

CS 61C:
Great Ideas in Computer Architecture
Amdahl's Law, Data-level Parallelism

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<http://inst.eecs.berkeley.edu/~cs61c/>

New-School Machine Structures (It's a bit more complicated!)

Software

Hardware

- Parallel Requests

Assigned to computer
e.g., Search "Katz"

Warehouse Scale Computer



Smart Phone



- Parallel Threads

Assigned to core
e.g., Lookup, Ads

Harness Parallelism & Achieve High Performance

- Parallel Instructions

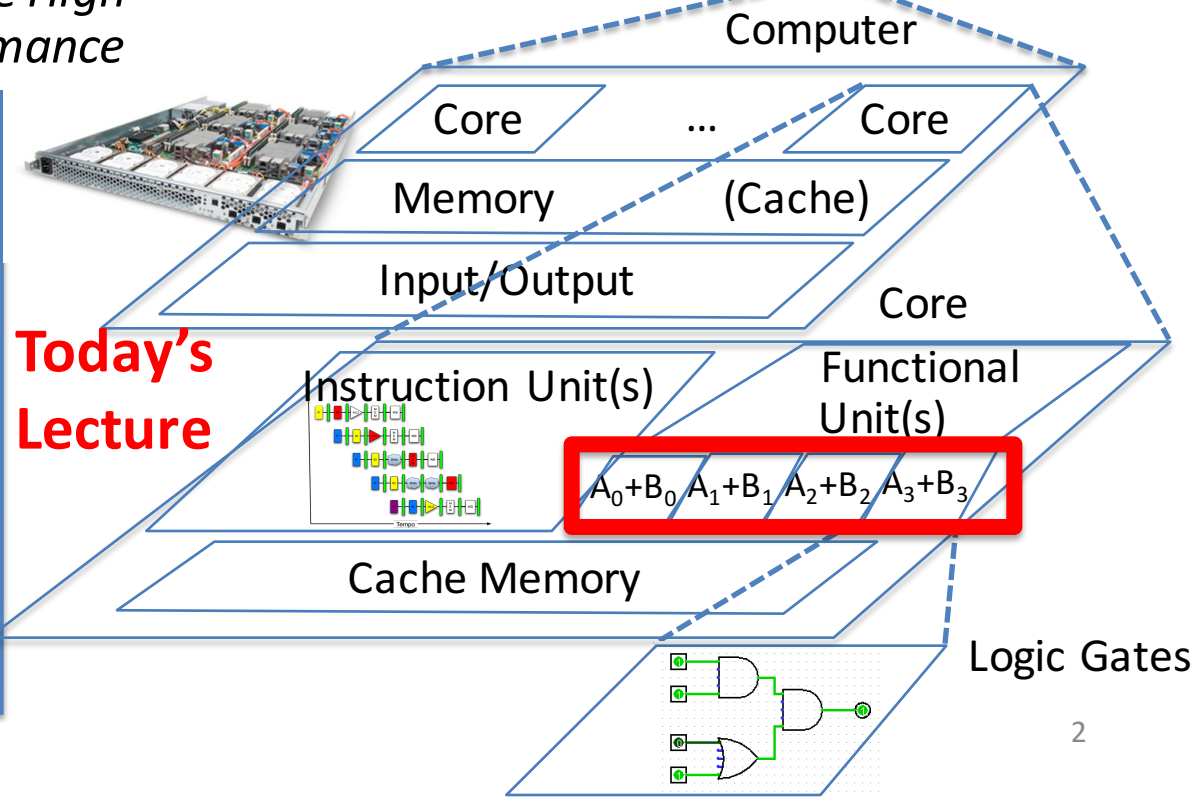
>1 instruction @ one time
e.g., 5 pipelined instructions

- Parallel Data

>1 data item @ one time
e.g., Add of 4 pairs of words



Today's Lecture



- Hardware descriptions

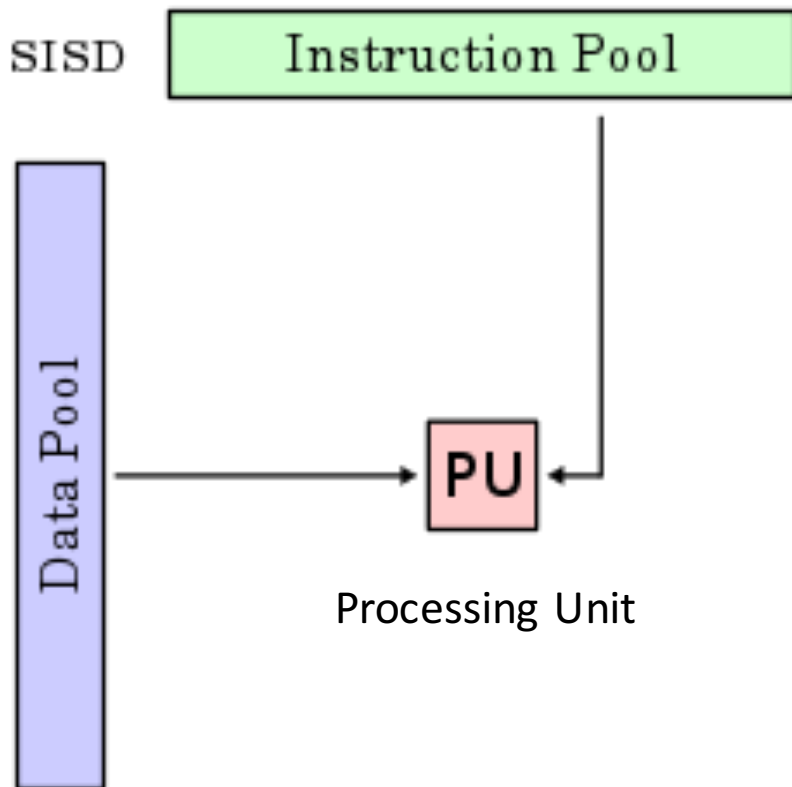
All gates @ one time

- Programming Languages

Using Parallelism for Performance

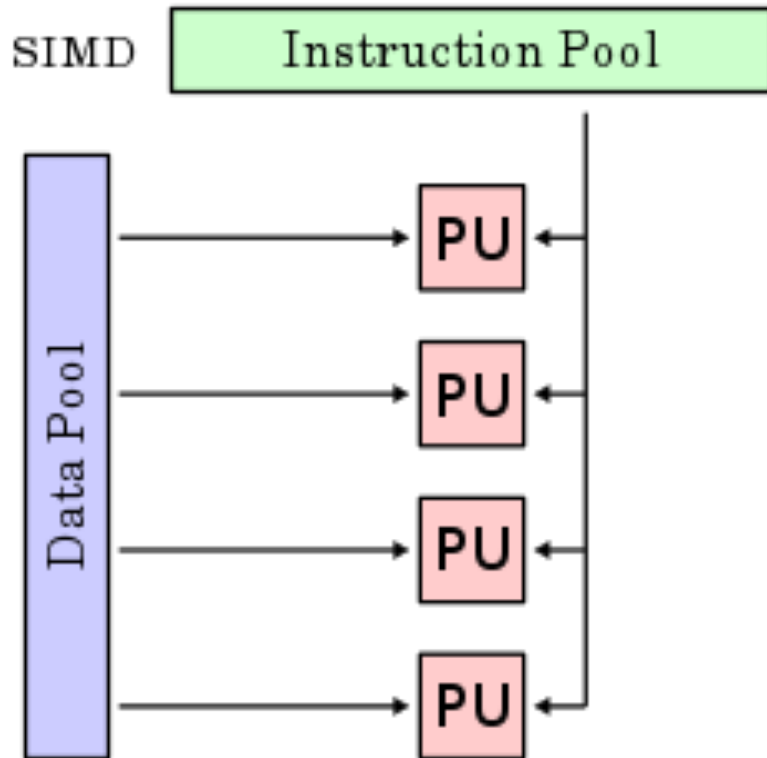
- Two basic ways:
 - Multiprogramming
 - run multiple independent programs in parallel
 - “Easy”
 - Parallel computing
 - run one program faster
 - “Hard”
- We’ll focus on parallel computing for next few lectures

Single-Instruction/Single-Data Stream (SISD)



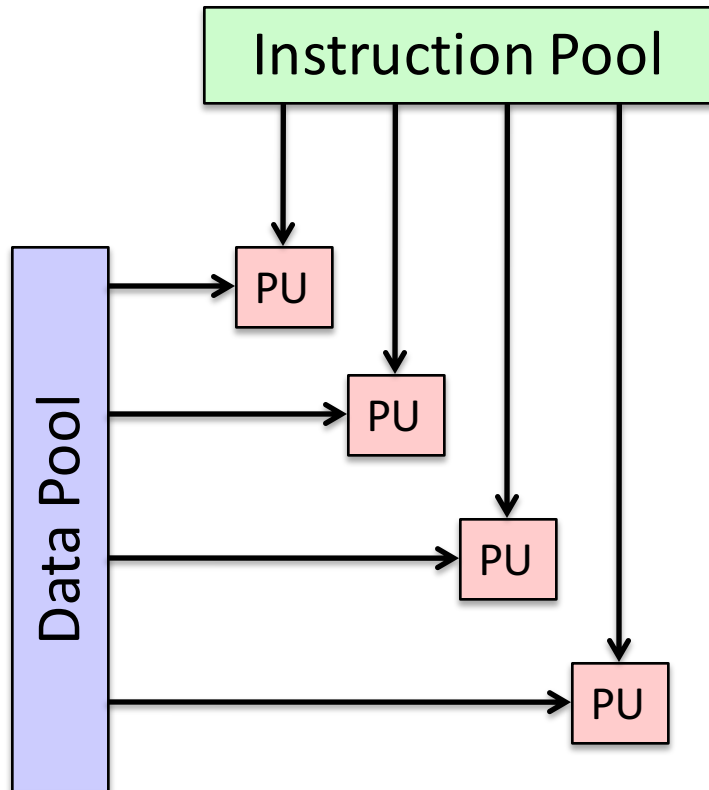
- Sequential computer that exploits no parallelism in either the instruction or data streams. Examples of SISD architecture are traditional uniprocessor machines

Single-Instruction/Multiple-Data Stream (SIMD or “sim-dee”)



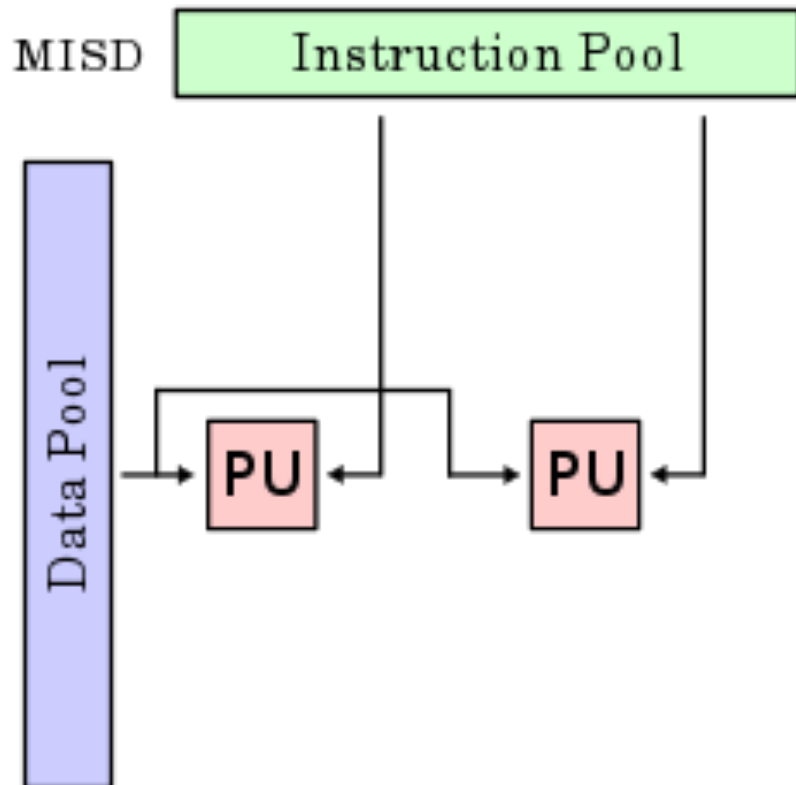
- SIMD computer exploits multiple data streams against a single instruction stream to operations that may be naturally parallelized, e.g., Intel SIMD instruction extensions or NVIDIA Graphics Processing Unit (GPU)

Multiple-Instruction/Multiple-Data Streams (MIMD or “mim-dee”)



- Multiple autonomous processors simultaneously executing different instructions on different data.
 - MIMD architectures include multicore and Warehouse-Scale Computers

Multiple-Instruction/Single-Data Stream (MISD)



- Multiple-Instruction, Single-Data stream computer that exploits multiple instruction streams against a single data stream.
 - Rare, mainly of historical interest only

Flynn* Taxonomy, 1966

		Data Streams	
		Single	Multiple
Instruction Streams	Single	SISD: Intel Pentium 4	SIMD: SSE instructions of x86
	Multiple	MISD: No examples today	MIMD: Intel Xeon e5345 (Clovertown)

- In 2013, SIMD and MIMD most common parallelism in architectures – usually both in same system!
- Most common parallel processing programming style: Single Program Multiple Data (“SPMD”)
 - Single program that runs on all processors of a MIMD
 - Cross-processor execution coordination using synchronization primitives
- SIMD (aka hw-level *data parallelism*): specialized function units, for handling lock-step calculations involving arrays
 - Scientific computing, signal processing, multimedia (audio/video processing)

*Prof. Michael Flynn, Stanford

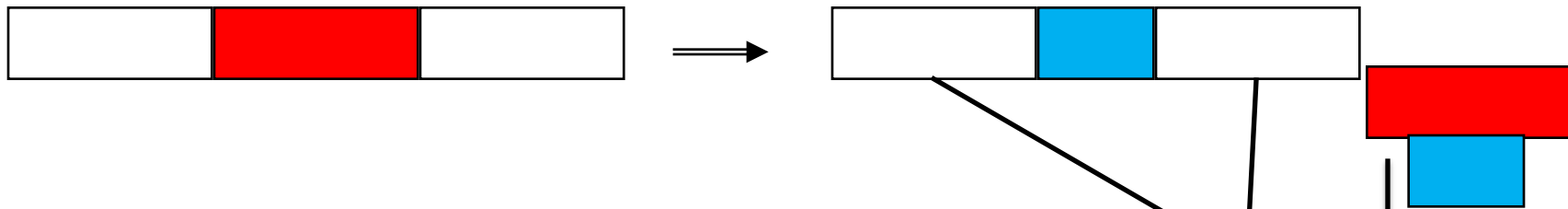


Big Idea: Amdahl's (Heartbreaking) Law

- Speedup due to enhancement E is

$$\text{Speedup w/ E} = \frac{\text{Exec time w/o E}}{\text{Exec time w/ E}}$$

- Suppose that enhancement E accelerates a fraction F (F < 1) of the task by a factor S (S > 1) and the remainder of the task is unaffected



$$\text{Execution Time w/ E} = \text{Execution Time w/o E} \times [(1-F) + F/S]$$

$$\text{Speedup w/ E} = 1 / [(1-F) + F/S]$$

Big Idea: Amdahl's Law

$$\text{Speedup} = \frac{1}{(1 - F) + \frac{F}{S}}$$

Non-speed-up part \rightarrow (1 - F) \leftarrow Speed-up part \leftarrow $\frac{F}{S}$

Example: the execution time of half of the program can be accelerated by a factor of 2.

What is the program speed-up overall?

$$\frac{1}{\frac{0.5 + 0.5}{2}} = \frac{1}{0.5 + 0.25} = 1.33$$

Example #1: Amdahl's Law

$$\text{Speedup } w/ E = 1 / [(1-F) + F/S]$$

- Consider an enhancement which runs 20 times faster but which is only usable 25% of the time

$$\text{Speedup } w/ E = 1 / (.75 + .25/20) = 1.31$$

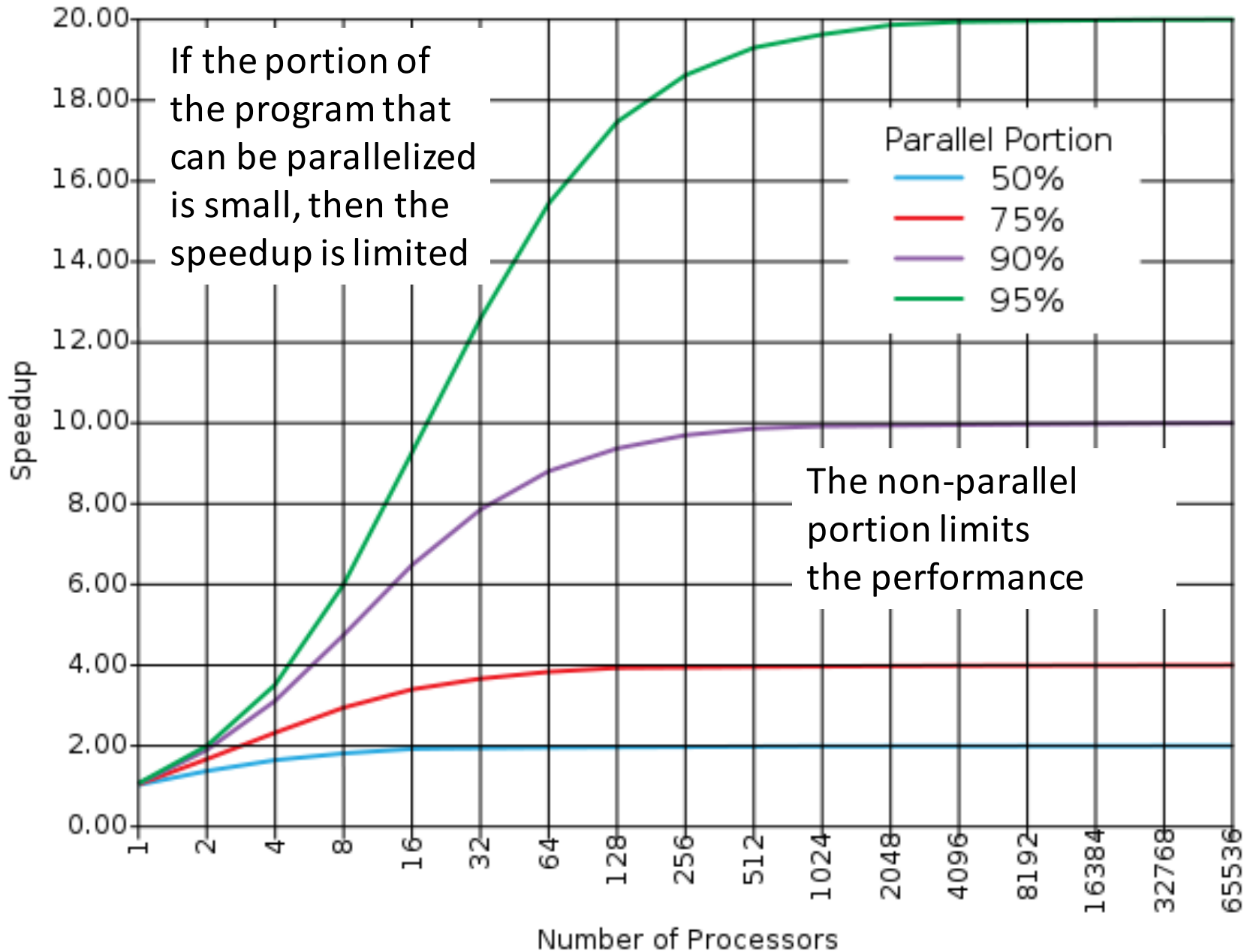
- What if its usable only 15% of the time?

$$\text{Speedup } w/ E = 1 / (.85 + .15/20) = 1.17$$

- Amdahl's Law tells us that to achieve linear speedup with 100 processors, none of the original computation can be scalar!
- To get a speedup of 90 from 100 processors, the percentage of the original program that could be scalar would have to be 0.1% or less

$$\text{Speedup } w/ E = 1 / (.001 + .999/100) = 90.99$$

Amdahl's Law



Strong and Weak Scaling

- To get good speedup on a parallel processor while keeping the problem size fixed is harder than getting good speedup by increasing the size of the problem.
 - *Strong scaling*: when speedup can be achieved on a parallel processor without increasing the size of the problem
 - *Weak scaling*: when speedup is achieved on a parallel processor by increasing the size of the problem proportionally to the increase in the number of processors
- **Load balancing** is another important factor: every processor doing same amount of work
 - Just one unit with twice the load of others cuts speedup almost in half

Clickers/Peer Instruction

Suppose a program spends 80% of its time in a square root routine. How much must you speedup square root to make the program run 5 times faster?

$$\text{Speedup w/ E} = 1 / [(1-F) + F/S]$$

A: 5

B: 16

C: 20

D: 100

E: None of the above

Administrativa

- MT2 is Tue, November 10th:
 - Covers lecture material up till today's lecture
 - Conflict: Email Fred or William by midnight **today**

SIMD Architectures

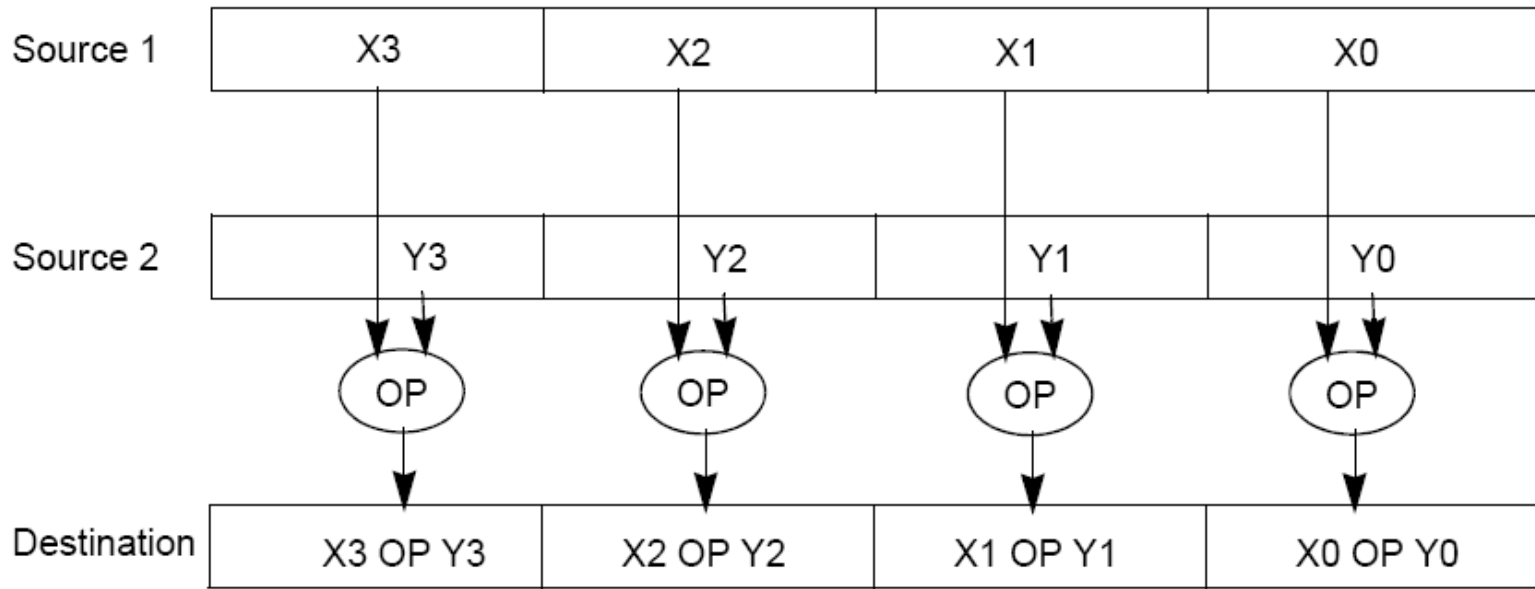
- *Data parallelism*: executing same operation on multiple data streams
- Example to provide context:
 - Multiplying a coefficient vector by a data vector (e.g., in filtering)

$$y[i] := c[i] \times x[i], \quad 0 \leq i < n$$

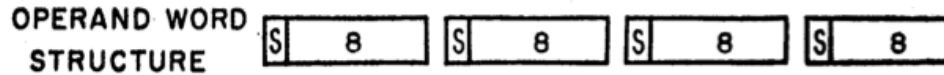
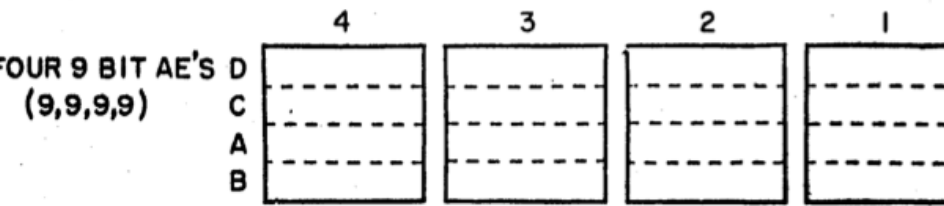
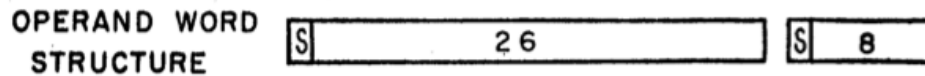
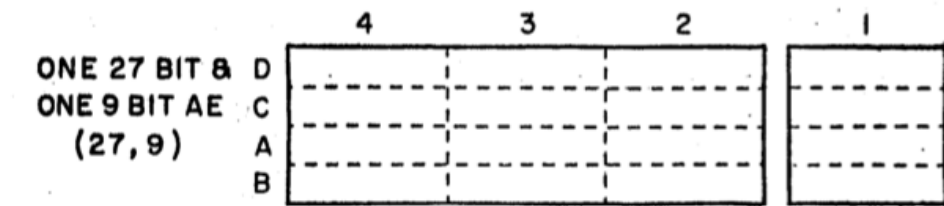
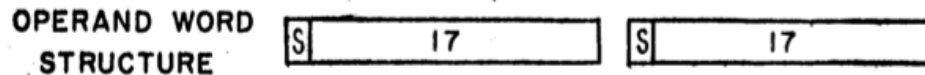
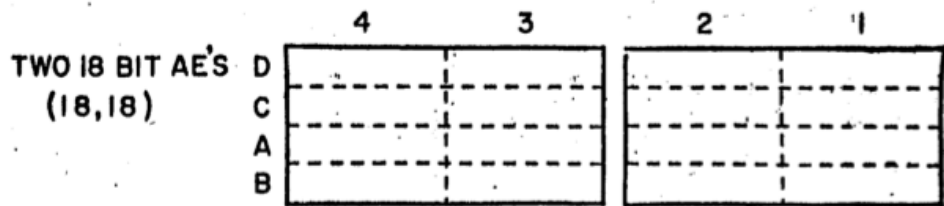
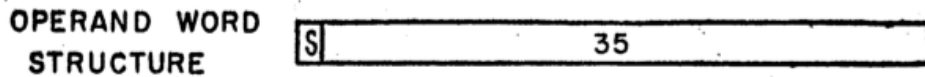
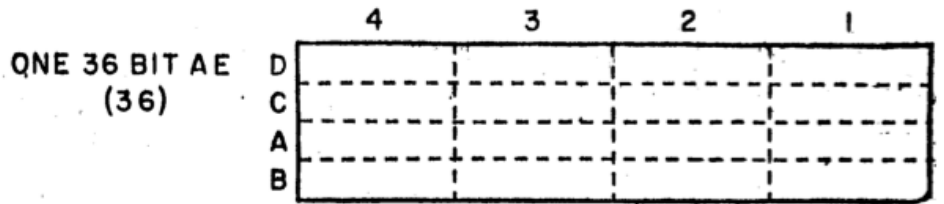
- Sources of performance improvement:
 - One instruction is fetched & decoded for entire operation
 - Multiplications are known to be independent
 - Pipelining/concurrency in memory access as well

Intel “Advanced Digital Media Boost”

- To improve performance, Intel’s SIMD instructions
 - Fetch one instruction, do the work of multiple instructions



First SIMD Extensions: MIT Lincoln Labs TX-2, 1957



Intel SIMD Extensions

- MMX 64-bit registers, reusing floating-point registers [1992]
- SSE2/3/4, new 128-bit registers [1999]
- AVX, new 256-bit registers [2011]
 - Space for expansion to 1024-bit registers

XMM Registers

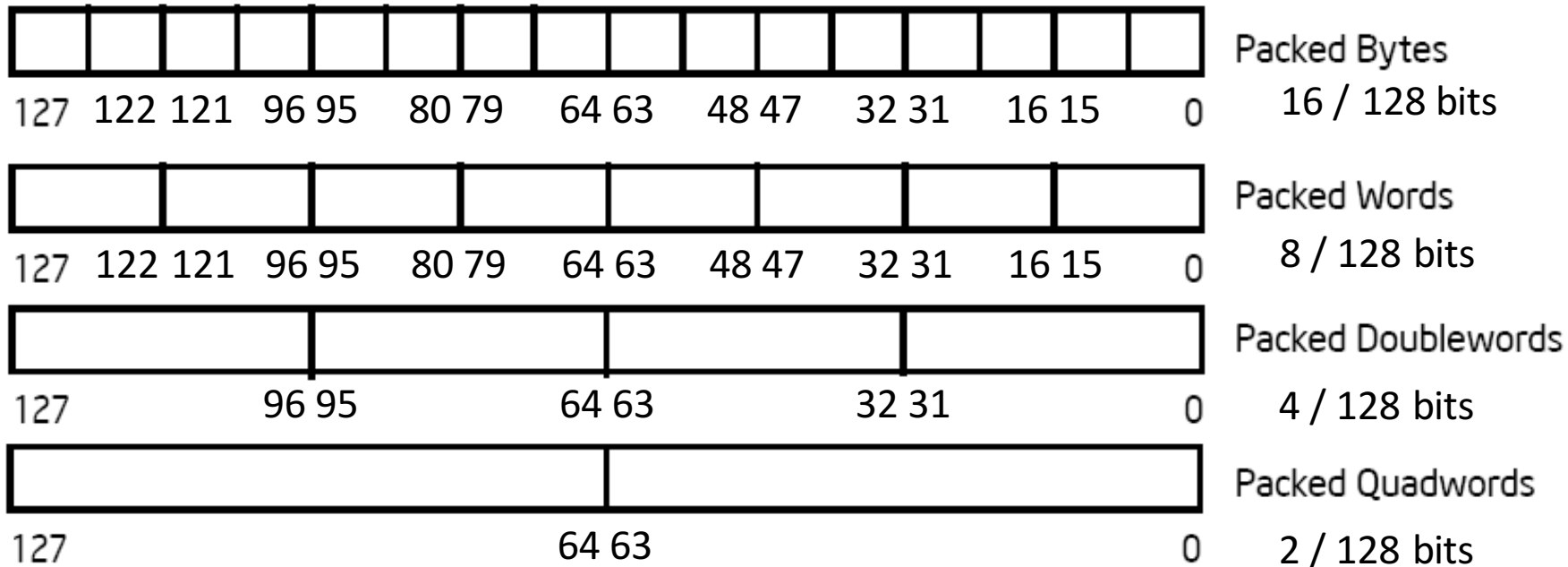
127		0
	XMM7	
	XMM6	
	XMM5	
	XMM4	
	XMM3	
	XMM2	
	XMM1	
	XMM0	

- Architecture extended with eight 128-bit data registers: XMM registers
 - x86 64-bit address architecture adds 8 additional registers (XMM8 – XMM15)

Intel Architecture SSE2+ 128-Bit SIMD Data Types

- Note: in Intel Architecture (unlike MIPS) a word is 16 bits
 - Single-precision FP: Double word (32 bits)
 - Double-precision FP: Quad word (64 bits)

Fundamental 128-Bit Packed SIMD Data Types



SSE/SSE2 Floating Point Instructions

Move
does
both
load
and
store

Data transfer	Arithmetic	Compare
MOV{A/U}{SS/PS/SD/PD} xmm, mem/xmm	ADD{SS/PS/SD/PD} xmm, mem/xmm	CMP{SS/PS/SD/PD}
	SUB{SS/PS/SD/PD} xmm, mem/xmm	
MOV {H/L} {PS/PD} xmm, mem/xmm	MUL{SS/PS/SD/PD} xmm, mem/xmm	
	DIV{SS/PS/SD/PD} xmm, mem/xmm	
	SQRT{SS/PS/SD/PD} mem/xmm	
	MAX {SS/PS/SD/PD} mem/xmm	
	MIN{SS/PS/SD/PD} mem/xmm	

xmm: one operand is a 128-bit SSE2 register

mem/xmm: other operand is in memory or an SSE2 register

{SS} Scalar Single precision FP: one 32-bit operand in a 128-bit register

{PS} Packed Single precision FP: four 32-bit operands in a 128-bit register

{SD} Scalar Double precision FP: one 64-bit operand in a 128-bit register

{PD} Packed Double precision FP, or two 64-bit operands in a 128-bit register

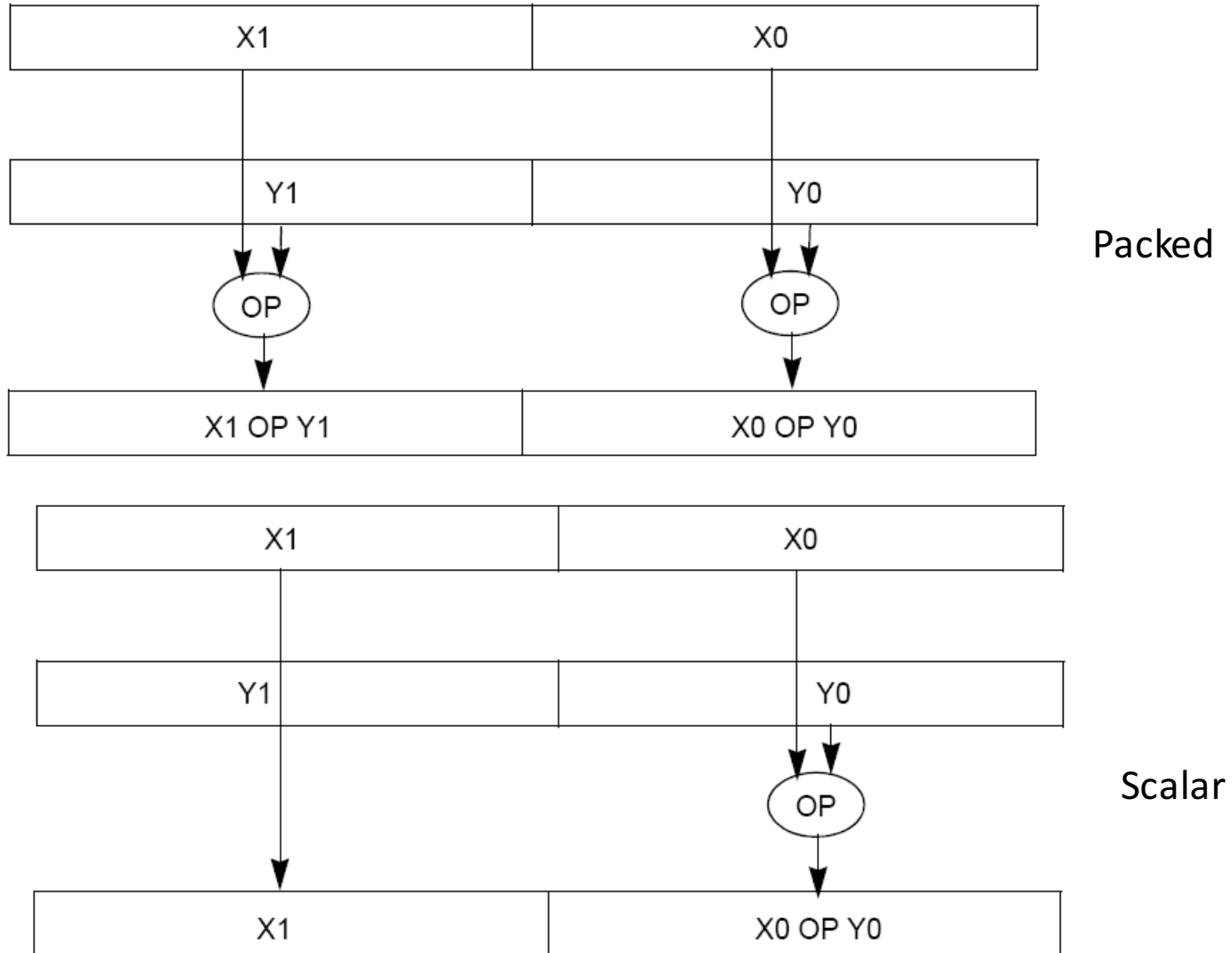
{A} 128-bit operand is aligned in memory

{U} means the 128-bit operand is unaligned in memory

{H} means move the high half of the 128-bit operand

{L} means move the low half of the 128-bit operand

Packed and Scalar Double-Precision Floating-Point Operations



Example: SIMD Array Processing

```
for each f in array  
  f = sqrt(f)
```

```
for each f in array  
{  
  load f to the floating-point register  
  calculate the square root  
  write the result from the register to memory  
}
```

```
{  
for each 4 members in array  
{  
  load 4 members to the SSE register  
  calculate 4 square roots in one operation  
  store the 4 results from the register to memory  
}
```

SIMD style

Data-Level Parallelism and SIMD

- SIMD wants adjacent values in memory that can be operated in parallel
- Usually specified in programs as loops
for(i=1000; i>0; i=i-1)
x[i] = x[i] + s;
- How can reveal more data-level parallelism than available in a single iteration of a loop?
- *Unroll loop* and adjust iteration rate

Looping in MIPS

Assumptions:

- \$t1 is initially the address of the element in the array with the highest address
- \$f0 contains the scalar value s
- 8(\$t2) is the address of the last element to operate on

CODE:

```
Loop: 1. l.d      $f2,0($t1)      ; $f2=array element
      2. add.d   $f10,$f2,$f0     ; add s to $f2
      3. s.d     $f10,0($t1)     ; store result
      4. addiu  $t1,$t1,#-8      ; decrement pointer 8 byte
      5. bne    $t1,$t2,Loop     ;repeat loop if $t1 != $t2
```

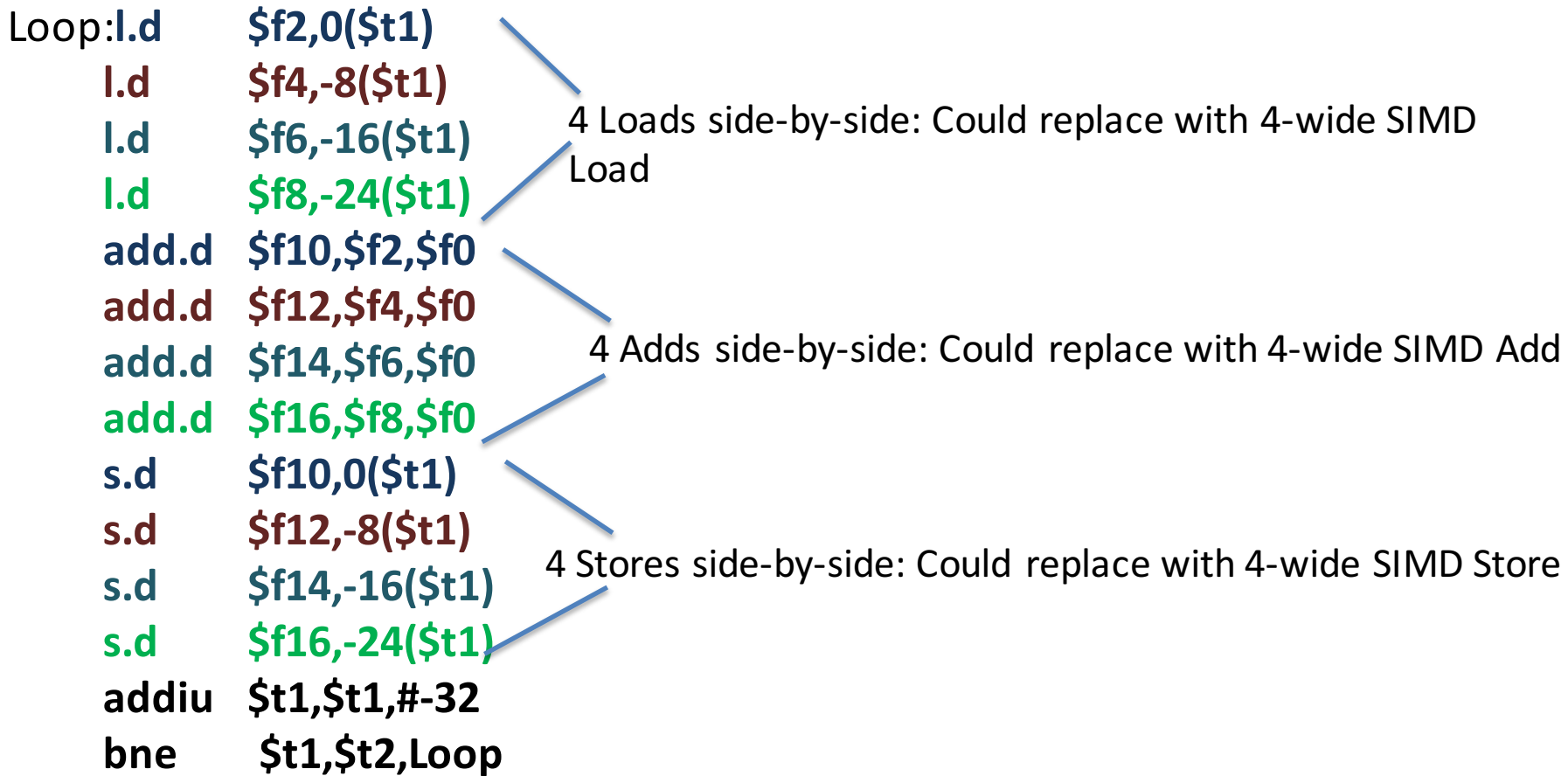
Loop Unrolled

Loop: **l.d** \$f2,0(\$t1)
add.d \$f10,\$f2,\$f0
s.d \$f10,0(\$t1)
l.d \$f4,-8(\$t1)
add.d \$f12,\$f4,\$f0
s.d \$f12,-8(\$t1)
l.d \$f6,-16(\$t1)
add.d \$f14,\$f6,\$f0
s.d \$f14,-16(\$t1)
l.d \$f8,-24(\$t1)
add.d \$f16,\$f8,\$f0
s.d \$f16,-24(\$t1)
addiu \$t1,\$t1,#-32
bne \$t1,\$t2,Loop

NOTE:

1. Only 1 Loop Overhead every 4 iterations
2. This unrolling works if
loop_limit(mod 4) = 0
3. Using different registers for each iteration eliminates data hazards in pipeline

Loop Unrolled Scheduled



Loop Unrolling in C

- Instead of compiler doing loop unrolling, could do it yourself in C

```
for(i=1000; i>0; i=i-1)  
    x[i] = x[i] + s;
```

- Could be rewritten What is downside of doing it in C?

```
for(i=1000; i>0; i=i-4) {  
    x[i] = x[i] + s;  
    x[i-1] = x[i-1] + s;  
    x[i-2] = x[i-2] + s;  
    x[i-3] = x[i-3] + s;  
}
```

Generalizing Loop Unrolling

- A loop of **n iterations**
- **k copies** of the body of the loop
- **Assuming $(n \bmod k) \neq 0$**

Then we will run the loop with 1 copy of the body **$(n \bmod k)$** times and with k copies of the body **$\text{floor}(n/k)$** times

Example: Add Two Single-Precision Floating-Point Vectors

Computation to be performed:

```
vec_res.x = v1.x + v2.x;  
vec_res.y = v1.y + v2.y;  
vec_res.z = v1.z + v2.z;  
vec_res.w = v1.w + v2.w;
```

mov a ps : **move** from mem to XMM register,
memory **aligned**, **packed** single precision

add ps : **add** from mem to XMM register,
packed single precision

SSE Instruction Sequence:

mov a ps : **move** from XMM register to mem,
memory **aligned**, **packed** single precision

(Note: Destination on the right in x86 assembly)

```
movaps address-of-v1, %xmm0
```

```
// v1.w | v1.z | v1.y | v1.x -> xmm0
```

```
addps address-of-v2, %xmm0
```

```
// v1.w+v2.w | v1.z+v2.z | v1.y+v2.y | v1.x+v2.x ->
```

```
xmm0
```

```
movaps %xmm0, address-of-vec_res
```

In The News: Intel acquired Altera

- Altera is 2nd biggest FPGA maker after Xilinx
 - FPGA (Field-Programmable Gate Array)
- Altera already has fabrication deal to use Intel's 14nm technology
- Intel experimenting with FPGA next to server processor
- Microsoft to use programmable logic chips to accelerate Bing search engine

Break

- Come join [CSUA Hackathon](#)!! Form teams of 4, hack, and win awesome prizes! Prizes include monitors, headsets, and more! Delicious food will be served throughout, including some secret midnight goodies!
- Register your team day-of and write a good description of your project (1-2 sentences).
Hackathon starts from 6PM on October 30th - 2PM, October 31st.
See you there!
- Also, feel free to join CSUA's General Meeting #2 to listen and network with Jeff Atwood, our speaker, and socialize with other people from the CS community.

Intel SSE Intrinsics

- Intrinsics are C functions and procedures for inserting assembly language into C code, including SSE instructions
 - With intrinsics, can program using these instructions indirectly
 - One-to-one correspondence between SSE instructions and intrinsics

Example SSE Intrinsics

Intrinsics:

Corresponding SSE instructions:

- Vector data type:

`_m128d`

- Load and store operations:

`_mm_load_pd`

MOVAPD/aligned, packed double

`_mm_store_pd`

MOVAPD/aligned, packed double

`_mm_loadu_pd`

MOVUPD/unaligned, packed double

`_mm_storeu_pd`

MOVUPD/unaligned, packed double

- Load and broadcast across vector

`_mm_load1_pd`

MOVSD + shuffling/duplicating

- Arithmetic:

`_mm_add_pd`

ADDPD/add, packed double

`_mm_mul_pd`

MULPD/multiple, packed double

Example: 2 x 2 Matrix Multiply

Definition of Matrix Multiply:

$$C_{i,j} = (A \times B)_{i,j} = \sum_{k=1}^2 A_{i,k} \times B_{k,j}$$

$$\begin{bmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{bmatrix} \times \begin{bmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{bmatrix} = \begin{bmatrix} C_{1,1} & C_{1,2} \\ C_{2,1} & C_{2,2} \end{bmatrix}$$

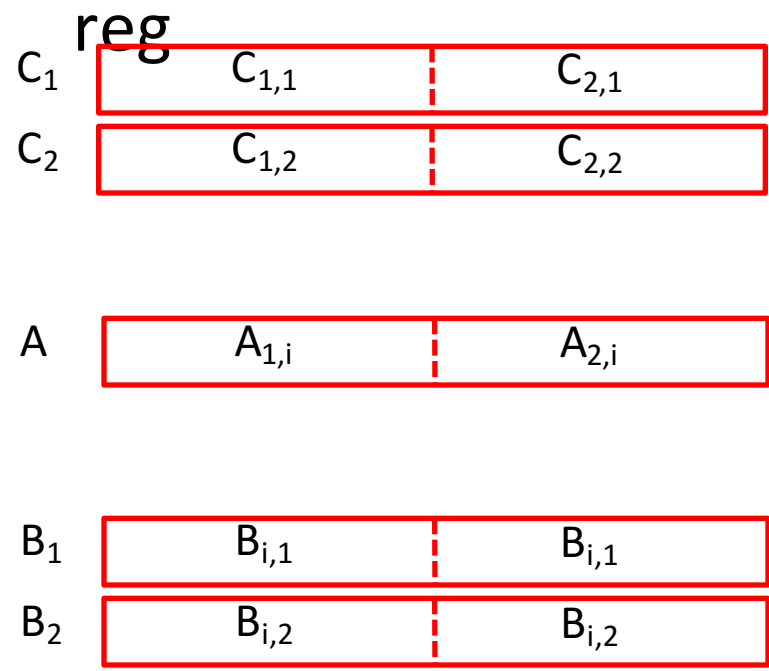
$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix} = \begin{bmatrix} C_{1,1} & C_{1,2} \\ C_{2,1} & C_{2,2} \end{bmatrix}$$

$$\begin{bmatrix} C_{1,1} = A_{1,1}B_{1,1} + A_{1,2}B_{2,1} & C_{1,2} = A_{1,1}B_{1,2} + A_{1,2}B_{2,2} \\ C_{2,1} = A_{2,1}B_{1,1} + A_{2,2}B_{2,1} & C_{2,2} = A_{2,1}B_{1,2} + A_{2,2}B_{2,2} \end{bmatrix}$$

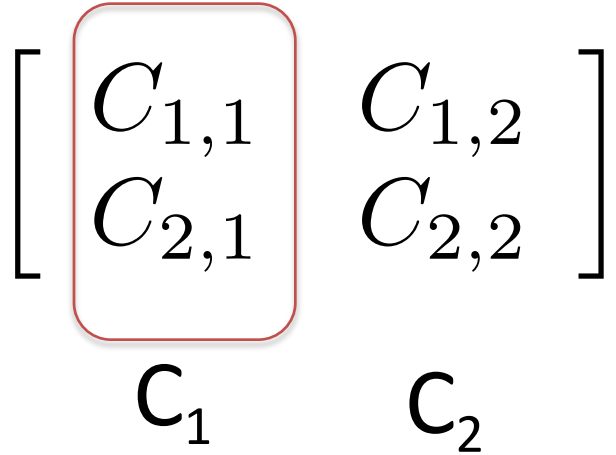
$$\begin{bmatrix} C_{1,1} = 1*1 + 0*2 = 1 & C_{1,2} = 1*3 + 0*4 = 3 \\ C_{2,1} = 0*1 + 1*2 = 2 & C_{2,2} = 0*3 + 1*4 = 4 \end{bmatrix}$$

Example: 2 x 2 Matrix Multiply

- Using the XMM registers
 - 64-bit/double precision/two doubles per XMM



Stored in memory in Column order



Example: 2 x 2 Matrix Multiply

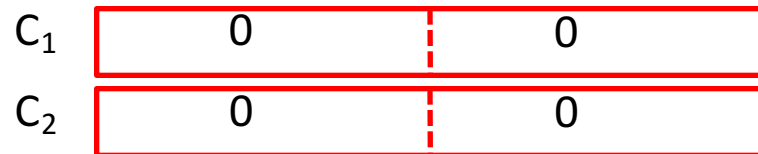
- Initialization

C_1	0	0
C_2	0	0

Example: 2 x 2 Matrix Multiply

$$\begin{bmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{bmatrix} \times \begin{bmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{bmatrix} = \begin{bmatrix} C_{1,1} = A_{1,1}B_{1,1} + A_{1,2}B_{2,1} & C_{1,2} = A_{1,1}B_{1,2} + A_{1,2}B_{2,2} \\ C_{2,1} = A_{2,1}B_{1,1} + A_{2,2}B_{2,1} & C_{2,2} = A_{2,1}B_{1,2} + A_{2,2}B_{2,2} \end{bmatrix}$$

- Initialization



- l = 1



`_mm_load_pd`: Load 2 doubles into XMM reg, Stored in memory in Column order



`_mm_load1_pd`: SSE instruction that loads a double word and stores it in the high and low double words of the XMM register (duplicates value in both halves of XMM)



Example: 2 x 2 Matrix Multiply

$$\begin{bmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{bmatrix} \times \begin{bmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{bmatrix} = \begin{bmatrix} C_{1,1} = A_{1,1}B_{1,1} + A_{1,2}B_{2,1} & C_{1,2} = A_{1,1}B_{1,2} + A_{1,2}B_{2,2} \\ C_{2,1} = A_{2,1}B_{1,1} + A_{2,2}B_{2,1} & C_{2,2} = A_{2,1}B_{1,2} + A_{2,2}B_{2,2} \end{bmatrix}$$

- First iteration intermediate result

$$\begin{array}{l} C_1 \\ C_2 \end{array} \begin{array}{|c|c|} \hline 0 + A_{1,1}B_{1,1} & 0 + A_{2,1}B_{1,1} \\ \hline 0 + A_{1,1}B_{1,2} & 0 + A_{2,1}B_{1,2} \\ \hline \end{array}$$

`c1 = _mm_add_pd(c1, _mm_mul_pd(a, b1));`
`c2 = _mm_add_pd(c2, _mm_mul_pd(a, b2));`
 SSE instructions first do parallel multiplies and then parallel adds in XMM registers

- $i = 1$

$$A \begin{array}{|c|c|} \hline A_{1,1} & A_{2,1} \\ \hline \end{array}$$

`_mm_load_pd`: Stored in memory in Column order

$$B_1 \begin{array}{|c|c|} \hline B_{1,1} & B_{1,1} \\ \hline \end{array}$$

$$B_2 \begin{array}{|c|c|} \hline B_{1,2} & B_{1,2} \\ \hline \end{array}$$

`_mm_load1_pd`: SSE instruction that loads a double word and stores it in the high and low double words of the XMM register (duplicates value in both halves of XMM)

Example: 2 x 2 Matrix Multiply

$$\begin{bmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{bmatrix} \times \begin{bmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{bmatrix} = \begin{bmatrix} C_{1,1} & C_{1,2} \\ C_{2,1} & C_{2,2} \end{bmatrix}$$

$C_{1,1} = A_{1,1}B_{1,1} + A_{1,2}B_{2,1}$ $C_{1,2} = A_{1,1}B_{1,2} + A_{1,2}B_{2,2}$
 $C_{2,1} = A_{2,1}B_{1,1} + A_{2,2}B_{2,1}$ $C_{2,2} = A_{2,1}B_{1,2} + A_{2,2}B_{2,2}$

- First iteration intermediate result

$$\begin{array}{l} C_1 \\ C_2 \end{array}
 \begin{array}{|c|c|} \hline 0 + A_{1,1}B_{1,1} & 0 + A_{2,1}B_{1,1} \\ \hline 0 + A_{1,1}B_{1,2} & 0 + A_{2,1}B_{1,2} \\ \hline \end{array}$$

`c1 = _mm_add_pd(c1, _mm_mul_pd(a, b1));`
`c2 = _mm_add_pd(c2, _mm_mul_pd(a, b2));`
 SSE instructions first do parallel multiplies and then parallel adds in XMM registers

- $l = 2$

$$A \begin{array}{|c|c|} \hline A_{1,2} & A_{2,2} \\ \hline \end{array}$$

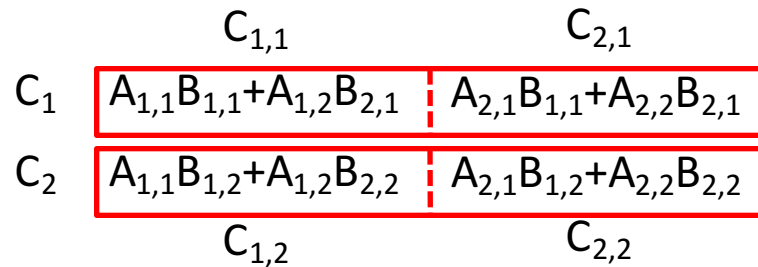
`_mm_load_pd`: Stored in memory in Column order

$$\begin{array}{l} B_1 \\ B_2 \end{array}
 \begin{array}{|c|c|} \hline B_{2,1} & B_{2,1} \\ \hline B_{2,2} & B_{2,2} \\ \hline \end{array}$$

`_mm_load1_pd`: SSE instruction that loads a double word and stores it in the high and low double words of the XMM register (duplicates value in both halves of XMM)

Example: 2 x 2 Matrix Multiply

- Second iteration intermediate result



`c1 = _mm_add_pd(c1, _mm_mul_pd(a, b1));`
`c2 = _mm_add_pd(c2, _mm_mul_pd(a, b2));`
 SSE instructions first do parallel multiplies and then parallel adds in XMM registers

- $l = 2$



`_mm_load_pd`: Stored in memory in Column order



`_mm_load1_pd`: SSE instruction that loads a double word and stores it in the high and low double words of the XMM register (duplicates value in both halves of XMM)



Example: 2 x 2 Matrix Multiply (Part 1 of 2)

```
#include <stdio.h>
// header file for SSE compiler intrinsics
#include <emmintrin.h>

// NOTE: vector registers will be represented in
// comments as v1 = [ a | b ]
// where v1 is a variable of type __m128d and
// a, b are doubles

int main(void) {
    // allocate A,B,C aligned on 16-byte boundaries
    double A[4] __attribute__((aligned (16)));
    double B[4] __attribute__((aligned (16)));
    double C[4] __attribute__((aligned (16)));
    int lda = 2;
    int i = 0;
    // declare several 128-bit vector variables
    __m128d c1,c2,a,b1,b2;
```

```
// Initialize A, B, C for example
/* A = (note column order!)
    1 0
    0 1
*/
A[0] = 1.0; A[1] = 0.0; A[2] = 0.0; A[3] = 1.0;

/* B = (note column order!)
    1 3
    2 4
*/
B[0] = 1.0; B[1] = 2.0; B[2] = 3.0; B[3] = 4.0;

/* C = (note column order!)
    0 0
    0 0
*/
C[0] = 0.0; C[1] = 0.0; C[2] = 0.0; C[3] = 0.0;
```

Example: 2 x 2 Matrix Multiply (Part 2 of 2)

```
// used aligned loads to set
// c1 = [c_11 | c_21]
c1 = _mm_load_pd(C+0*lda);
// c2 = [c_12 | c_22]
c2 = _mm_load_pd(C+1*lda);

for (i = 0; i < 2; i++) {
    /* a =
    i = 0: [a_11 | a_21]
    i = 1: [a_12 | a_22]
    */
    a = _mm_load_pd(A+i*lda);
    /* b1 =
    i = 0: [b_11 | b_11]
    i = 1: [b_21 | b_21]
    */
    b1 = _mm_load1_pd(B+i*0*lda);
    /* b2 =
    i = 0: [b_12 | b_12]
    i = 1: [b_22 | b_22]
    */
    b2 = _mm_load1_pd(B+i+1*lda);
```

```
    /* c1 =
    i = 0: [c_11 + a_11*b_11 | c_21 + a_21*b_11]
    i = 1: [c_11 + a_21*b_21 | c_21 + a_22*b_21]
    */
    c1 = _mm_add_pd(c1, _mm_mul_pd(a, b1));
    /* c2 =
    i = 0: [c_12 + a_11*b_12 | c_22 + a_21*b_12]
    i = 1: [c_12 + a_21*b_22 | c_22 + a_22*b_22]
    */
    c2 = _mm_add_pd(c2, _mm_mul_pd(a, b2));
}

// store c1, c2 back into C for completion
_mm_store_pd(C+0*lda, c1);
_mm_store_pd(C+1*lda, c2);

// print C
printf("%g,%g\n%g,%g\n", C[0], C[2], C[1], C[3]);
return 0;
}
```

Inner loop from gcc -O -S

```
L2: movapd    (%rax,%rsi), %xmm1 //Load aligned A[i,i+1]->m1
    movddup  (%rdx), %xmm0      //Load B[j], duplicate->m0
    mulpd    %xmm1, %xmm0      //Multiply m0*m1->m0
    addpd    %xmm0, %xmm3      //Add m0+m3->m3
    movddup  16(%rdx), %xmm0    //Load B[j+1], duplicate->m0
    mulpd    %xmm0, %xmm1      //Multiply m0*m1->m1
    addpd    %xmm1, %xmm2      //Add m1+m2->m2
    addq     $16, %rax          // rax+16 -> rax (i+=2)
    addq     $8, %rdx          // rdx+8 -> rdx (j+=1)
    cmpq    $32, %rax         // rax == 32?
    jne     L2                // jump to L2 if not equal
    movapd  %xmm3, (%rcx)     //store aligned m3 into C[k,k+1]
    movapd  %xmm2, (%rdi)     //store aligned m2 into C[l,l+1]
```

And in Conclusion, ...

- Amdahl's Law: Serial sections limit speedup
- Flynn Taxonomy
- Intel SSE SIMD Instructions
 - Exploit data-level parallelism in loops
 - One instruction fetch that operates on multiple operands simultaneously
 - 128-bit XMM registers
- SSE Instructions in C
 - Embed the SSE machine instructions directly into C programs through use of intrinsics
 - Achieve efficiency beyond that of optimizing compiler