\tan \alpha + \cot \alpha \geq 2$$

Announcements

- **Today:** More pointer hacking.
- **Handing in labs and homework:** We'll be lenient about accepting late homework and labs for lab1, lab2, and hw0. Just get it done: part of the point is getting to understand the tools involved. We will *not* accept submissions by email.
- We will feel free to interpret the absence of a central repository for you or a lack of a lab1 submission from you as indicating that you intend to drop the course.

Small Test of Understanding

- In Java, the keyword **final** in a variable declaration means that the variable's value may not be changed after the variable is initialized.
- Is the following class valid?

```
public class Issue {  
  
    private final IntList aList = new IntList(0, null);  
  
    public void modify(int k) {  
        this.aList.head = k;  
    }  
}
```

Why or why not?

Small Test of Understanding

- In Java, the keyword **final** in a variable declaration means that the variable's value may not be changed after the variable is initialized.
- Is the following class valid?

```
public class Issue {  
  
    private final IntList aList = new IntList(0, null);  
  
    public void modify(int k) {  
        this.aList.head = k;  
    }  
}
```

Why or why not?

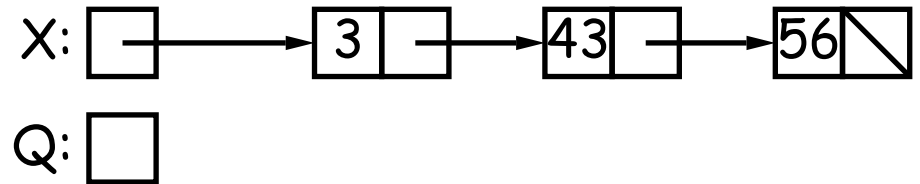
Answer: This is *valid*. Although `modify` changes the head variable of the object pointed to by `aList`, it does *not* modify the contents of `aList` itself (which is a pointer).

Destructive Incrementing

Destructive solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

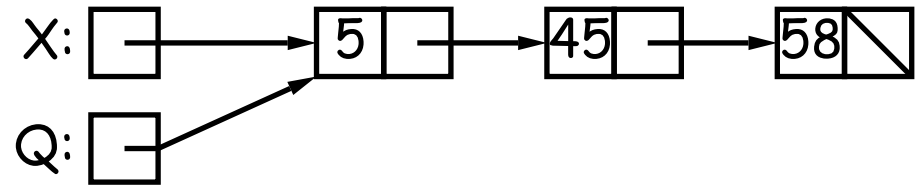


Destructive Incrementing

Destructive solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

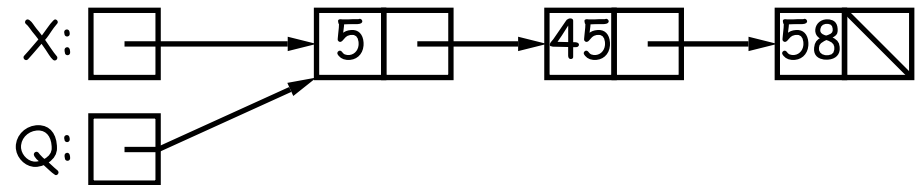


Destructive Incrementing

Destructive solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
    if (P == null)  
        return null;  
    ?  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

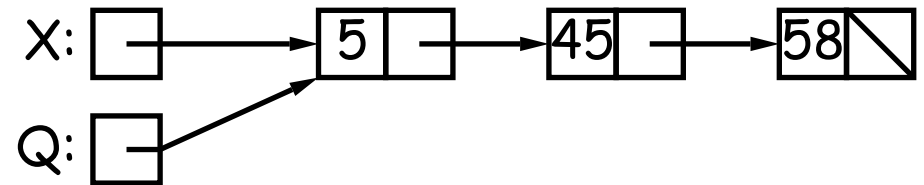


Destructive Incrementing

Destructive solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
    if (P == null)  
        return null;  
    else {  
        P.head += n;  
        P.tail = dincrList(P.tail, n);  
        return P;  
    }  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

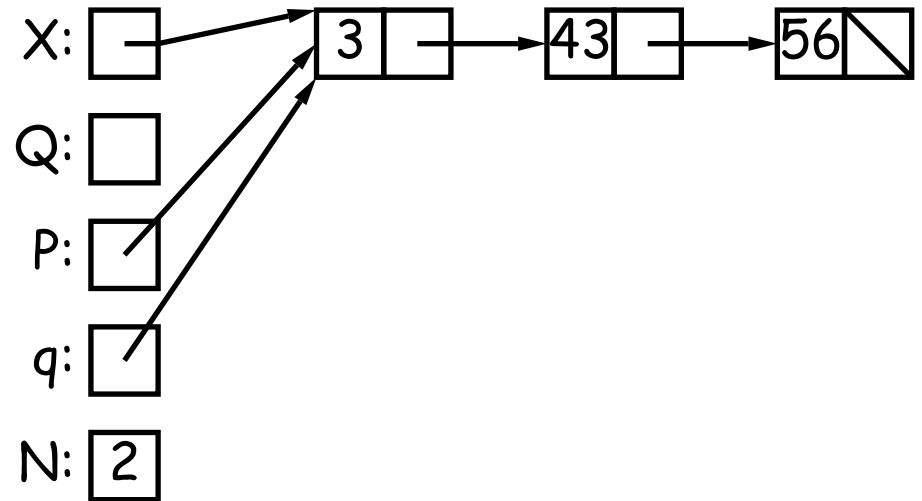


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

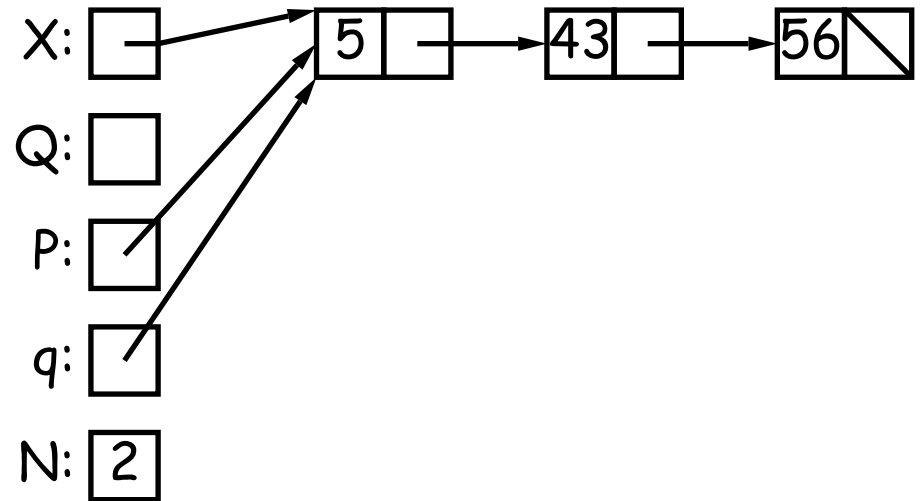


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

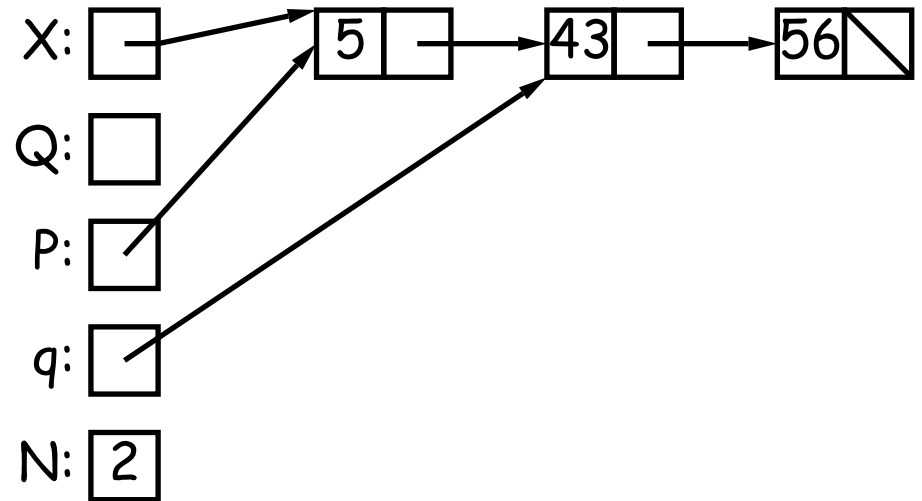


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

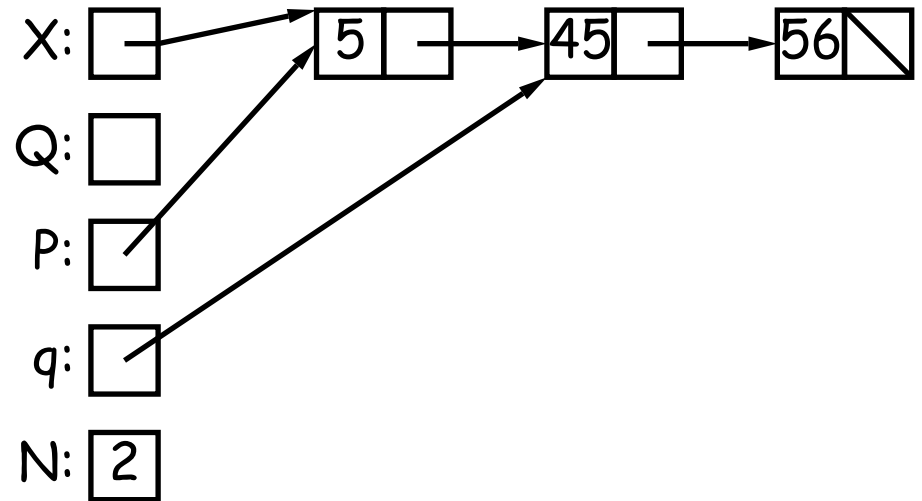


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

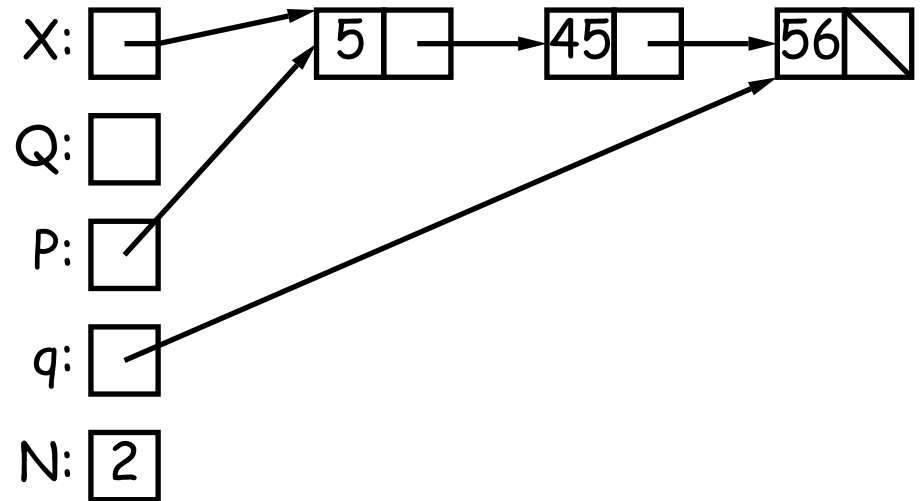


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

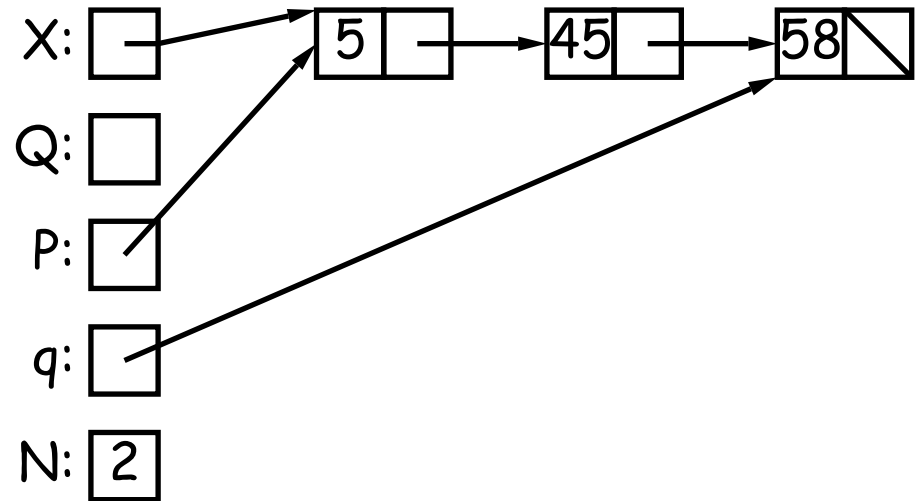


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

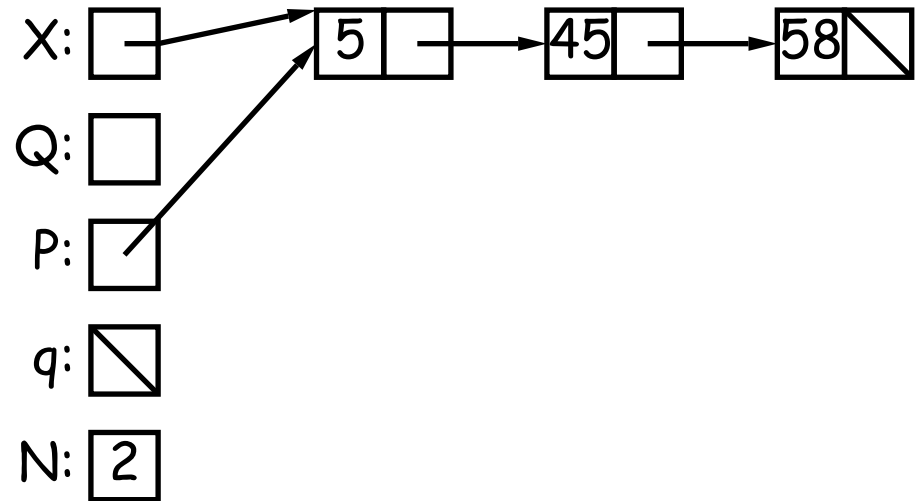


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

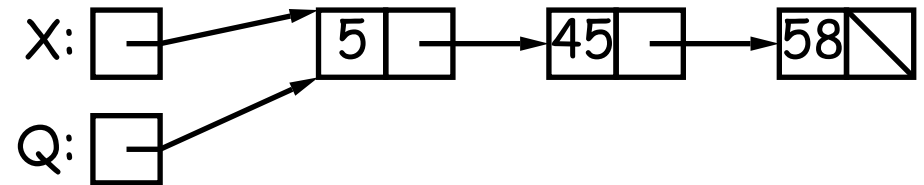


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
    IntList q;  
    q = P;  
    while (?) {  
    }  
    return ?;  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

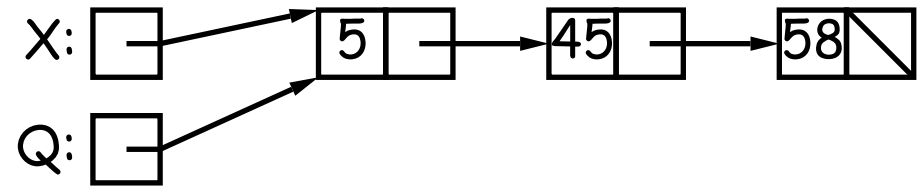


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
    IntList q;  
    q = P;  
    while (q != null) {  
        q.head += n;  
        q = q.tail;  
    }  
    return P;  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```

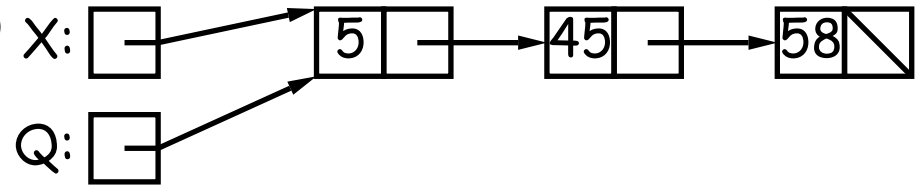


Iterative Destructive Incrementing

Let's try using a **while** loop:

```
/** Destructively add N to P's items.  
 * Return modified list. */  
static IntList dincrList(IntList P, int n) {  
    // 'for' can do more than count!  
    for (IntList q = P; q != null; q = q.tail)  
        q.head += n;  
    return P;  
}
```

```
X = IntList.list(3, 43, 56);  
/* IntList.list from HW #1 */  
Q = dincrList(X, 2);
```



Another Example: Non-destructive List Deletion

If L is the list $[2, 1, 2, 9, 2]$, we want `removeAll(L,2)` to be the new list $[1, 9]$.

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return /*( null with all x's removed )*/;
    else if (L.head == x)
        return /*( L with all x's removed (L!=null, L.head==x) )*/;
    else
        return /*( L with all x's removed (L!=null, L.head!=x) )*/;
}
```

Another Example: Non-destructive List Deletion

If L is the list $[2, 1, 2, 9, 2]$, we want $\text{removeAll}(L, 2)$ to be the new list $[1, 9]$.

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return /*( L with all x's removed (L!=null, L.head==x) )*/;
    else
        return /*( L with all x's removed (L!=null, L.head!=x) )*/;
}
```

Another Example: Non-destructive List Deletion

If L is the list $[2, 1, 2, 9, 2]$, we want `removeAll(L, 2)` to be the new list $[1, 9]$.

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return removeAll(L.tail, x);
    else
        return /*( L with all x's removed (L!=null, L.head!=x) )*/;
}
```

Another Example: Non-destructive List Deletion

If L is the list $[2, 1, 2, 9, 2]$, we want `removeAll(L, 2)` to be the new list $[1, 9]$.

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return removeAll(L.tail, x);
    else
        return new IntList(L.head, removeAll(L.tail, x));
}
```

Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;

    ?

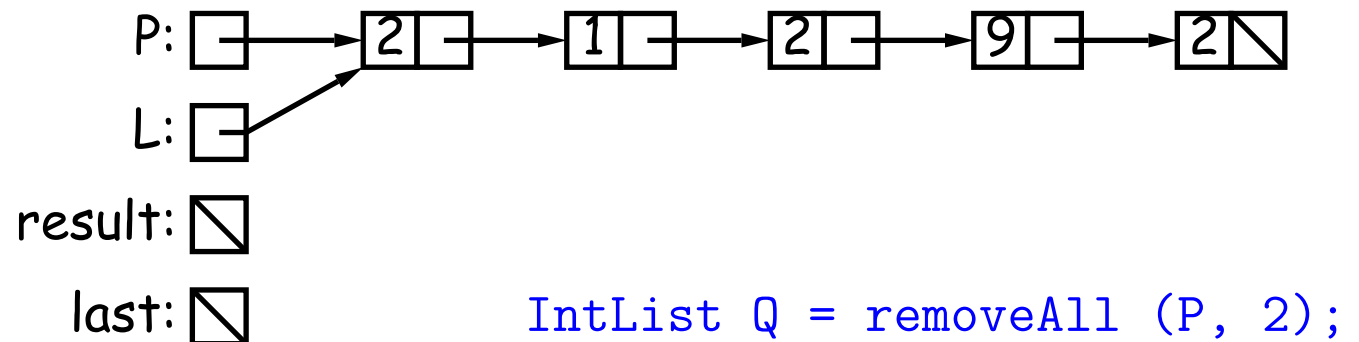
    return result;
}
```

Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances  
 * of X from L non-destructively. */
```

```
static IntList removeAll(IntList L, int x) {  
    IntList result, last;  
    result = last = null;  
  
    ?  
  
    return result;  
}
```



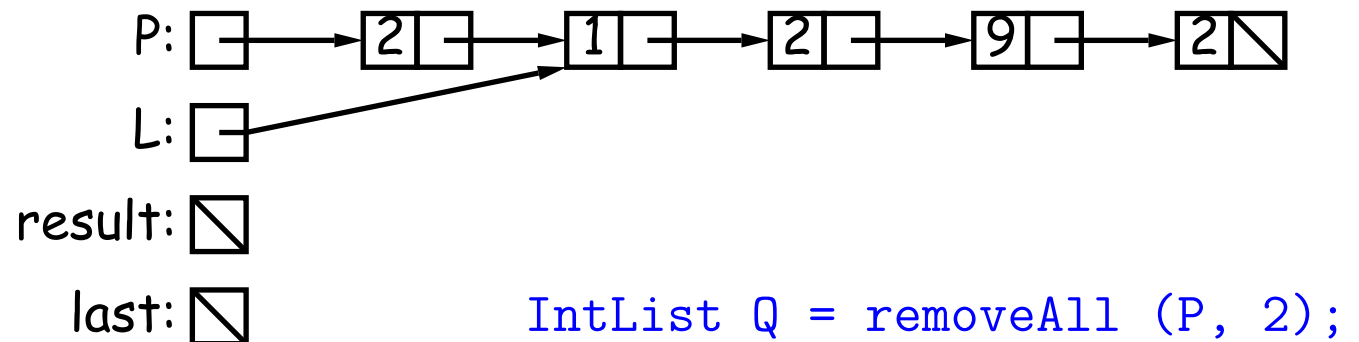
Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;

    ?

    return result;
}
```



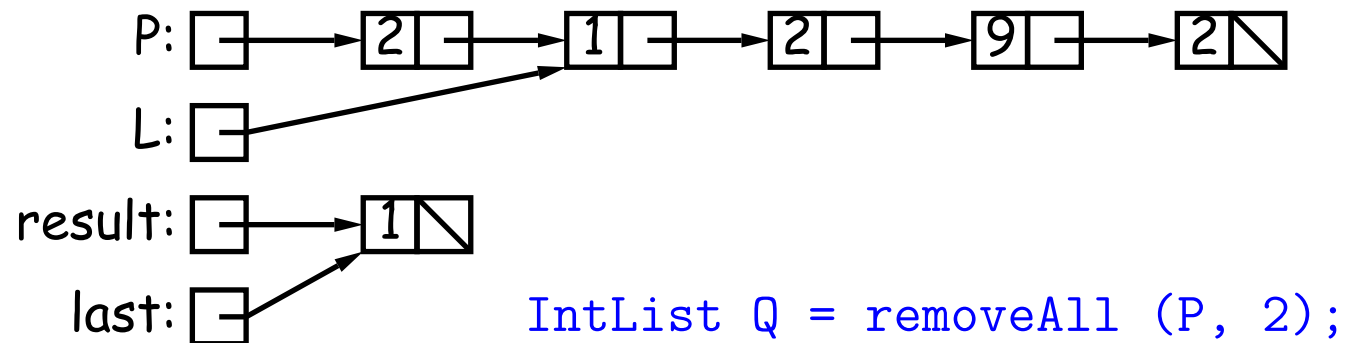
Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;

    ?

    return result;
}
```



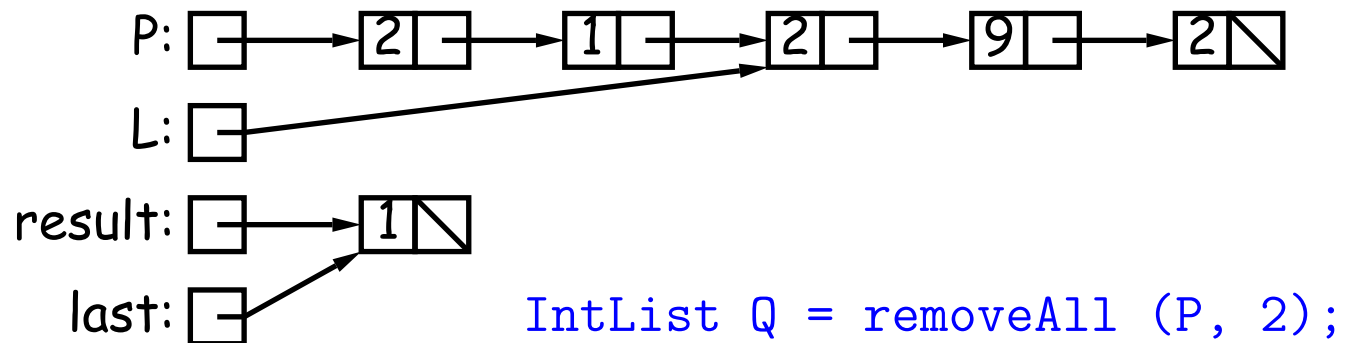
Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;

    ?

    return result;
}
```



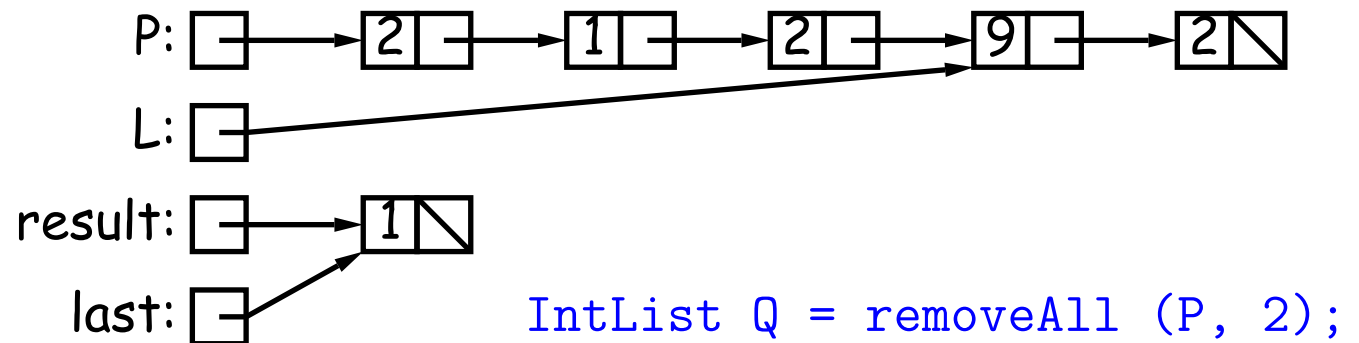
Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;

    ?

    return result;
}
```

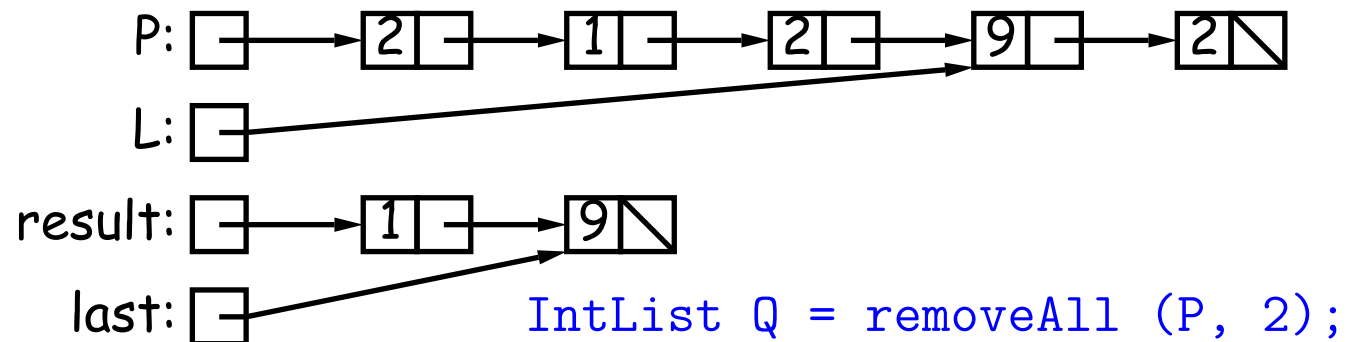


Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances  
 * of X from L non-destructively. */
```

```
static IntList removeAll(IntList L, int x) {  
    IntList result, last;  
    result = last = null;  
  
    ?  
  
    return result;  
}
```



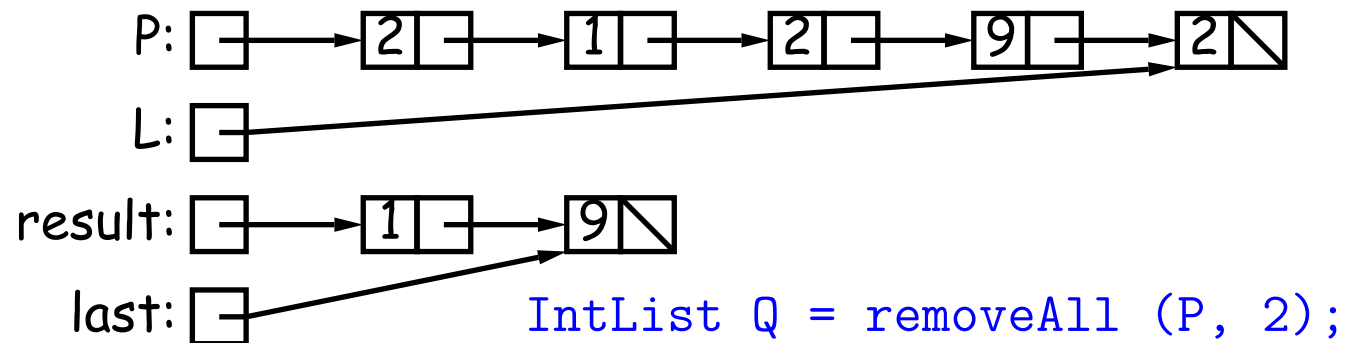
Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;

    ?

    return result;
}
```

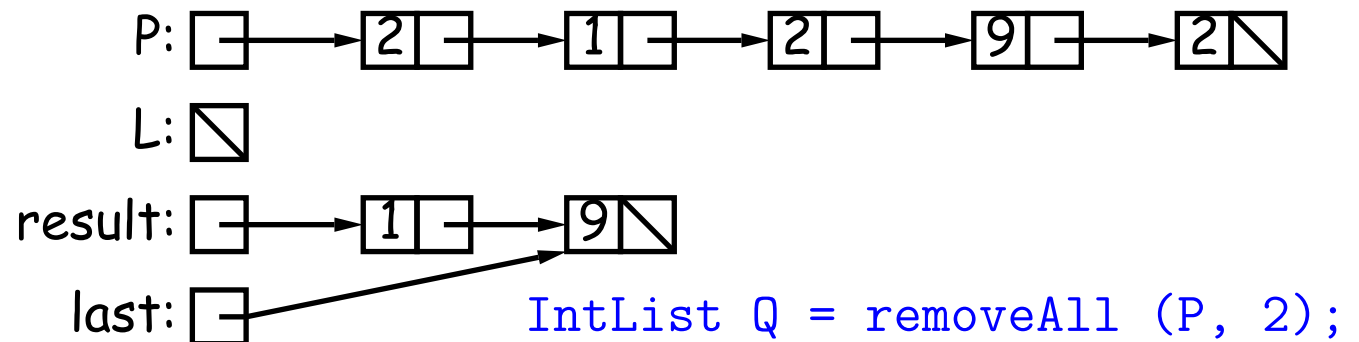


Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances  
 * of X from L non-destructively. */
```

```
static IntList removeAll(IntList L, int x) {  
    IntList result, last;  
    result = last = null;  
  
    ?  
  
    return result;  
}
```

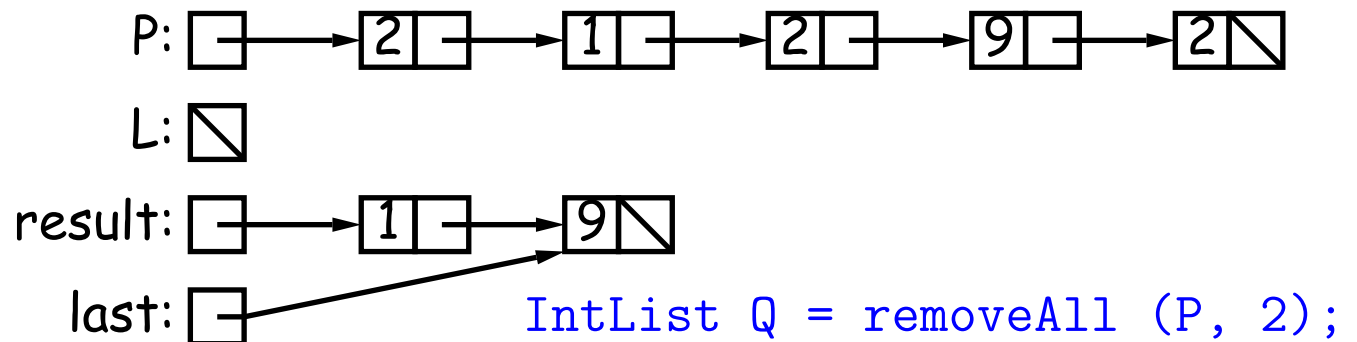


Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances  
 * of X from L non-destructively. */
```

```
static IntList removeAll(IntList L, int x) {  
    IntList result, last;  
    result = last = null;  
    for ( ; L != null; L = L.tail) {  
        if (x == L.head)  
            continue;  
        else if (last == null)  
            result = last = new IntList(L.head, null);  
        else  
            last = last.tail = new IntList(L.head, null);  
    }  
    return result;  
}
```

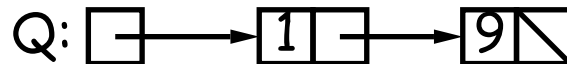
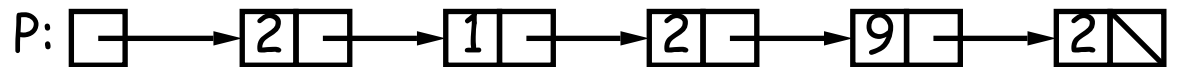


Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances  
 * of X from L non-destructively. */
```

```
static IntList removeAll(IntList L, int x) {  
    IntList result, last;  
    result = last = null;  
    for ( ; L != null; L = L.tail) {  
        if (x == L.head)  
            continue;  
        else if (last == null)  
            result = last = new IntList(L.head, null);  
        else  
            last = last.tail = new IntList(L.head, null);  
    }  
    return result;  
}
```



```
IntList Q = removeAll (P, 2);
```


Destructive Deletion

→ : Original

..... : after Q = dremoveAll (Q,1)



```
/** The list resulting from removing all instances of X from L.
```

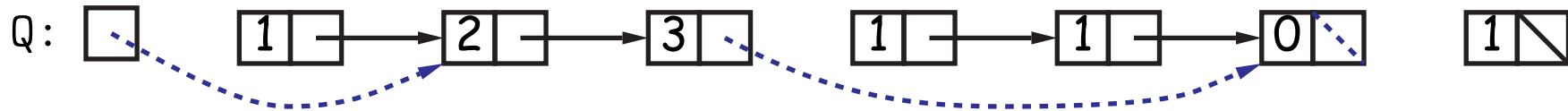
```
 * The original list may be destroyed. */
```

```
static IntList dremoveAll(IntList L, int x) {  
    if (L == null)  
        return /*( null with all x's removed )*/;  
    else if (L.head == x)  
        return /*( L with all x's removed (L != null) )*/;  
    else {  
        /*{ Remove all x's from L's tail. }*/;  
        return L;  
    }  
}
```

Destructive Deletion

→ : Original

⋯ : after Q = dremoveAll (Q,1)



`/** The list resulting from removing all instances of X from L.`

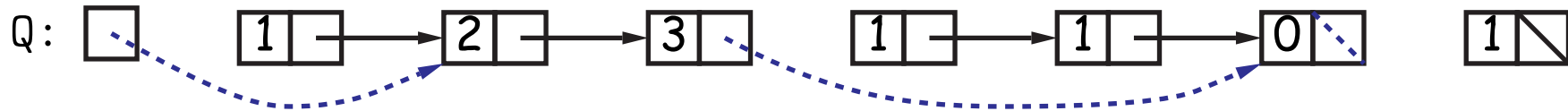
`* The original list may be destroyed. */`

```
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return /*( null with all x's removed )*/;
    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

Destructive Deletion

→ : Original

⋯ : after Q = dremoveAll (Q,1)



/** The list resulting from removing all instances of X from L.

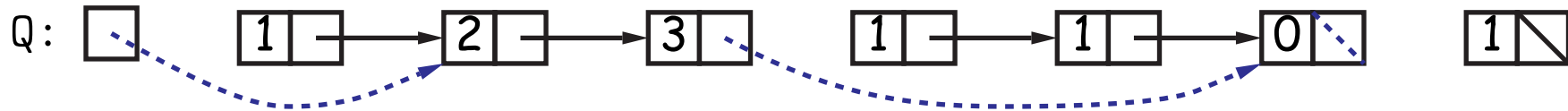
* The original list may be destroyed. */

```
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return /*( null with all x's removed )*/;
    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

Destructive Deletion

→ : Original

⋯ : after Q = dremoveAll (Q,1)



`/** The list resulting from removing all instances of X from L.`

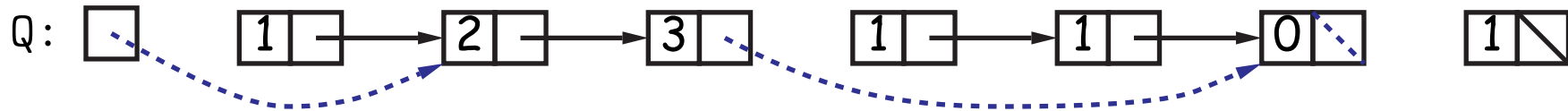
`* The original list may be destroyed. */`

```
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return /*( null with all x's removed )*/;
    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

Destructive Deletion

→ : Original

⋯ : after Q = dremoveAll (Q,1)



*/** The list resulting from removing all instances of X from L.*

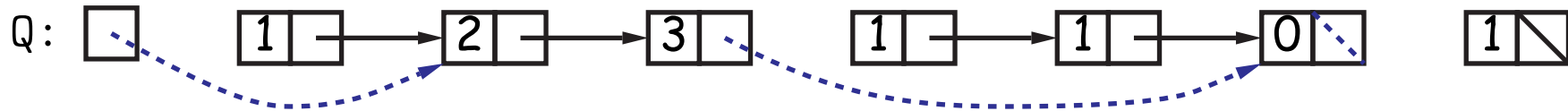
** The original list may be destroyed. */*

```
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

Destructive Deletion

→ : Original

⋯ : after Q = dremoveAll (Q,1)



/** The list resulting from removing all instances of X from L.

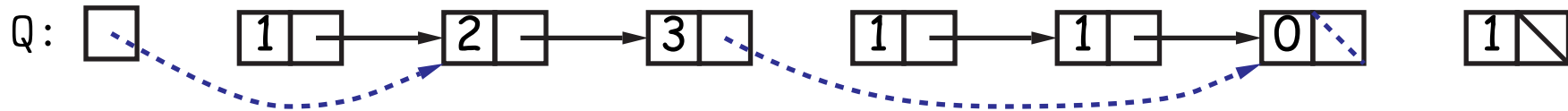
* The original list may be destroyed. */

```
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return
    else if (L.head == x)
        return dremoveAll(L.tail, x);
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

Destructive Deletion

→ : Original

⋯ : after Q = dremoveAll (Q,1)



`/** The list resulting from removing all instances of X from L.`

`* The original list may be destroyed. */`

```
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return
    else if (L.head == x)
        return dremoveAll(L.tail, x);
    else {
        L.tail = dremoveAll(L.tail, x);
        return L;
    }
}
```

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

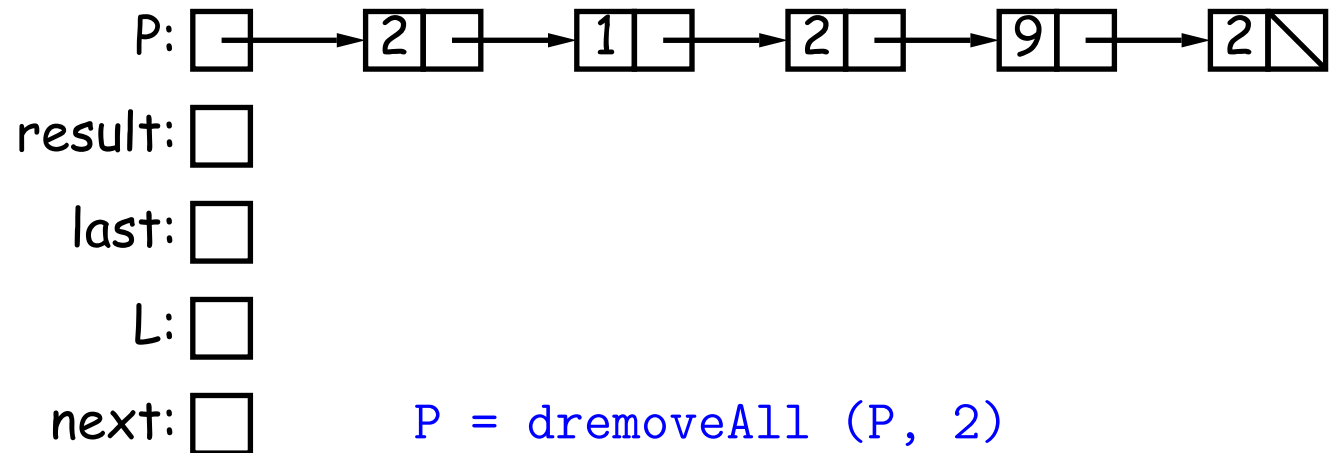
    }
    return result;
}
```


Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}
```

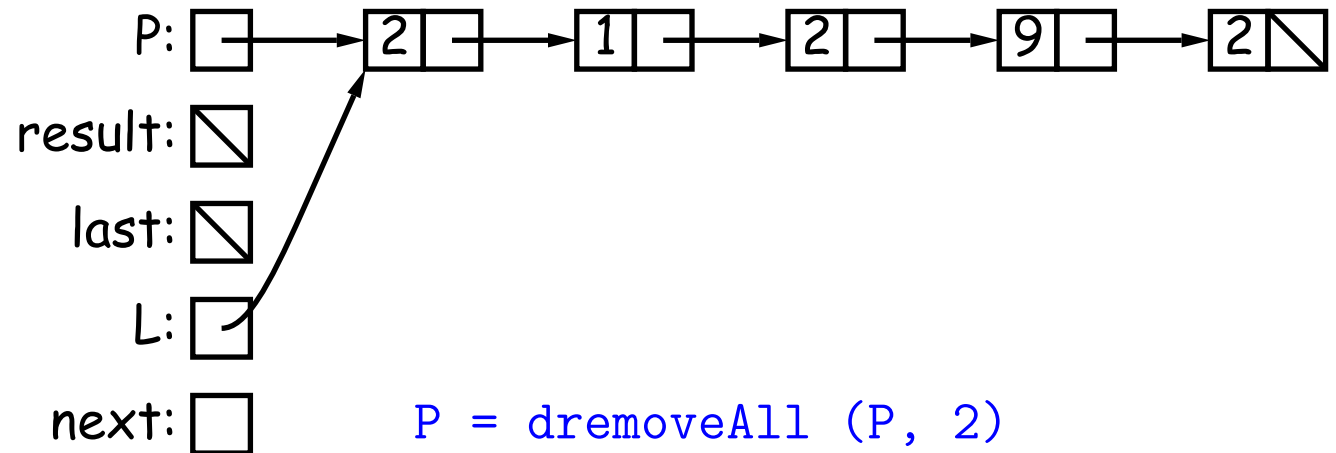


Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}
```

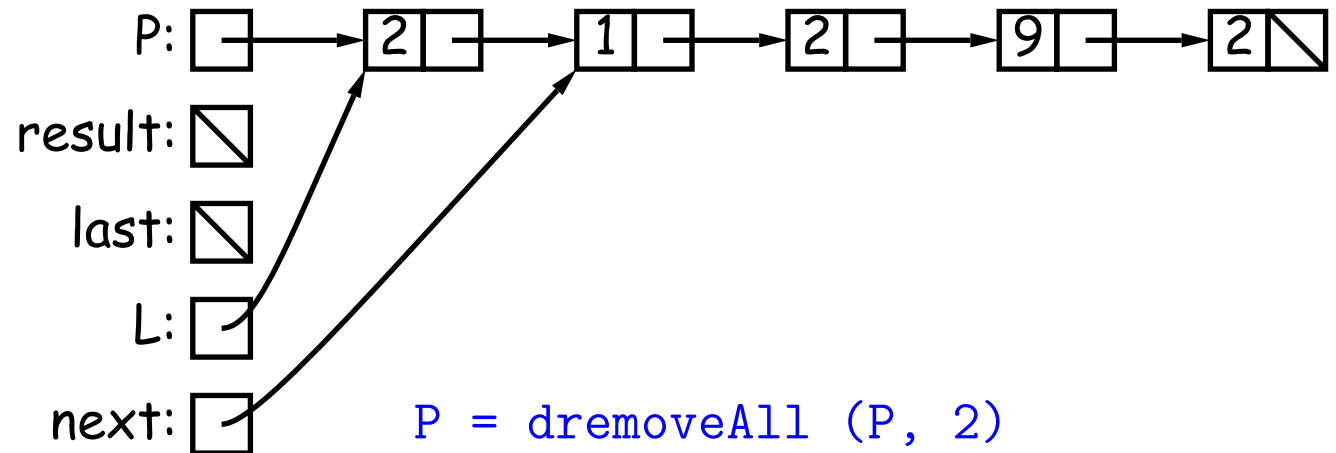


Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}
```

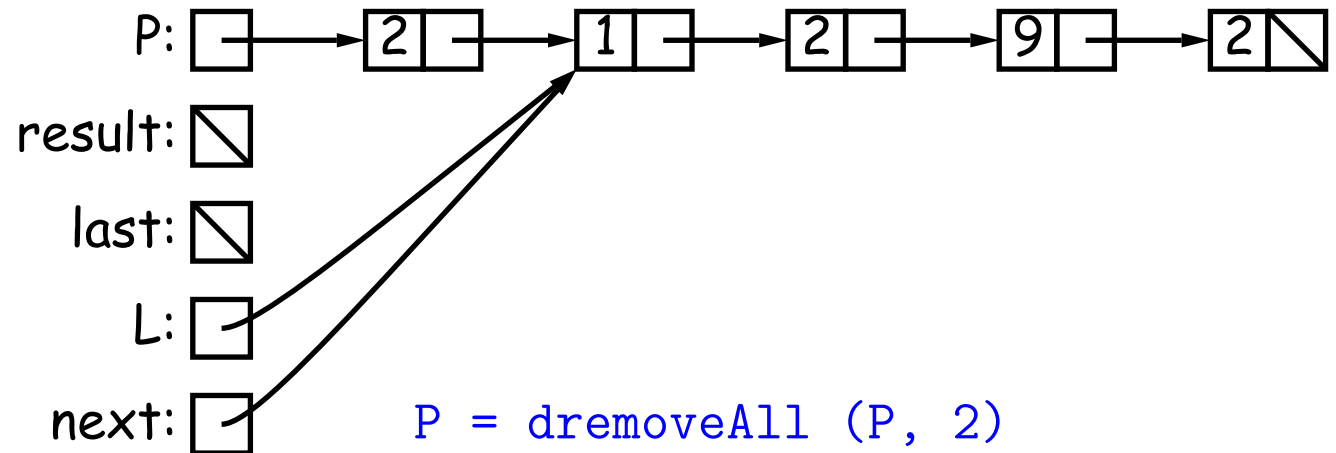


Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}
```

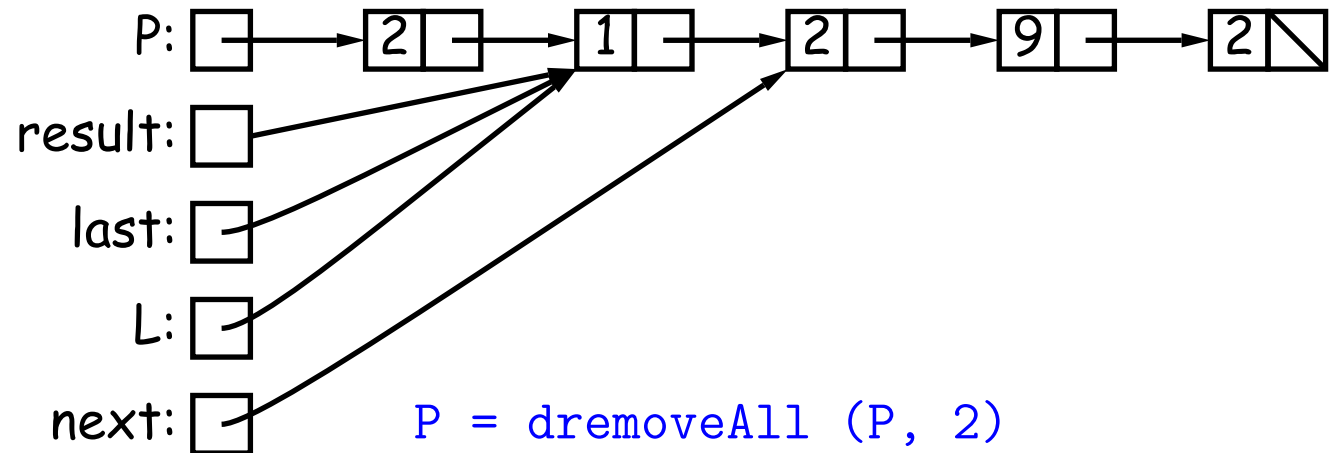


Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}
```

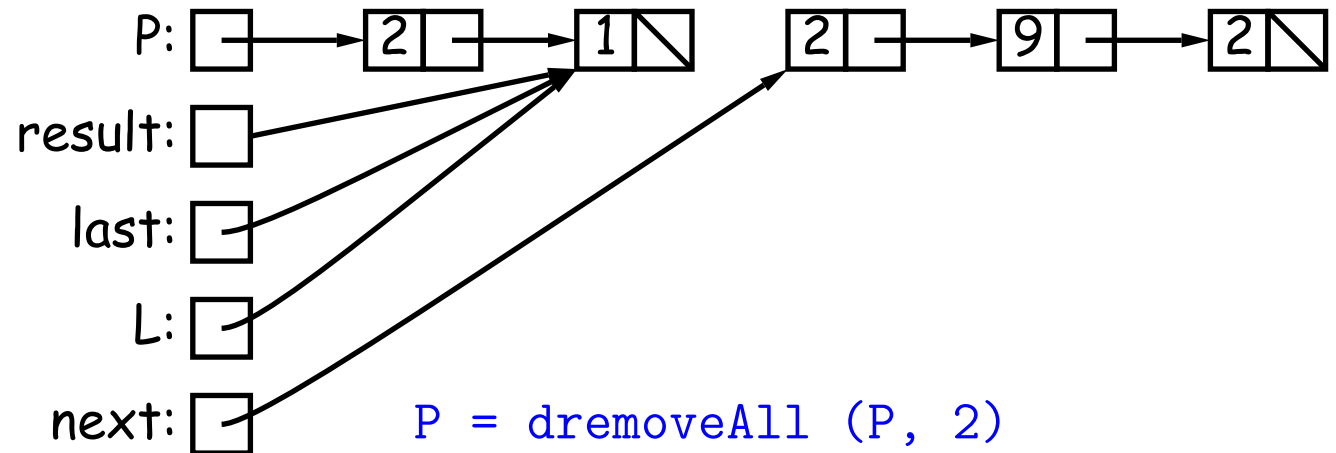


Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}
```



Iterative Destructive Deletion

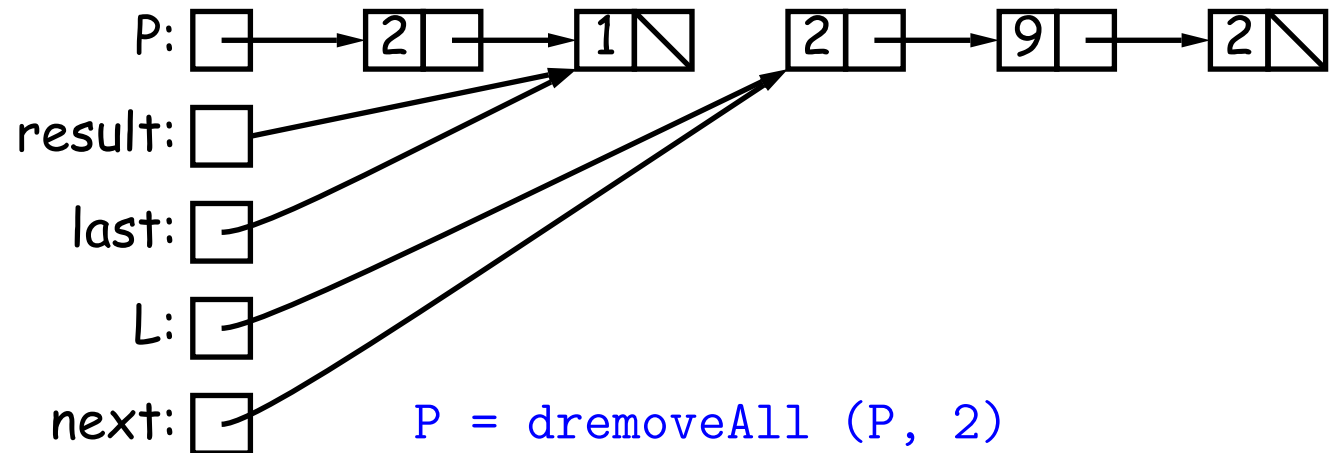
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```

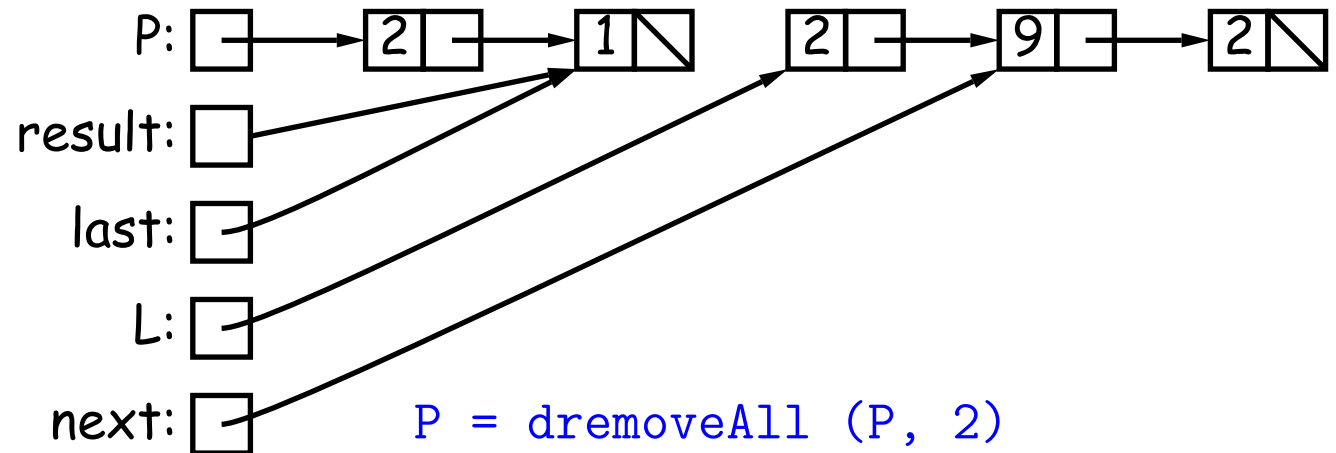


Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}
```



Iterative Destructive Deletion

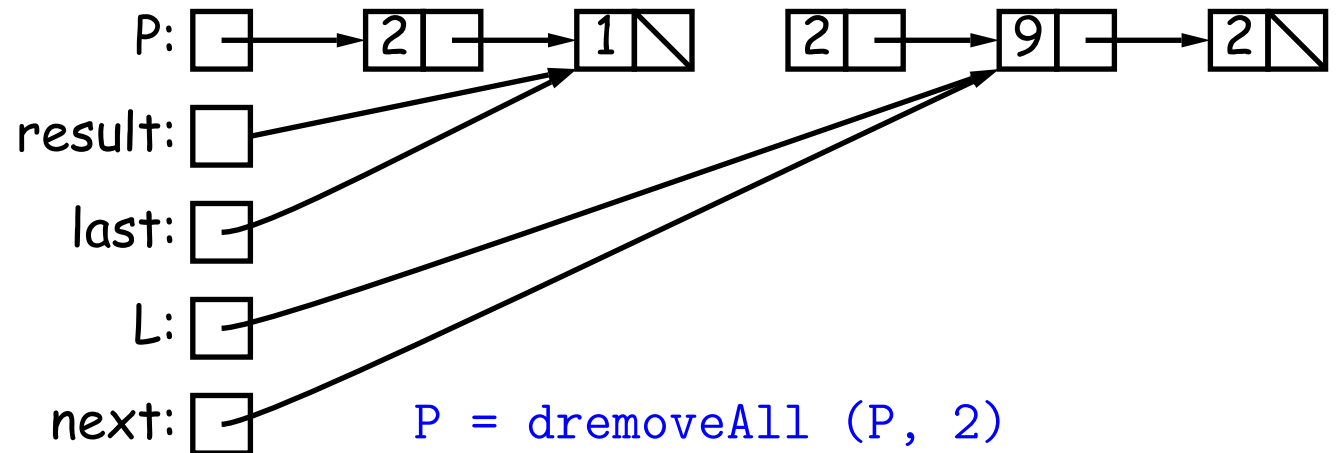
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```



Iterative Destructive Deletion

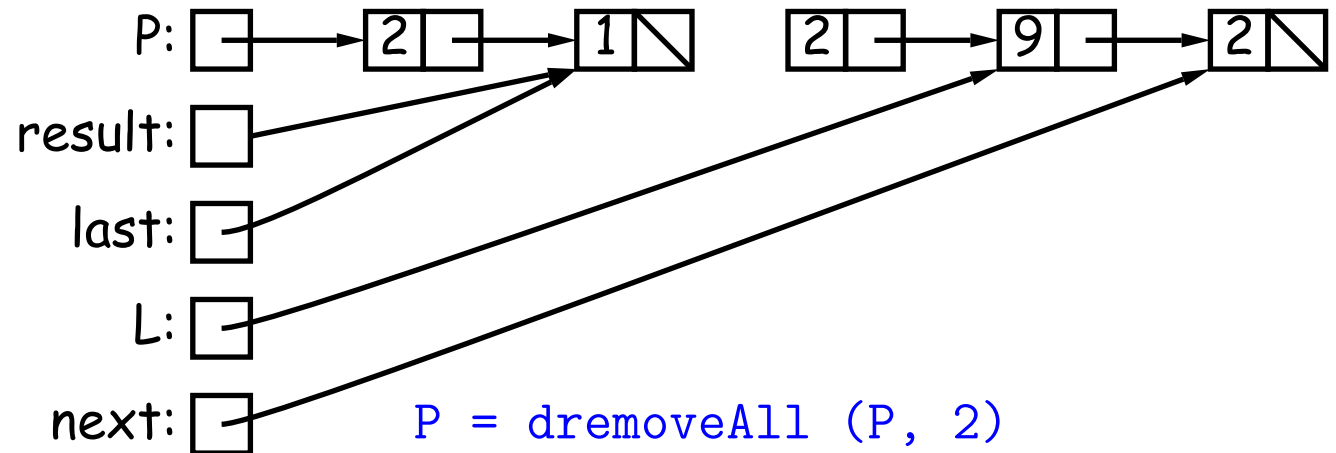
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```



Iterative Destructive Deletion

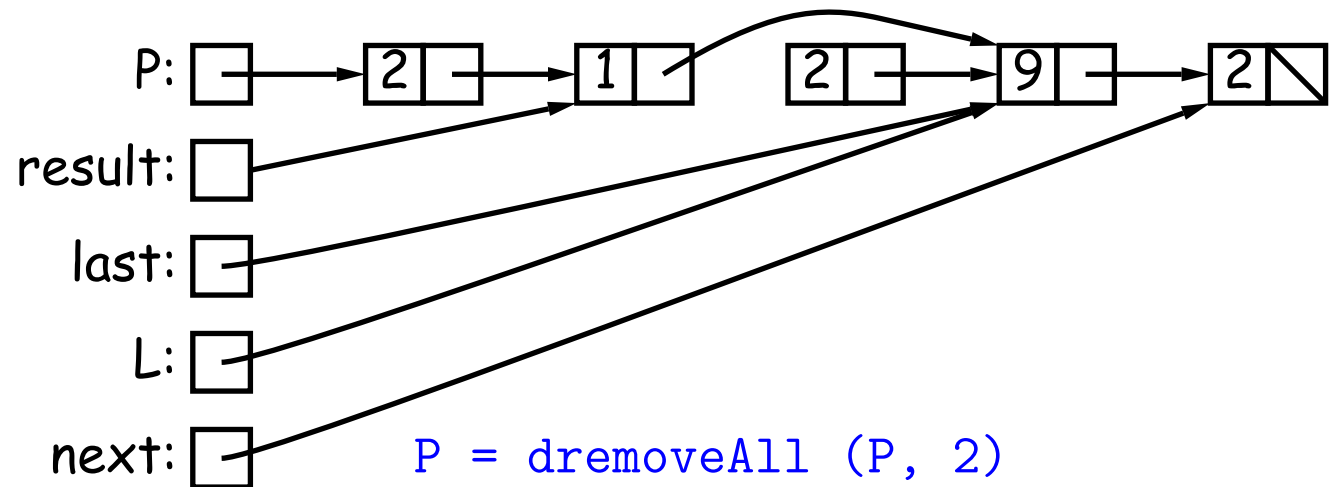
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```



Iterative Destructive Deletion

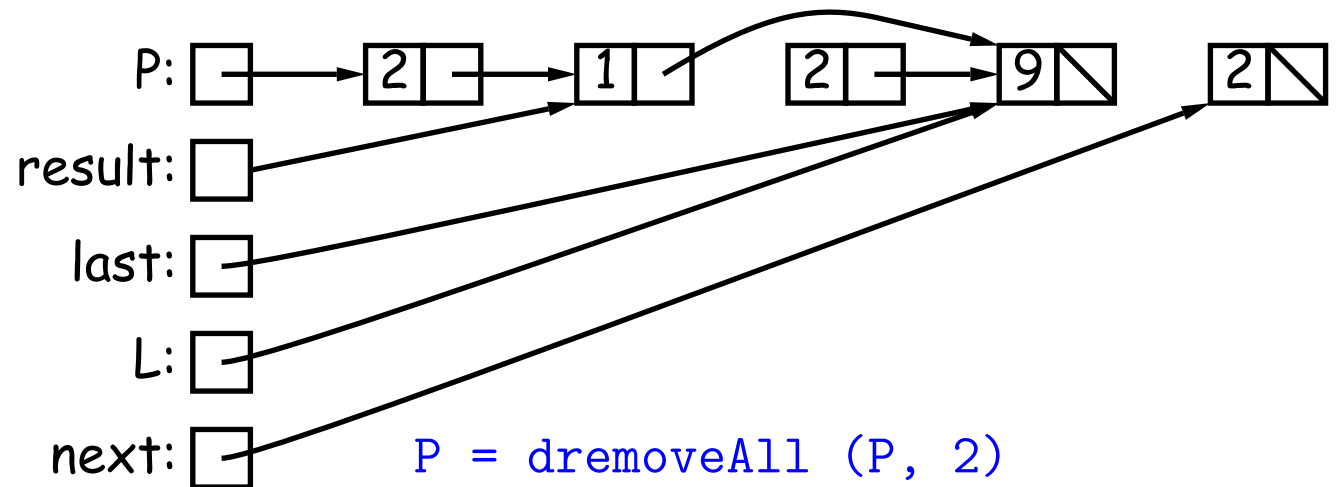
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```



Iterative Destructive Deletion

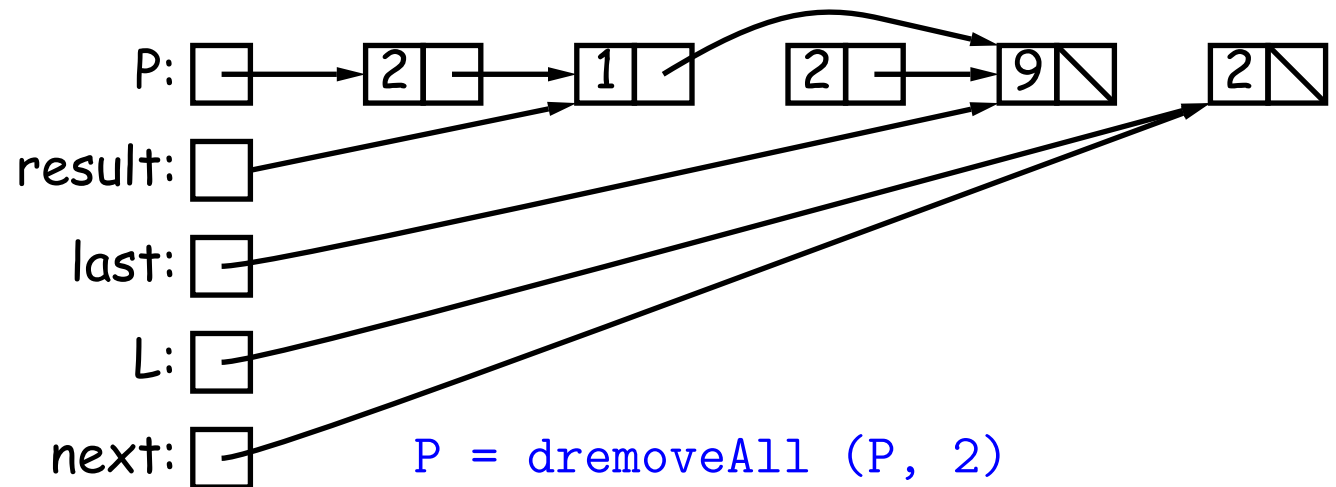
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```



Iterative Destructive Deletion

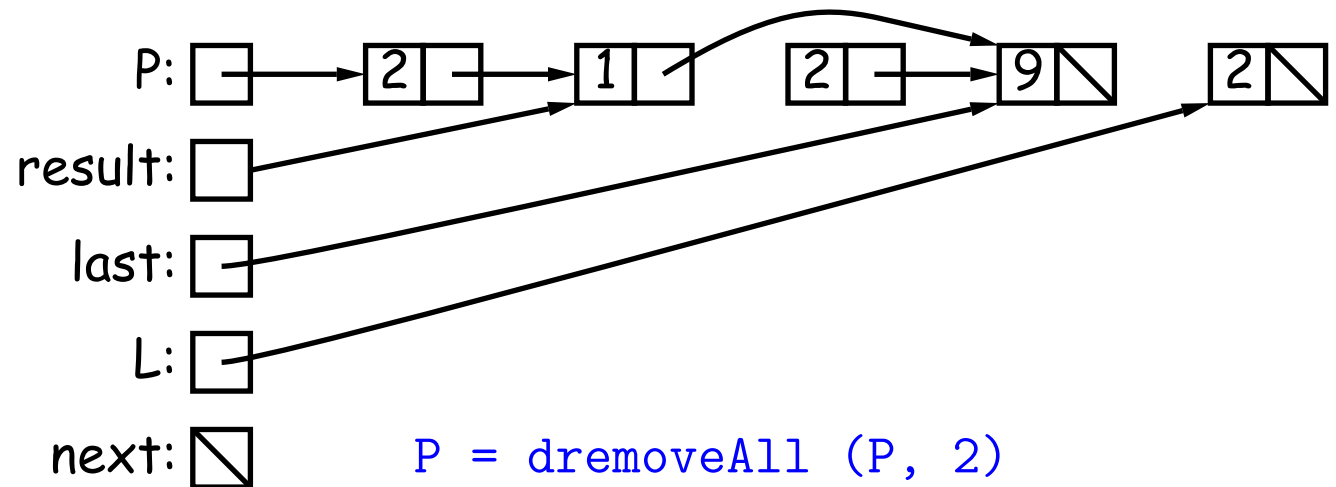
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```



Iterative Destructive Deletion

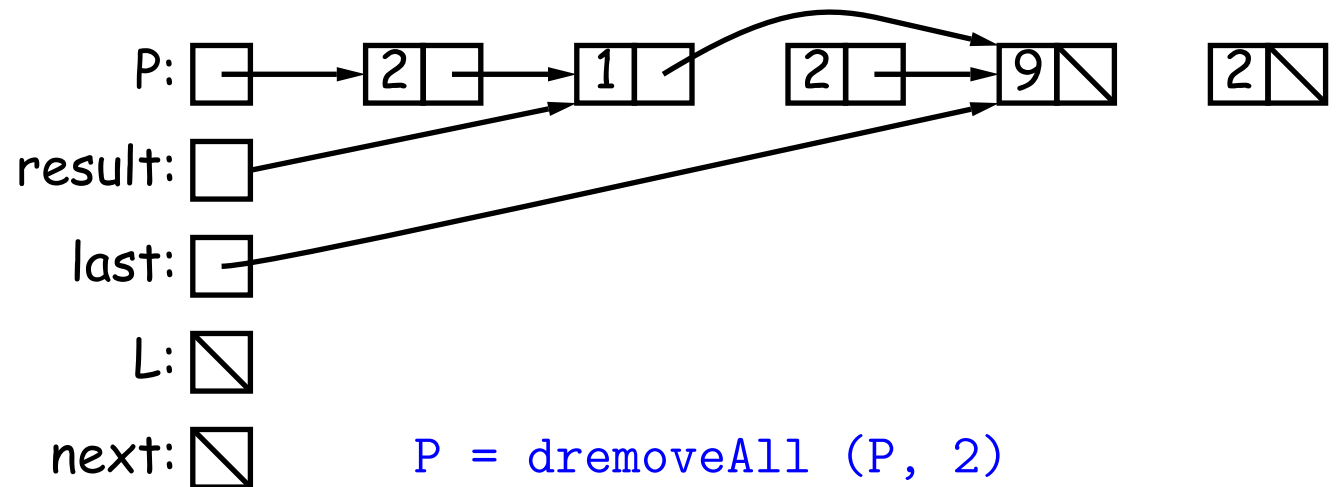
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```



Iterative Destructive Deletion

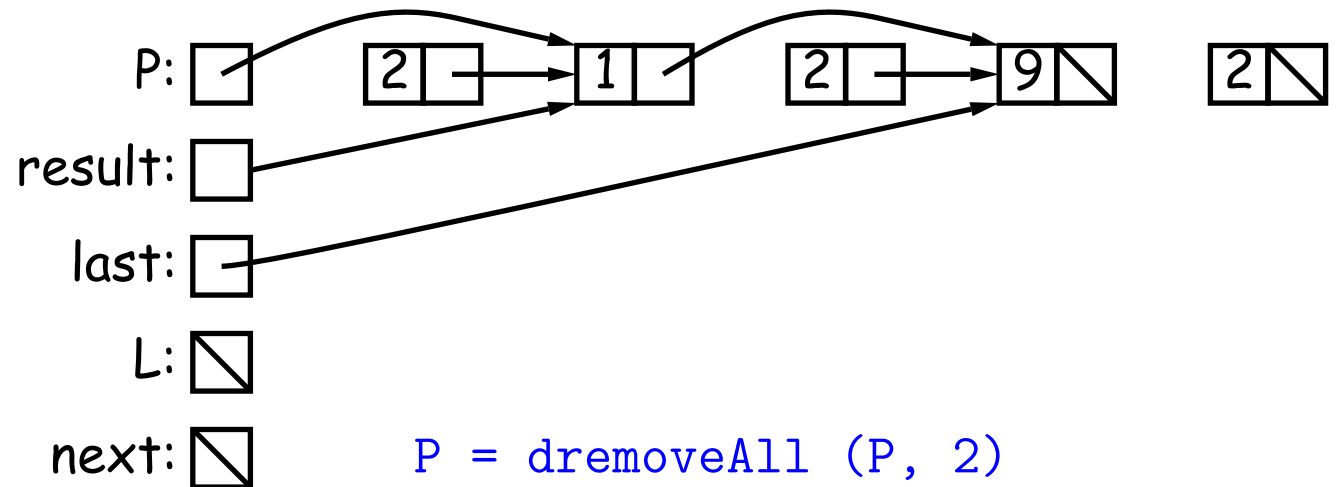
```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}

```



Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {

        // FIXME

    }
    return result;
}
```



`P = dremoveAll (P, 2)`

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
```

```
static IntList dremoveAll(IntList L, int x) {
    IntList result, last, next;
    result = last = null;
    while (L != null) {
        next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```



P = dremoveAll (P, 2)