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UC Berkeley CS61C : Machine Structures

Lecture 26 – Combinational Logic Blocks

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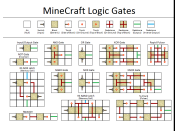
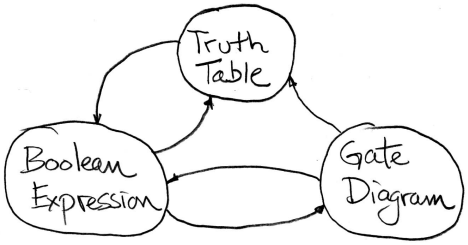
MineCraft Logic Gates ⇒ Using redstone circuits, which are "structures that can be built to active or control mechamisms", you can create all the logic gates using MineCraft.



minecraft.gamepedia.com/Tutorials/Basic_Logic_Gates

Review

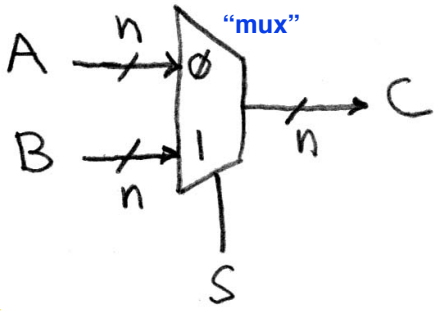
- Use this table and techniques we learned to transform from 1 to another



Today

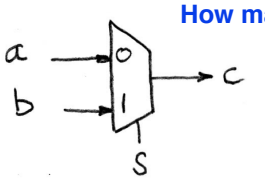
- Data Multiplexors
- Arithmetic and Logic Unit
- Adder/Subtractor

Data Multiplexor (here 2-to-1, n-bit-wide)



N instances of 1-bit-wide mux

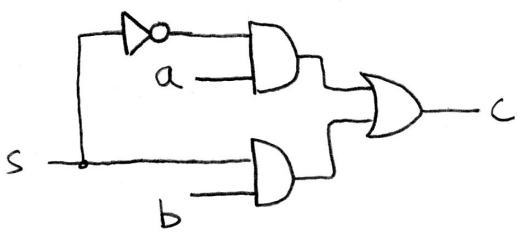
How many rows in TT?



$$
\begin{aligned}
c &= \bar{s}a\bar{b} + \bar{s}ab + s\bar{a}b + sab \\
&= \bar{s}(a\bar{b} + ab) + s(\bar{a}b + ab) \\
&= \bar{s}(a(\bar{b} + b)) + s((\bar{a} + a)b) \\
&= \bar{s}(a(1) + s((1)b) \\
&= \bar{s}a + sb
\end{aligned}
$$

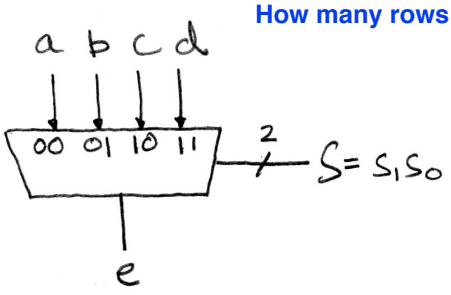
How do we build a 1-bit-wide mux?

$$\bar{s}a + sb$$



4-to-1 Multiplexor?

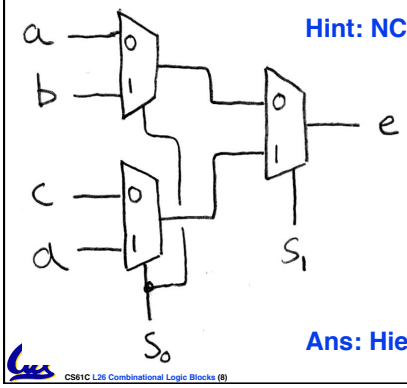
How many rows in TT?



$$e = \overline{s_1}\,\overline{s_0}a + \overline{s_1}s_0b + s_1\overline{s_0}c + s_1s_0d$$

Is there any other way to do it?

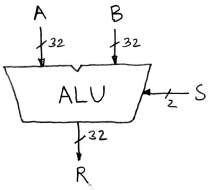
Hint: NCAA tourney!



Ans: Hierarchically!

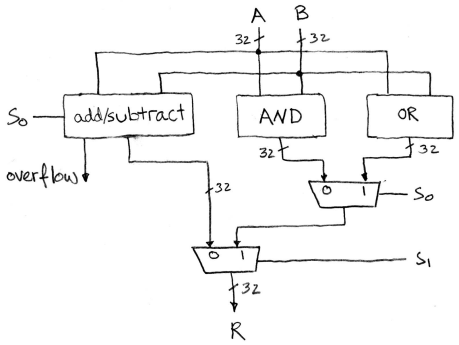
Arithmetic and Logic Unit

- Most processors contain a special logic block called "Arithmetic and Logic Unit" (ALU)
- We'll show you an easy one that does ADD, SUB, bitwise AND, bitwise OR



when S=00, R=A+B
when S=01, R=A-B
when S=10, R=A AND B
when S=11, R=A OR B

Our simple ALU



Administrivia

- How did you find project 2?
  a) Hated it
  b) Disliked it
  c) Neutral
  d) Liked it
  e) Loved it

Adder/Subtracter Design -- how?

- Truth-table, then determine canonical form, then minimize and implement as we've seen before
- Look at breaking the problem down into smaller pieces that we can cascade or hierarchically layer

Adder/Subtracter – One-bit adder LSB…

	a_3	a_2	a_1	a_0
+	b_3	b_2	b_1	b_0
	s_3	s_2	s_1	s_0

a_0	b_0	s_0	c_1
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

$s_0 =$

$c_1 =$

Adder/Subtracter – One-bit adder (1/2)…

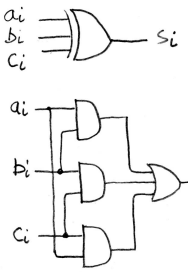
	a_3	a_2	a_1	a_0
+	b_3	b_2	b_1	b_0
	s_3	s_2	s_1	s_0

a_i	b_i	c_i	s_i	c_{i+1}
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

$s_i =$

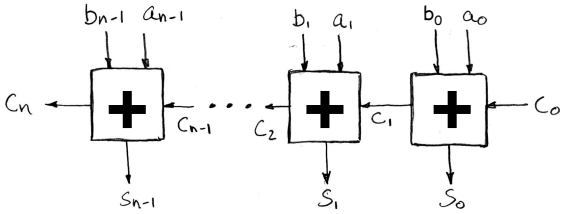
$c_{i+1} =$

Adder/Subtracter – One-bit adder (2/2)…



$$s_i = \text{XOR}(a_i, b_i, c_i)$$
$$c_{i+1} = \text{MAJ}(a_i, b_i, c_i) = a_i b_i + a_i c_i + b_i c_i$$

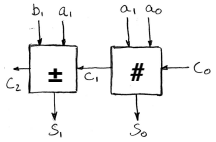
N 1-bit adders ⇒ 1 N-bit adder



What about overflow?
Overflow = c_n?

What about overflow?

- **Consider a 2-bit signed # & overflow:**
  - `10 = -2 + -2 or -1`
  - `11 = -1 + -2 only`
  - `00 = 0 NOTHING!`
  - `01 = 1 + 1 only`

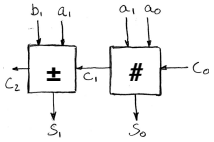


- **Highest adder**
  - **C_1 = Carry-in = C_{in}, C_2 = Carry-out = C_{out}**
  - **No C_{out} or C_{in} ⇒ NO overflow!**
  - **C_{in}, and C_{out} ⇒ NO overflow!**
  - **C_{in}, but no C_{out} ⇒ A,B both > 0, overflow!**
  - **C_{out}, but no C_{in} ⇒ A,B both < 0, overflow!**

What op?

What about overflow?

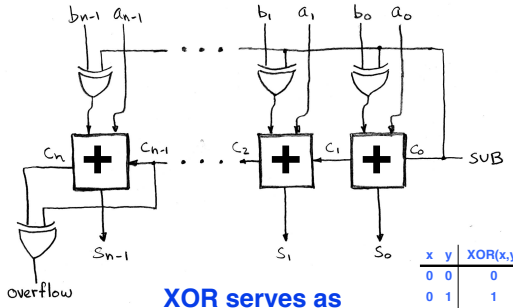
- **Consider a 2-bit signed # & overflow:**
  - `10 = -2`
  - `11 = -1`
  - `00 = 0`
  - `01 = 1`



- **Overflows when…**
  - **C_{in}, but no C_{out} ⇒ A,B both > 0, overflow!**
  - **C_{out}, but no C_{in} ⇒ A,B both < 0, overflow!**

$$\text{overflow} = c_n \text{ XOR } c_{n-1}$$

Extremely Clever Subtractor



x	y	XOR(x,y)
0	0	0
0	1	1
1	0	1
1	1	0

XOR serves as conditional inverter!

Peer Instruction

1) Truth table for mux with 4-bits of signals has 2^4 rows
2) We could cascade N 1-bit shifters to make 1 N-bit shifter for sll, srl

	1	2
a)	F	F
b)	F	T
c)	T	F
d)	T	T

"And In conclusion…"

- Use muxes to select among input
  - S input bits selects 2^S inputs
  - Each input can be n-bits wide, indep of S
- Can implement muxes hierarchically
- ALU can be implemented using a mux
  - Coupled with basic block elements
- N-bit adder-subtractor done using N 1-bit adders with XOR gates on input
  - XOR serves as conditional inverter